

NAG Library Function Document

nag_regsn_mult_linear_upd_model (g02ddc)

1 Purpose

nag_regsn_mult_linear_upd_model (g02ddc) calculates the regression arguments for a general linear regression model. It is intended to be called after nag_regsn_mult_linear_addrem_obs (g02dcc), nag_regsn_mult_linear_add_var (g02dec) or nag_regsn_mult_linear_delete_var (g02dfc).

2 Specification

```
#include <nag.h>
#include <nagg02.h>

void nag_regsn_mult_linear_upd_model (Integer n, Integer ip,
    const double q[], Integer tdq, double *rss, double *df, double b[],
    double se[], double cov[], Nag_Boolean *svd, Integer *rank, double p[],
    double tol, NagError *fail)
```

3 Description

A general linear regression model fitted by nag_regsn_mult_linear (g02dac) may be adjusted by adding or deleting an observation using nag_regsn_mult_linear_addrem_obs (g02dcc), adding a new independent variable using nag_regsn_mult_linear_add_var (g02dec) or deleting an existing independent variable using nag_regsn_mult_linear_delete_var (g02dfc). These functions compute the vector c and the upper triangular matrix R . nag_regsn_mult_linear_upd_model (g02ddc) takes these basic results and computes the regression coefficients, $\hat{\beta}$, their standard errors and their variance-covariance matrix.

If R is of full rank, then $\hat{\beta}$ is the solution to:

$$R\hat{\beta} = c_1,$$

where c_1 is the first p elements of c .

If R is not of full rank a solution is obtained by means of a singular value decomposition (SVD) of R ,

$$R = Q_* \begin{pmatrix} D & 0 \\ 0 & 0 \end{pmatrix} P^T$$

where D is a k by k diagonal matrix with nonzero diagonal elements, k being the rank of R , and Q_* and P are p by p orthogonal matrices. This gives the solution

$$\hat{\beta} = P_1 D^{-1} Q_*^T c_1$$

P_1 being the first k columns of P , i.e., $P = (P_1 P_0)$ and Q_*^T being the first k columns of Q_* .

Details of the SVD, are made available, in the form of the matrix P^* :

$$P^* = \begin{pmatrix} D^{-1} P_1^T \\ P_0^T \end{pmatrix}$$

This will be only one of the possible solutions. Other estimates may be obtained by applying constraints to the arguments. These solutions can be obtained by calling nag_regsn_mult_linear_tran_model (g02dkc) after calling nag_regsn_mult_linear_upd_model (g02ddc). Only certain linear combinations of the arguments will have unique estimates, these are known as estimable functions. These can be estimated using nag_regsn_mult_linear_est_func (g02dnc).

The residual sum of squares required to calculate the standard errors and the variance-covariance matrix can either be input or can be calculated if additional information on c for the whole sample is provided.

4 References

Golub G H and Van Loan C F (1996) *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

Hammarling S (1985) The singular value decomposition in multivariate statistics *SIGNUM Newsl.* **20(3)** 2–25

Searle S R (1971) *Linear Models* Wiley

5 Arguments

- 1: **n** – Integer *Input*
On entry: number of observations.
Constraint: $n \geq 1$.

- 2: **ip** – Integer *Input*
On entry: the number of terms in the regression model, p .
Constraint: $ip \geq 1$.

- 3: **q[n × tdq]** – const double *Input*
Note: the (i, j) th element of the matrix Q is stored in $q[(i - 1) \times tdq + j - 1]$.
On entry: **q** must be the array **q** as output by nag_regsn_mult_linear_addrem_obs (g02dcc), nag_regsn_mult_linear_add_var (g02dec) or nag_regsn_mult_linear_delete_var (g02dfc). If on entry $rss \leq 0.0$ then all **n** elements of c are needed. This is provided by functions nag_regsn_mult_linear_add_var (g02dec) or nag_regsn_mult_linear_delete_var (g02dfc).

- 4: **tdq** – Integer *Input*
On entry: the stride separating matrix column elements in the array **q**.
Constraint: $tdq \geq ip + 1$.

- 5: **rss** – double * *Input/Output*
On entry: either the residual sum of squares or a value less than or equal to 0.0 to indicate that the residual sum of squares is to be calculated by the function.
On exit: if $rss \leq 0.0$ on entry, then on exit **rss** will contain the residual sum of squares as calculated by nag_regsn_mult_linear_upd_model (g02ddc).
 If **rss** was positive on entry, then it will be unchanged.

- 6: **df** – double * *Output*
On exit: the degrees of freedom associated with the residual sum of squares.

- 7: **b[ip]** – double *Output*
On exit: the estimates of the p arguments, $\hat{\beta}$.

- 8: **se[ip]** – double *Output*
On exit: the standard errors of the p arguments given in **b**.

- 9: **cov[ip × (ip + 1)/2]** – double *Output*
On exit: the upper triangular part of the variance-covariance matrix of the p parameter estimates given in **b**. They are stored packed by column, i.e., the covariance between the parameter estimate

given in $\mathbf{b}[i]$ and the parameter estimate given in $\mathbf{b}[j]$, $j \geq i$, is stored in $\mathbf{cov}[j(j+1)/2 + i]$, for $i = 0, 1, \dots, \mathbf{ip} - 1$ and $j = i, \dots, \mathbf{ip} - 1$.

10: **svd** – Nag_Boolean * *Output*

On exit: if a singular value decomposition has been performed, then **svd** = Nag_TRUE, otherwise **svd** = Nag_FALSE.

11: **rank** – Integer * *Output*

On exit: the rank of the independent variables.

If **svd** = Nag_FALSE, **rank** = **ip**.

If **svd** = Nag_TRUE, **rank** is an estimate of the rank of the independent variables.

rank is calculated as the number of singular values greater than $\mathbf{tol} \times$ (largest singular value). It is possible for the singular value decomposition to be carried out but **rank** to be returned as **ip**.

12: **p**[$\mathbf{ip} \times \mathbf{ip} + 2 \times \mathbf{ip}$] – double *Output*

On exit: **p** contains details of the singular value decomposition if used.

If **svd** = Nag_FALSE, **p** is not referenced.

If **svd** = Nag_TRUE, the first **ip** elements of **p** will not be referenced, the next **ip** values contain the singular values. The following $\mathbf{ip} \times \mathbf{ip}$ values contain the matrix P^* stored by rows.

13: **tol** – double *Input*

On entry: the value of **tol** is used to decide if the independent variables are of full rank and, if not, what is the rank of the independent variables. The smaller the value of **tol** the stricter the criterion for selecting the singular value decomposition. If **tol** = 0.0, then the singular value decomposition will never be used, this may cause run time errors or inaccuracies if the independent variables are not of full rank.

Suggested value: **tol** = 0.000001.

Constraint: **tol** \geq 0.0.

14: **fail** – NagError * *Input/Output*

The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE_2_INT_ARG_LT

On entry, **n** = $\langle value \rangle$ while **ip** = $\langle value \rangle$. These arguments must satisfy **n** \geq **ip**.

On entry, **tdq** = $\langle value \rangle$ while **ip** + 1 = $\langle value \rangle$. These arguments must satisfy **tdq** \geq **ip** + 1.

NE_ALLOC_FAIL

Dynamic memory allocation failed.

NE_DOF_LE_ZERO

The degrees of freedom for error are less than or equal to 0. In this case the estimates, $\hat{\beta}$, are returned but not the standard errors or covariances.

NE_INT_ARG_LT

On entry, **ip** = $\langle value \rangle$.

Constraint: **ip** \geq 1.

On entry, $n = \langle value \rangle$.
 Constraint: $n \geq 1$.

NE_REAL_ARG_LT

On entry, **tol** must not be less than 0.0: **tol** = $\langle value \rangle$.

NE_SVD_NOT_CONV

The singular value decomposition has failed to converge. This is an unlikely error exit.

7 Accuracy

The accuracy of the results will depend on the accuracy of the input R matrix, which may lose accuracy if a large number of observations or variables have been dropped.

8 Parallelism and Performance

Not applicable.

9 Further Comments

None.

10 Example

A dataset consisting of 12 observations and four independent variables is input and a regression model fitted by calls to `nag_regsn_mult_linear_add_var` (g02dec). The arguments are then calculated by `nag_regsn_mult_linear_upd_model` (g02ddc) and the results printed.

10.1 Program Text

```
/* nag_regsn_mult_linear_upd_model (g02ddc) Example Program.
 *
 * Copyright 2014 Numerical Algorithms Group.
 *
 * Mark 2, 1991.
 * Mark 8 revised, 2004.
 */

#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagg02.h>

#define X(I, J) x[(I) *tdx + J]
#define Q(I, J) q[(I) *tdq + J]
int main(void)
{
  Integer      exit_status = 0, i, ip, ipmax, j, m, n, rank, tdq, tdx;
  double       *b = 0, *cov = 0, df, *p = 0, *q = 0, rss, *se = 0, tol, *wt = 0;
  double       *wtptr, *x = 0, *xe = 0;
  char         nag_enum_arg[40];
  Nag_Boolean  svd, weight;
  NagError     fail;

  INIT_FAIL(fail);

  printf(
    "nag_regsn_mult_linear_upd_model (g02ddc) Example Program Results\n");
  /* Skip heading in data file */
#ifdef _WIN32
  scanf_s("%*[\n]");
#else

```

```

    scanf("%*[\n]");
#endif
#ifdef _WIN32
    scanf_s("%"NAG_IFMT" %"NAG_IFMT" %39s", &n, &m, nag_enum_arg, _countof(nag_en-
um_arg));
#else
    scanf("%"NAG_IFMT" %"NAG_IFMT" %39s", &n, &m, nag_enum_arg);
#endif
/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
weight = (Nag_Boolean) nag_enum_name_to_value(nag_enum_arg);
ipmax = 4;
if (n >= 1 && m >= 1)
{
    if (!(b = NAG_ALLOC(ipmax, double)) ||
        !(cov = NAG_ALLOC(ipmax*(ipmax+1)/2, double)) ||
        !(p = NAG_ALLOC(ipmax*(ipmax+2), double)) ||
        !(wt = NAG_ALLOC(n, double)) ||
        !(x = NAG_ALLOC(n*m, double)) ||
        !(xe = NAG_ALLOC(n, double)) ||
        !(se = NAG_ALLOC(ipmax, double)) ||
        !(q = NAG_ALLOC(n*(ipmax+1), double)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    tdx = m;
    tdq = ipmax+1;
}
else
{
    printf("Invalid n or m.\n");
    exit_status = 1;
    return exit_status;
}
if (weight)
    wtptr = wt;
else
    wtptr = (double *) 0;

if (wtptr)
{
    for (i = 0; i < n; i++)
    {
        for (j = 0; j < m; j++)
#ifdef _WIN32
            scanf_s("%lf", &X(i, j));
#else
            scanf("%lf", &X(i, j));
#endif
#ifdef _WIN32
            scanf_s("%lf%lf", &Q(i, 0), &wt[i]);
#else
            scanf("%lf%lf", &Q(i, 0), &wt[i]);
#endif
    }
}
else
{
    for (i = 0; i < n; i++)
    {
        for (j = 0; j < m; j++)
#ifdef _WIN32
            scanf_s("%lf", &X(i, j));
#else
            scanf("%lf", &X(i, j));
#endif
#ifdef _WIN32
            scanf_s("%lf", &Q(i, 0));

```

```

#else
    scanf("%lf", &Q(i, 0));
#endif
    }
}
/* Set tolerance */
tol = 0.000001e0;
ip = 0;
for (j = 0; j < m; ++j)
{
    /*
     *          Fit model using g02dec
     */
    for (i = 0; i < n; i++)
        xe[i] = X(i, j);
    /* nag_regsn_mult_linear_add_var (g02dec).
     * Add a new independent variable to a general linear
     * regression model
     */
    nag_regsn_mult_linear_add_var(n, ip, q, tdq, p, wtptr, xe, &rss, tol,
                                  &fail);

    if (fail.code == NE_NOERROR)
        ip += 1;
    else if (fail.code == NE_NVAR_NOT_IND)
        printf(" * New variable not added * \n");
    else
    {
        printf(
            "Error from nag_regsn_mult_linear_add_var (g02dec).\n%s\n",
            fail.message);
        exit_status = 1;
        goto END;
    }
}
}
rss = 0.0;
/* nag_regsn_mult_linear_upd_model (g02ddc).
 * Estimates of regression parameters from an updated model
 */
nag_regsn_mult_linear_upd_model(n, ip, q, tdq, &rss, &df, b, se, cov, &svd,
                                &rank, p, tol, &fail);

if (fail.code != NE_NOERROR)
{
    printf(
        "Error from nag_regsn_mult_linear_upd_model (g02ddc).\n%s\n",
        fail.message);
    exit_status = 1;
    goto END;
}

printf("\n");
if (svd)
    printf("Model not of full rank\n\n");
printf("Residual sum of squares = %13.4e\n", rss);
printf("Degrees of freedom = %3.1f\n\n", df);
printf("Variable      Parameter estimate      Standard error\n\n");
for (j = 0; j < ip; j++)
    printf("%6"NAG_IFMT"%20.4e%20.4e\n", j+1, b[j], se[j]);
printf("\n");

END:
NAG_FREE(b);
NAG_FREE(cov);
NAG_FREE(p);
NAG_FREE(wt);
NAG_FREE(x);
NAG_FREE(xe);

```

```

NAG_FREE(se);
NAG_FREE(q);

return exit_status;
}

```

10.2 Program Data

```

nag_regsn_mult_linear_upd_model (g02ddc) Example Program Data
12 4 Nag_FALSE
1.0 0.0 0.0 0.0 33.63
0.0 0.0 0.0 1.0 39.62
0.0 1.0 0.0 0.0 38.18
0.0 0.0 1.0 0.0 41.46
0.0 0.0 0.0 1.0 38.02
0.0 1.0 0.0 0.0 35.83
0.0 0.0 0.0 1.0 35.99
1.0 0.0 0.0 0.0 36.58
0.0 0.0 1.0 0.0 42.92
1.0 0.0 0.0 0.0 37.80
0.0 0.0 1.0 0.0 40.43
0.0 1.0 0.0 0.0 37.89

```

10.3 Program Results

```

nag_regsn_mult_linear_upd_model (g02ddc) Example Program Results

```

```

Residual sum of squares = 2.2227e+01
Degrees of freedom = 8.0

```

Variable	Parameter estimate	Standard error
1	3.6003e+01	9.6235e-01
2	3.7300e+01	9.6235e-01
3	4.1603e+01	9.6235e-01
4	3.7877e+01	9.6235e-01
