

# NAG Library Function Document

## nag\_dtbsv (f16pkc)

### 1 Purpose

nag\_dtbsv (f16pkc) solves a system of equations given as a real triangular band matrix.

### 2 Specification

```
#include <nag.h>
#include <nagf16.h>

void nag_dtbsv (Nag_OrderType order, Nag_UploType uplo, Nag_TransType trans,
               Nag_DiagType diag, Integer n, Integer k, double alpha,
               const double ab[], Integer pdab, double x[], Integer incx,
               NagError *fail)
```

### 3 Description

nag\_dtbsv (f16pkc) performs one of the matrix-vector operations

$$x \leftarrow \alpha A^{-1}x \quad \text{or} \quad x \leftarrow \alpha A^{-T}x,$$

where  $A$  is an  $n$  by  $n$  real triangular band matrix with  $k$  subdiagonals or superdiagonals,  $x$  is an  $n$ -element real vector and  $\alpha$  is a real scalar.  $A^{-T}$  denotes  $(A^T)^{-1}$  or equivalently  $(A^{-1})^T$ .

No test for singularity or near-singularity of  $A$  is included in this function. Such tests must be performed before calling this function.

### 4 References

Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001) *Basic Linear Algebra Subprograms Technical (BLAST) Forum Standard* University of Tennessee, Knoxville, Tennessee <http://www.netlib.org/blas/blast-forum/blas-report.pdf>

### 5 Arguments

1: **order** – Nag\_OrderType *Input*

*On entry:* the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag\_RowMajor. See Section 3.2.1.3 in the Essential Introduction for a more detailed explanation of the use of this argument.

*Constraint:* **order** = Nag\_RowMajor or Nag\_ColMajor.

2: **uplo** – Nag\_UploType *Input*

*On entry:* specifies whether  $A$  is upper or lower triangular.

**uplo** = Nag\_Upper  
 $A$  is upper triangular.

**uplo** = Nag\_Lower  
 $A$  is lower triangular.

*Constraint:* **uplo** = Nag\_Upper or Nag\_Lower.

- 3: **trans** – Nag\_TransType Input  
*On entry:* specifies the operation to be performed.  
**trans** = Nag\_NoTrans  
 $x \leftarrow \alpha A^{-1}x.$   
**trans** = Nag\_Trans or Nag\_ConjTrans  
 $x \leftarrow \alpha A^{-T}x.$   
*Constraint:* **trans** = Nag\_NoTrans, Nag\_Trans or Nag\_ConjTrans.
- 4: **diag** – Nag\_DiagType Input  
*On entry:* specifies whether  $A$  has nonunit or unit diagonal elements.  
**diag** = Nag\_NonUnitDiag  
The diagonal elements are stored explicitly.  
**diag** = Nag\_UnitDiag  
The diagonal elements are assumed to be 1 and are not referenced.  
*Constraint:* **diag** = Nag\_NonUnitDiag or Nag\_UnitDiag.
- 5: **n** – Integer Input  
*On entry:*  $n$ , the order of the matrix  $A$ .  
*Constraint:*  $n \geq 0$ .
- 6: **k** – Integer Input  
*On entry:*  $k$ , the number of subdiagonals or superdiagonals of the matrix  $A$ .  
*Constraint:*  $k \geq 0$ .
- 7: **alpha** – double Input  
*On entry:* the scalar  $\alpha$ .
- 8: **ab**[*dim*] – const double Input  
**Note:** the dimension, *dim*, of the array **ab** must be at least  $\max(1, \mathbf{pdab} \times \mathbf{n})$ .  
*On entry:* the  $n$  by  $n$  triangular band matrix  $A$ .  
This is stored as a notional two-dimensional array with row elements or column elements stored contiguously. The storage of elements of  $A_{ij}$ , depends on the **order** and **uplo** arguments as follows:  
if **order** = Nag\_ColMajor and **uplo** = Nag\_Upper,  
 $A_{ij}$  is stored in **ab**[ $k + i - j + (j - 1) \times \mathbf{pdab}$ ], for  $j = 1, \dots, n$  and  
 $i = \max(1, j - k), \dots, j$ ;  
if **order** = Nag\_ColMajor and **uplo** = Nag\_Lower,  
 $A_{ij}$  is stored in **ab**[ $i - j + (j - 1) \times \mathbf{pdab}$ ], for  $j = 1, \dots, n$  and  
 $i = j, \dots, \min(n, j + k)$ ;  
if **order** = Nag\_RowMajor and **uplo** = Nag\_Upper,  
 $A_{ij}$  is stored in **ab**[ $j - i + (i - 1) \times \mathbf{pdab}$ ], for  $i = 1, \dots, n$  and  
 $j = i, \dots, \min(n, i + k)$ ;  
if **order** = Nag\_RowMajor and **uplo** = Nag\_Lower,  
 $A_{ij}$  is stored in **ab**[ $k + j - i + (i - 1) \times \mathbf{pdab}$ ], for  $i = 1, \dots, n$  and  
 $j = \max(1, i - k), \dots, i$ .  
If **diag** = Nag\_UnitDiag, the diagonal elements of AB are assumed to be 1, and are not referenced.

- 9: **pdab** – Integer *Input*  
*On entry:* the stride separating row or column elements (depending on the value of **order**) of the matrix  $A$  in the array **ab**.  
*Constraint:* **pdab**  $\geq$  **k** + 1.
- 10: **x**[*dim*] – double *Input/Output*  
**Note:** the dimension, *dim*, of the array **x** must be at least  $\max(1, 1 + (\mathbf{n} - 1)|\mathbf{incx}|)$ .  
*On entry:* the right-hand side vector  $b$ .  
*On exit:* the solution vector  $x$ .
- 11: **incx** – Integer *Input*  
*On entry:* the increment in the subscripts of **x** between successive elements of  $x$ .  
*Constraint:* **incx**  $\neq$  0.
- 12: **fail** – NagError \* *Input/Output*  
The NAG error argument (see Section 3.6 in the Essential Introduction).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Dynamic memory allocation failed.  
See Section 3.2.1.2 in the Essential Introduction for further information.

### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

### NE\_INT

On entry, **incx** =  $\langle value \rangle$ .  
Constraint: **incx**  $\neq$  0.

On entry, **k** =  $\langle value \rangle$ .  
Constraint: **k**  $\geq$  0.

On entry, **n** =  $\langle value \rangle$ .  
Constraint: **n**  $\geq$  0.

### NE\_INT\_2

On entry, **pdab** =  $\langle value \rangle$ , **k** =  $\langle value \rangle$ .  
Constraint: **pdab**  $\geq$  **k** + 1.

### NE\_INTERNAL\_ERROR

An unexpected error has been triggered by this function. Please contact NAG.  
See Section 3.6.6 in the Essential Introduction for further information.

### NE\_NO\_LICENCE

Your licence key may have expired or may not have been installed correctly.  
See Section 3.6.5 in the Essential Introduction for further information.

## 7 Accuracy

The BLAS standard requires accurate implementations which avoid unnecessary over/underflow (see Section 2.7 of Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001)).

## 8 Parallelism and Performance

Not applicable.

## 9 Further Comments

None.

## 10 Example

This example solves the real triangular band system of linear equations  $Ax = y$ , where  $A$  is the 4 by 4 triangular matrix given with one subdiagonal given by

$$A = \begin{pmatrix} -4.16 & & & \\ -2.25 & 4.78 & & \\ & 5.86 & 6.32 & \\ & & -4.82 & 0.16 \end{pmatrix}$$

and where

$$y = (-16.64, -13.78, 13.10, -14.14)^T.$$

$A$  is stored in array **ab** using banded storage format and  $y$  is stored in array **x**. nag\_dtbsv (f16pkc) returns the solution in **x**.

### 10.1 Program Text

```
/* nag_dtbsv (f16pkc) Example Program.
 *
 * Copyright 2014 Numerical Algorithms Group.
 *
 * Mark 8, 2005.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf16.h>

int main(void)
{
    /* Scalars */
    double      alpha;
    Integer      exit_status, i, incx, j, kd, n, pdab, xlen;

    /* Arrays */
    double      *ab = 0, *x = 0;
    char        nag_enum_arg[40];

    /* Nag Types */
    NagError     fail;
    Nag_OrderType order;
    Nag_TransType trans;
    Nag_UploType uplo;
    Nag_DiagType diag;

#ifdef NAG_COLUMN_MAJOR
#define AB_UPPER(I, J) ab[(J-1)*pdab + kd + I - J]
#define AB_LOWER(I, J) ab[(J-1)*pdab + I - J]
#endif
}
```

```

#define B(I, J)          b[(J-1)*pdb + I - 1]
    order = Nag_ColMajor;
#else
#define AB_UPPER(I, J)  ab[(I-1)*pdab + J - I]
#define AB_LOWER(I, J) ab[(I-1)*pdab + kd + J - I]
#define B(I, J)        b[(I-1)*pdb + J - 1]
    order = Nag_RowMajor;
#endif

    exit_status = 0;
    INIT_FAIL(fail);

    printf("nag_dtbsv (f16pkc) Example Program Results\n\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

    /* Read the problem dimensions */
#ifdef _WIN32
    scanf_s("%"NAG_IFMT%"NAG_IFMT"%*[\n] ", &n, &kd);
#else
    scanf("%"NAG_IFMT%"NAG_IFMT"%*[\n] ", &n, &kd);
#endif

    /* Read the uplo storage parameter */
#ifdef _WIN32
    scanf_s("%39s%*[\n] ", nag_enum_arg, _countof(nag_enum_arg));
#else
    scanf("%39s%*[\n] ", nag_enum_arg);
#endif
    /* nag_enum_name_to_value (x04nac).
     * Converts NAG enum member name to value
     */
    uplo = (Nag_UploType) nag_enum_name_to_value(nag_enum_arg);
    /* Read the transpose parameter */
#ifdef _WIN32
    scanf_s("%39s%*[\n] ", nag_enum_arg, _countof(nag_enum_arg));
#else
    scanf("%39s%*[\n] ", nag_enum_arg);
#endif
    /* nag_enum_name_to_value (x04nac), see above. */
    trans = (Nag_TransType) nag_enum_name_to_value(nag_enum_arg);
    /* Read the unit-diagonal parameter */
#ifdef _WIN32
    scanf_s("%39s%*[\n] ", nag_enum_arg, _countof(nag_enum_arg));
#else
    scanf("%39s%*[\n] ", nag_enum_arg);
#endif
    /* nag_enum_name_to_value (x04nac), see above. */
    diag = (Nag_DiagType) nag_enum_name_to_value(nag_enum_arg);

    /* Read scalar parameters */
#ifdef _WIN32
    scanf_s("%lf%*[\n] ", &alpha);
#else
    scanf("%lf%*[\n] ", &alpha);
#endif
    /* Read increment parameter */
#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%*[\n] ", &incx);
#else
    scanf("%"NAG_IFMT"%*[\n] ", &incx);
#endif

    pdab = kd + 1;
    xlen = MAX(1, 1 + (n - 1)*ABS(incx));

```

```

if (n > 0)
{
  /* Allocate memory */
  if (!(ab = NAG_ALLOC(pdab*n, double)) ||
      !(x = NAG_ALLOC(xlen, double)))
  {
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
  }
}
else
{
  printf("Invalid n\n");
  exit_status = 1;
  return exit_status;
}

/* Input matrix AB and vector x*/

if (uplo == Nag_Upper)
{
  for (i = 1; i <= n; ++i)
  {
    if (diag == Nag_NonUnitDiag)
#ifdef _WIN32
      scanf_s("%lf", &AB_UPPER(i, i));
#else
      scanf("%lf", &AB_UPPER(i, i));
#endif
    for (j = i+1; j <= MIN(i+kd, n); ++j)
#ifdef _WIN32
      scanf_s("%lf", &AB_UPPER(i, j));
#else
      scanf("%lf", &AB_UPPER(i, j));
#endif
  }
#ifdef _WIN32
  scanf_s("%*[\n] ");
#else
  scanf("%*[\n] ");
#endif
}
else
{
  for (i = 1; i <= n; ++i)
  {
    for (j = MAX(1, i-kd); j < i; ++j)
#ifdef _WIN32
      scanf_s("%lf", &AB_LOWER(i, j));
#else
      scanf("%lf", &AB_LOWER(i, j));
#endif
    if (diag == Nag_NonUnitDiag)
#ifdef _WIN32
      scanf_s("%lf", &AB_LOWER(i, i));
#else
      scanf("%lf", &AB_LOWER(i, i));
#endif
  }
#ifdef _WIN32
  scanf_s("%*[\n] ");
#else
  scanf("%*[\n] ");
#endif
}
  for (i = 0; i < xlen; ++i)
#ifdef _WIN32
  scanf_s("%lf%*[\n] ", &x[i]);
#else
  scanf("%lf%*[\n] ", &x[i]);

```

```

#endif

/* nag_dtbsv (f16pkc).
 * Solution of real triangular band system of linear equations.
 *
 */
nag_dtbsv(order, uplo, trans, diag, n, kd, alpha, ab, pdab, x, incx,
          &fail);
if (fail.code != NE_NOERROR)
{
    printf("Error from nag_dtbsv (f16pkc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Print output vector x */
printf("%s\n", " Solution x:");
for (i = 0; i < xlen; ++i)
{
    printf("%11f\n", x[i]);
}

END:
NAG_FREE(ab);
NAG_FREE(x);

return exit_status;
}

```

## 10.2 Program Data

```

nag_dtbsv (f16pkc) Example Program Data
4 1 :Values of n and kd
Nag_Lower :Storage of A
Nag_NoTrans :Transpose A?
Nag_NonUnitDiag :Unit diagonal elements?
1.0 :Value of alpha
1 :Value of incx
-4.16
-2.25 4.78
5.86 6.32
-4.82 0.16 :End of matrix A
-16.64
-13.78
13.10
-14.14 :End of vector x

```

## 10.3 Program Results

```

nag_dtbsv (f16pkc) Example Program Results

Solution x:
4.000000
-1.000000
3.000000
2.000000

```

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