NAG Library Routine Document

C09EAF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

C09EAF computes the two-dimensional discrete wavelet transform (DWT) at a single level. The initialization routine C09ABF must be called first to set up the DWT options.

2 Specification

```
SUBROUTINE CO9EAF (M, N, A, LDA, CA, LDCA, CH, LDCH, CV, LDCV, CD, LDCD, ICOMM, IFAIL)

INTEGER

M, N, LDA, LDCA, LDCH, LDCV, LDCD, ICOMM(180), IFAIL

REAL (KIND=nag_wp) A(LDA,N), CA(LDCA,*), CH(LDCH,*), CV(LDCV,*), &

CD(LDCD,*)
```

3 Description

C09EAF computes the two-dimensional DWT of a given input data array, considered as a matrix A, at a single level. For a chosen wavelet filter pair, the output coefficients are obtained by applying convolution and downsampling by two to the input, A, first over columns and then to the result over rows. The matrix of approximation (or smooth) coefficients, C_a , is produced by the low pass filter over columns and rows; the matrix of horizontal coefficients, C_h , is produced by the high pass filter over columns and the low pass filter over rows; the matrix of vertical coefficients, C_v , is produced by the low pass filter over columns and rows and the matrix of diagonal coefficients, C_d , is produced by the high pass filter over columns and rows. To reduce distortion effects at the ends of the data array, several end extension methods are commonly used. Those provided are: periodic or circular convolution end extension, half-point symmetric end extension, whole-point symmetric end extension and zero end extension. The total number, n_{ct} , of coefficients computed for C_a , C_h , C_v , and C_d together and the number of columns of each coefficients matrix, n_{cn} , are returned by the initialization routine C09ABF. These values can be used to calculate the number of rows of each coefficients matrix, n_{cm} , using the formula $n_{cm} = n_{ct}/(4n_{cn})$.

4 References

Daubechies I (1992) Ten Lectures on Wavelets SIAM, Philadelphia

5 Arguments

1: M – INTEGER Input

On entry: number of rows, m, of data matrix A.

Constraint: this must be the same as the value M passed to the initialization routine C09ABF.

2: N – INTEGER Input

On entry: number of columns, n, of data matrix A.

Constraint: this must be the same as the value N passed to the initialization routine C09ABF.

3: A(LDA, N) - REAL (KIND=nag_wp) array

On entry: the m by n data matrix A.

Mark 26 C09EAF.1

C09EAF NAG Library Manual

4: LDA – INTEGER Input

On entry: the first dimension of the array A as declared in the (sub)program from which C09EAF is called.

Constraint: LDA \geq M.

5: CA(LDCA,*) - REAL (KIND=nag_wp) array

Output

Note: the second dimension of the array CA must be at least n_{cn} where n_{cn} is the argument NWCN returned by routine C09ABF.

On exit: contains the $n_{\rm cm}$ by $n_{\rm cn}$ matrix of approximation coefficients, C_a .

6: LDCA – INTEGER

Input

On entry: the first dimension of the array CA as declared in the (sub)program from which C09EAF is called.

Constraint: LDCA $\geq n_{\rm cm}$ where $n_{\rm cm} = n_{\rm ct}/(4n_{\rm cn})$ and $n_{\rm cn}$, $n_{\rm ct}$ are returned by the initialization routine C09ABF.

7: CH(LDCH, *) - REAL (KIND=nag wp) array

Output

Note: the second dimension of the array CH must be at least $n_{\rm cn}$ where $n_{\rm cn}$ is the argument NWCN returned by routine C09ABF.

On exit: contains the n_{cm} by n_{cn} matrix of horizontal coefficients, C_h .

8: LDCH - INTEGER

Input

On entry: the first dimension of the array CH as declared in the (sub)program from which C09EAF is called.

Constraint: LDCH $\geq n_{\rm cm}$ where $n_{\rm cm} = n_{\rm ct}/(4n_{\rm cn})$ and $n_{\rm cn}$, $n_{\rm ct}$ are returned by the initialization routine C09ABF.

9: CV(LDCV, *) - REAL (KIND=nag wp) array

Output

Note: the second dimension of the array CV must be at least n_{cn} where n_{cn} is the argument NWCN returned by routine C09ABF.

On exit: contains the $n_{\rm cm}$ by $n_{\rm cn}$ matrix of vertical coefficients, C_v .

10: LDCV - INTEGER

Input

On entry: the first dimension of the array CV as declared in the (sub)program from which C09EAF is called.

Constraint: LDCV $\geq n_{\rm cm}$ where $n_{\rm cm} = n_{\rm ct}/(4n_{\rm cn})$ and $n_{\rm cn}$, $n_{\rm ct}$ are returned by the initialization routine C09ABF.

11: CD(LDCD, *) - REAL (KIND=nag_wp) array

Output

Note: the second dimension of the array CD must be at least n_{cn} where n_{cn} is the argument NWCN returned by routine C09ABF.

On exit: contains the n_{cm} by n_{cn} matrix of diagonal coefficients, C_d .

12: LDCD – INTEGER

Input

On entry: the first dimension of the array CD as declared in the (sub)program from which C09EAF is called.

Constraint: LDCD $\geq n_{\rm cm}$ where $n_{\rm cm} = n_{\rm ct}/(4n_{\rm cn})$ and $n_{\rm cn}$, $n_{\rm ct}$ are returned by the initialization routine C09ABF.

C09EAF.2 Mark 26

13: ICOMM(180) – INTEGER array

Communication Array

On entry: contains details of the discrete wavelet transform and the problem dimension as setup in the call to the initialization routine C09ABF.

14: IFAIL - INTEGER

Input/Output

On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this argument you should refer to Section 3.4 in How to Use the NAG Library and its Documentation for details.

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this argument, the recommended value is 0. When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.

On exit: IFAIL = 0 unless the routine detects an error or a warning has been flagged (see Section 6).

6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

```
IFAIL = 1
```

On entry, $M = \langle value \rangle$.

Constraint: $M = \langle value \rangle$, the value of M on initialization (see C09ABF).

On entry, $N = \langle value \rangle$.

Constraint: $N = \langle value \rangle$, the value of N on initialization (see C09ABF).

IFAIL = 2

On entry, LDA = $\langle value \rangle$ and M = $\langle value \rangle$.

Constraint: LDA > M.

IFAIL = 3

On entry, LDCA = $\langle value \rangle$.

Constraint: LDCA $\geq \langle value \rangle$, the number of wavelet coefficients in the first dimension.

On entry, LDCD = $\langle value \rangle$.

Constraint: LDCD $\geq \langle value \rangle$, the number of wavelet coefficients in the first dimension.

On entry, LDCH = $\langle value \rangle$.

Constraint: LDCH $\geq \langle value \rangle$, the number of wavelet coefficients in the first dimension.

On entry, LDCV = $\langle value \rangle$.

Constraint: LDCV $\geq \langle value \rangle$, the number of wavelet coefficients in the first dimension.

IFAIL = 6

Either the initialization routine has not been called first or ICOMM has been corrupted.

Either the initialization routine was called with WTRANS = 'M' or ICOMM has been corrupted.

IFAIL = -99

An unexpected error has been triggered by this routine. Please contact NAG.

See Section 3.9 in How to Use the NAG Library and its Documentation for further information.

Mark 26 C09EAF.3

C09EAF NAG Library Manual

```
IFAIL = -399
```

Your licence key may have expired or may not have been installed correctly.

See Section 3.8 in How to Use the NAG Library and its Documentation for further information.

```
IFAIL = -999
```

Dynamic memory allocation failed.

See Section 3.7 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

The accuracy of the wavelet transform depends only on the floating-point operations used in the convolution and downsampling and should thus be close to *machine precision*.

8 Parallelism and Performance

C09EAF is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this routine. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

None.

10 Example

This example computes the two-dimensional discrete wavelet decomposition for a 6×6 input matrix using the Daubechies wavelet, WAVNAM = 'DB4', with half point symmetric end extension.

10.1 Program Text

```
Program c09eafe
!
      CO9EAF Example Program Text
1
     Mark 26 Release. NAG Copyright 2016.
!
      .. Use Statements ..
     Use nag_library, Only: c09abf, c09eaf, c09ebf, nag_wp
!
      .. Implicit None Statement ..
     Implicit None
!
      .. Parameters ..
                                        :: nin = 5, nout = 6
      Integer, Parameter
!
      .. Local Scalars ..
      Integer
                                        :: i, ifail, lda, ldb, ldca, ldcd,
                                           ldch, ldcv, m, n, nf, nwcm, nwcn,
                                           nwct, nwl
     Character (12)
                                        :: mode, wavnam, wtrans
      .. Local Arrays ..
!
     Real (Kind=nag_wp), Allocatable :: a(:,:), b(:,:), ca(:,:), cd(:,:),
                                           ch(:,:), cv(:,:)
     Integer
                                        :: icomm(180)
!
      .. Executable Statements ..
     Write (nout,*) 'CO9EAF Example Program Results'
!
     Skip heading in data file
     Read (nin,*)
!
     Read problem parameters.
     Read (nin,*) m, n
     Read (nin,*) wavnam, mode
```

C09EAF.4 Mark 26

```
Write (nout, 99999) wavnam, mode
      lda = m
      ldb = m
     Allocate (a(lda,n),b(ldb,n))
     Read data array
1
     Do i = 1, m
       Read (nin,*) a(i,1:n)
     End Do
     Write (nout, 99998) 'Input Data
                                                         Α'
      Do i = 1, m
       Write (nout,99997) a(i,1:n)
     End Do
     Query wavelet filter dimensions
     wtrans = 'Single Level'
!
     ifail: behaviour on error exit
     =0 for hard exit, =1 for quiet-soft, =-1 for noisy-soft
!
      ifail = 0
     Call c09abf(wavnam,wtrans,mode,m,n,nwl,nf,nwct,nwcn,icomm,ifail)
     nwcm = nwct/(4*nwcn)
     Allocate (ca(nwcm,nwcn),cd(nwcm,nwcn),cv(nwcm,nwcn),ch(nwcm,nwcn))
      ldca = nwcm
      ldch = nwcm
      ldcv = nwcm
      ldcd = nwcm
     ifail = 0
     Call c09eaf(m,n,a,lda,ca,ldca,ch,ldch,cv,ldcv,cd,ldcd,icomm,ifail)
     Write (nout, 99998) 'Approximation coefficients
     Do i = 1, nwcm
       Write (nout, 99997) ca(i, 1:nwcn)
     End Do
     Write (nout,99998) 'Diagonal coefficients
                                                        CD′
     Do i = 1, nwcm
       Write (nout, 99997) cd(i, 1:nwcn)
     End Do
                                                        CH '
     Write (nout, 99998) 'Horizontal coefficients
      Do i = 1, nwcm
       Write (nout, 99997) ch(i,1:nwcn)
     End Do
     Write (nout,99998) 'Vertical coefficients
                                                        CV′
     Do i = 1, nwcm
       Write (nout, 99997) cv(i, 1:nwcn)
     End Do
      ifail = 0
     Call c09ebf(m,n,ca,ldca,ch,ldch,cv,ldcv,cd,ldcd,b,ldb,icomm,ifail)
     Write (nout, 99998) 'Reconstruction
                                                         В'
     Do i = 1, m
       Write (nout,99997) b(i,1:n)
     End Do
99999 Format (/,1X,'DWT ::',/,1X,'
                                          Wavelet: ',A,/,1X,
' End mode: ',A)
99998 Format (/,1X,A,':')
99997 Format (1X,8(F8.4,1X),:)
   End Program cO9eafe
```

Mark 26 C09EAF.5

C09EAF NAG Library Manual

10.2 Program Data

```
CO9EAF Example Program Data
                               : m,n
 DB4 Half : wavnam, mode

      8.0000
      7.0000
      3.0000

      4.0000
      6.0000
      1.0000

      8.0000
      1.0000
      4.0000

      9.0000
      3.0000
      8.0000

                                               3.0000
                                                               1.0000
                                                                                 1.0000
                               1.0000 5.0000
4.0000 9.0000
8.0000 2.0000
                                                                  2.0000
                                                                                 9.0000
                                                                  3.0000
                                                                                 7.0000
                                                                 4.0000
                                                                                 3.0000
   1.0000
                3.0000
                                7.0000 1.0000
                                                                  5.0000
                                                                                 2.0000
                  3.0000 7.0000 7.0000
                                                                  6.0000
   4.0000
                                                                                 1.0000
```

10.3 Program Results

```
CO9EAF Example Program Results
```

DWT ::

Wavelet : DB4
End mode: Half

Eı	nd mode: H	alf			
Input Dat 8.0000 4.0000 8.0000 9.0000 1.0000 4.0000	7.0000 6.0000 1.0000 3.0000 3.0000 3.0000	3.0000 1.0000 4.0000 8.0000 7.0000 7.0000	A: 3.0000 5.0000 9.0000 2.0000 1.0000 7.0000	1.0000 2.0000 3.0000 4.0000 5.0000	1.0000 9.0000 7.0000 3.0000 2.0000 1.0000
Approxima 6.3591 11.5754 2.0630 10.2143 6.3353 11.7141	ation coef 10.3477 6.3762 8.4499 6.2445 8.7805 11.1018	ficients 8.0995 12.1704 15.4726 13.8571 10.2727 5.2923	CA: 10.3210 7.4521 12.1764 8.1060 10.0472 8.1272	8.7587 8.6977 3.8920 7.7701 6.8614 14.5540	3.5783 14.8535 2.7112 13.2127 7.5814 2.5729
Diagonal 0.4777 1.0689 -0.9555 0.2899 0.4944 -1.3753	coefficie 1.0230 1.5671 -1.9276 0.4453 1.4145 -2.5224	nts -0.3147 -2.1422 0.9195 -0.5695 0.3488 1.7581	CD: 0.0625 0.5565 -0.2228 0.1541 -0.1187 -0.4316	0.0831 1.7593 -0.5125 0.4749 -0.6212 -1.1835	-1.3316 -2.8097 2.6989 -0.7946 -1.5177 3.7547
Horizonta 0.4100 2.3496 -1.2690 0.6317 -0.2343 -1.8880	al coeffic -0.1827 -0.9422 0.0152 -0.0969 0.3923 0.8142	ients 1.5354 2.3780 -6.9338 2.3300 5.5457 -4.8552	CH: 0.0784 -1.0540 -1.7435 0.4637 2.1818 0.0736	0.8101 2.7743 -1.6917 0.6365 0.2103 -2.7395	-1.3594 -2.2648 1.2388 -0.1162 -0.8573 3.3590
Vertical 1.5365 0.6779 -1.1065 -0.1359 1.4244 1.0288	coefficie 5.9678 -0.0294 -2.8791 -2.6633 5.2140 2.2521	nts 3.4309 -5.3274 0.1535 -5.8549 1.6410 0.0574	CV: -1.0585 1.6483 0.0982 1.8440 -0.4669 -0.1359	-5.0275 4.8689 0.8417 6.2403 -3.2369 -0.5170	-4.8492 -1.8383 2.8923 0.5697 -4.5757 -2.6854
Reconstru 8.0000 4.0000 8.0000 9.0000 1.0000 4.0000	7.0000 6.0000 1.0000 3.0000 3.0000 3.0000	3.0000 1.0000 4.0000 8.0000 7.0000	B: 3.0000 5.0000 9.0000 2.0000 1.0000 7.0000	1.0000 2.0000 3.0000 4.0000 5.0000	1.0000 9.0000 7.0000 3.0000 2.0000

C09EAF.6 (last) Mark 26