

NAG Library Routine Document

F06HQF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

1 Purpose

F06HQF generates a sequence of complex plane rotations.

2 Specification

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SUBROUTINE F06HQF (PIVOT, DIRECT, N, ALPHA, X, INCX, C, S)
INTEGER                N, INCX
REAL (KIND=nag_wp)    C(N)
COMPLEX (KIND=nag_wp) ALPHA, X(*), S(N)
CHARACTER(1)          PIVOT, DIRECT
```

3 Description

F06HQF generates the parameters of a complex unitary matrix P , of order $n + 1$, chosen so as to set to zero the elements of a supplied n -element complex vector x .

If PIVOT = 'F' and DIRECT = 'F', or if PIVOT = 'V' and DIRECT = 'B',

$$P \begin{pmatrix} \alpha \\ x \end{pmatrix} = \begin{pmatrix} \beta \\ 0 \end{pmatrix};$$

If PIVOT = 'F' and DIRECT = 'B', or if PIVOT = 'V' and DIRECT = 'F',

$$P \begin{pmatrix} x \\ \alpha \end{pmatrix} = \begin{pmatrix} 0 \\ \beta \end{pmatrix}.$$

Here α and β are complex scalars.

P is represented as a sequence of n plane rotations P_k , as specified by PIVOT and DIRECT; P_k is chosen to annihilate x_k , and its 2 by 2 plane rotation part has the form

$$\begin{pmatrix} c_k & \bar{s}_k \\ -s_k & c_k \end{pmatrix},$$

with c_k real. The tangent of the rotation, t_k , is overwritten on x_k .

4 References

None.

5 Arguments

1: PIVOT – CHARACTER(1) *Input*

On entry: specifies the plane rotated by P_k .

PIVOT = 'V' (variable pivot)

P_k rotates the $(k, k + 1)$ plane.

PIVOT = 'F' (fixed pivot)

P_k rotates the $(1, k + 1)$ plane if DIRECT = 'F', or the $(k, n + 1)$ plane if DIRECT = 'B'.

Constraint: PIVOT = 'V' or 'F'.

- 2: DIRECT – CHARACTER(1) *Input*
On entry: specifies the sequence direction.
 DIRECT = 'F' (forward sequence)

$$P = P_n \cdots P_2 P_1.$$
 DIRECT = 'B' (backward sequence)

$$P = P_1 P_2 \cdots P_n.$$
Constraint: DIRECT = 'F' or 'B'.
- 3: N – INTEGER *Input*
On entry: n , the number of elements in x .
- 4: ALPHA – COMPLEX (KIND=nag_wp) *Input/Output*
On entry: the scalar α .
On exit: the scalar β .
- 5: X(*) – COMPLEX (KIND=nag_wp) array *Input/Output*
Note: the dimension of the array X must be at least $\max(1, 1 + (N - 1) \times \text{INCX})$.
On entry: the n -element vector x . x_i must be stored in $X(1 + (i - 1) \times \text{INCX})$, for $i = 1, 2, \dots, N$.
 Intermediate elements of X are not referenced.
On exit: the referenced elements are overwritten by details of the plane rotations.
- 6: INCX – INTEGER *Input*
On entry: the increment in the subscripts of X between successive elements of x .
Constraint: $\text{INCX} > 0$.
- 7: C(N) – REAL (KIND=nag_wp) array *Output*
On exit: the values c_k , the cosines of the rotations.
- 8: S(N) – COMPLEX (KIND=nag_wp) array *Output*
On exit: the values s_k , the sines of the rotations.

6 Error Indicators and Warnings

None.

7 Accuracy

Not applicable.

8 Parallelism and Performance

F06HQF is not threaded in any implementation.

9 Further Comments

None.

10 Example

None.
