

NAG Library Function Document

nag_ztgsna (f08yyc)

1 Purpose

nag_ztgsna (f08yyc) estimates condition numbers for specified eigenvalues and/or eigenvectors of a complex matrix pair in generalized Schur form.

2 Specification

```
#include <nag.h>
#include <nagf08.h>

void nag_ztgsna (Nag_OrderType order, Nag_JobType job,
  Nag_HowManyType how_many, const Nag_Boolean select[], Integer n,
  const Complex a[], Integer pda, const Complex b[], Integer pdb,
  const Complex vl[], Integer pdvl, const Complex vr[], Integer pdvr,
  double s[], double dif[], Integer mm, Integer *m, NagError *fail)
```

3 Description

nag_ztgsna (f08yyc) estimates condition numbers for specified eigenvalues and/or right eigenvectors of an n by n matrix pair (S, T) in generalized Schur form. The function actually returns estimates of the reciprocals of the condition numbers in order to avoid possible overflow.

The pair (S, T) are in generalized Schur form if S and T are upper triangular as returned, for example, by nag_zgges (f08xnc) or nag_zggesx (f08xpc), or nag_zhgeqz (f08xsc) with **job** = Nag_Schur. The diagonal elements define the generalized eigenvalues (α_i, β_i) , for $i = 1, 2, \dots, n$, of the pair (S, T) and the eigenvalues are given by

$$\lambda_i = \alpha_i / \beta_i,$$

so that

$$\beta_i S x_i = \alpha_i T x_i \quad \text{or} \quad S x_i = \lambda_i T x_i,$$

where x_i is the corresponding (right) eigenvector.

If S and T are the result of a generalized Schur factorization of a matrix pair (A, B)

$$A = Q S Z^H, \quad B = Q T Z^H$$

then the eigenvalues and condition numbers of the pair (S, T) are the same as those of the pair (A, B) .

Let $(\alpha, \beta) \neq (0, 0)$ be a simple generalized eigenvalue of (A, B) . Then the reciprocal of the condition number of the eigenvalue $\lambda = \alpha / \beta$ is defined as

$$s(\lambda) = \frac{\left(|y^H A x|^2 + |y^H B x|^2 \right)^{1/2}}{(\|x\|_2 \|y\|_2)},$$

where x and y are the right and left eigenvectors of (A, B) corresponding to λ . If both α and β are zero, then (A, B) is singular and $s(\lambda) = -1$ is returned.

If U and V are unitary transformations such that

$$U^H(A, B)V = (S, T) = \begin{pmatrix} \alpha & * \\ 0 & S_{22} \end{pmatrix} \begin{pmatrix} \beta & * \\ 0 & T_{22} \end{pmatrix},$$

where S_{22} and T_{22} are $(n - 1)$ by $(n - 1)$ matrices, then the reciprocal condition number is given by

$$\text{Dif}(x) \equiv \text{Dif}(y) = \text{Dif}((\alpha, \beta), (S_{22}, T_{22})) = \sigma_{\min}(Z),$$

where $\sigma_{\min}(Z)$ denotes the smallest singular value of the $2(n-1)$ by $2(n-1)$ matrix

$$Z = \begin{pmatrix} \alpha \otimes I & -1 \otimes S_{22} \\ \beta \otimes I & -1 \otimes T_{22} \end{pmatrix}$$

and \otimes is the Kronecker product.

See Sections 2.4.8 and 4.11 of Anderson *et al.* (1999) and Kågström and Poromaa (1996) for further details and information.

4 References

Anderson E, Bai Z, Bischof C, Blackford S, Demmel J, Dongarra J J, Du Croz J J, Greenbaum A, Hammarling S, McKenney A and Sorensen D (1999) *LAPACK Users' Guide* (3rd Edition) SIAM, Philadelphia <http://www.netlib.org/lapack/lug>

Kågström B and Poromaa P (1996) LAPACK-style algorithms and software for solving the generalized Sylvester equation and estimating the separation between regular matrix pairs *ACM Trans. Math. Software* **22** 78–103

5 Arguments

- 1: **order** – Nag_OrderType *Input*
On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 3.2.1.3 in the Essential Introduction for a more detailed explanation of the use of this argument.
Constraint: **order** = Nag_RowMajor or Nag_ColMajor.
- 2: **job** – Nag_JobType *Input*
On entry: indicates whether condition numbers are required for eigenvalues and/or eigenvectors.
job = Nag_EigVals
 Condition numbers for eigenvalues only are computed.
job = Nag_EigVecs
 Condition numbers for eigenvectors only are computed.
job = Nag_DoBoth
 Condition numbers for both eigenvalues and eigenvectors are computed.
Constraint: **job** = Nag_EigVals, Nag_EigVecs or Nag_DoBoth.
- 3: **how_many** – Nag_HowManyType *Input*
On entry: indicates how many condition numbers are to be computed.
how_many = Nag_ComputeAll
 Condition numbers for all eigenpairs are computed.
how_many = Nag_ComputeSelected
 Condition numbers for selected eigenpairs (as specified by **select**) are computed.
Constraint: **how_many** = Nag_ComputeAll or Nag_ComputeSelected.
- 4: **select**[*dim*] – const Nag_Boolean *Input*
Note: the dimension, *dim*, of the array **select** must be at least **n** when **how_many** = Nag_ComputeSelected; otherwise **select** may be **NULL**.

On entry: specifies the eigenpairs for which condition numbers are to be computed if **how_many** = Nag_ComputeSelected. To select condition numbers for the eigenpair corresponding to the eigenvalue λ_j , **select**[$j - 1$] must be set to Nag_TRUE.

If **how_many** = Nag_ComputeAll, **select** is not referenced and may be **NULL**.

5: **n** – Integer *Input*

On entry: n , the order of the matrix pair (S, T) .

Constraint: $n \geq 0$.

6: **a**[dim] – const Complex *Input*

Note: the dimension, dim , of the array **a** must be at least $pda \times n$.

The (i, j) th element of the matrix A is stored in

$$\begin{aligned} & \mathbf{a}[(j-1) \times \mathbf{pda} + i - 1] \text{ when } \mathbf{order} = \text{Nag_ColMajor}; \\ & \mathbf{a}[(i-1) \times \mathbf{pda} + j - 1] \text{ when } \mathbf{order} = \text{Nag_RowMajor}. \end{aligned}$$

On entry: the upper triangular matrix S .

7: **pda** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **a**.

Constraint: $pda \geq n$.

8: **b**[dim] – const Complex *Input*

Note: the dimension, dim , of the array **b** must be at least $pdb \times n$.

The (i, j) th element of the matrix B is stored in

$$\begin{aligned} & \mathbf{b}[(j-1) \times \mathbf{pdb} + i - 1] \text{ when } \mathbf{order} = \text{Nag_ColMajor}; \\ & \mathbf{b}[(i-1) \times \mathbf{pdb} + j - 1] \text{ when } \mathbf{order} = \text{Nag_RowMajor}. \end{aligned}$$

On entry: the upper triangular matrix T .

9: **pdb** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **b**.

Constraint: $pdb \geq n$.

10: **vl**[dim] – const Complex *Input*

Note: the dimension, dim , of the array **vl** must be at least

$$\begin{aligned} & \mathbf{pdvl} \times \mathbf{mm} \text{ when } \mathbf{job} = \text{Nag_EigVals} \text{ or } \text{Nag_DoBoth} \text{ and } \mathbf{order} = \text{Nag_ColMajor}; \\ & \mathbf{n} \times \mathbf{pdvl} \text{ when } \mathbf{job} = \text{Nag_EigVals} \text{ or } \text{Nag_DoBoth} \text{ and } \mathbf{order} = \text{Nag_RowMajor}; \\ & \text{otherwise } \mathbf{vl} \text{ may be } \mathbf{NULL}. \end{aligned}$$

The i th element of the j th vector is stored in

$$\begin{aligned} & \mathbf{vl}[(j-1) \times \mathbf{pdvl} + i - 1] \text{ when } \mathbf{order} = \text{Nag_ColMajor}; \\ & \mathbf{vl}[(i-1) \times \mathbf{pdvl} + j - 1] \text{ when } \mathbf{order} = \text{Nag_RowMajor}. \end{aligned}$$

On entry: if **job** = Nag_EigVals or Nag_DoBoth, **vl** must contain left eigenvectors of (S, T) , corresponding to the eigenpairs specified by **how_many** and **select**. The eigenvectors must be stored in consecutive columns of **vl**, as returned by nag_zggeev (f08wnc) or nag_ztgevc (f08yxc).

If **job** = Nag_EigVecs, **vl** is not referenced and may be **NULL**.

- 11: **pdvl** – Integer *Input*
On entry: the stride used in the array **vl**.
Constraints:
 if **order** = Nag_ColMajor,
 if **job** = Nag_EigVals or Nag_DoBoth, **pdvl** \geq **n**;
 otherwise **pdvl** \geq 1.;
 if **order** = Nag_RowMajor,
 if **job** = Nag_EigVals or Nag_DoBoth, **pdvl** \geq **mm**;
 otherwise **vl** may be **NULL**..
- 12: **vr**[*dim*] – const Complex *Input*
Note: the dimension, *dim*, of the array **vr** must be at least
pdvr \times **mm** when **job** = Nag_EigVals or Nag_DoBoth and **order** = Nag_ColMajor;
n \times **pdvr** when **job** = Nag_EigVals or Nag_DoBoth and **order** = Nag_RowMajor;
 otherwise **vr** may be **NULL**.
 The *i*th element of the *j*th vector is stored in
vr[(*j* – 1) \times **pdvr** + *i* – 1] when **order** = Nag_ColMajor;
vr[(*i* – 1) \times **pdvr** + *j* – 1] when **order** = Nag_RowMajor.
On entry: if **job** = Nag_EigVals or Nag_DoBoth, **vr** must contain right eigenvectors of (*S*, *T*), corresponding to the eigenpairs specified by **how_many** and **select**. The eigenvectors must be stored in consecutive columns of **vr**, as returned by nag_zggevc (f08wnc) or nag_ztgevc (f08yxc).
 If **job** = Nag_EigVecs, **vr** is not referenced and may be **NULL**.
- 13: **pdvr** – Integer *Input*
On entry: the stride used in the array **vr**.
Constraints:
 if **order** = Nag_ColMajor,
 if **job** = Nag_EigVals or Nag_DoBoth, **pdvr** \geq **n**;
 otherwise **pdvr** \geq 1.;
 if **order** = Nag_RowMajor,
 if **job** = Nag_EigVals or Nag_DoBoth, **pdvr** \geq **mm**;
 otherwise **vr** may be **NULL**..
- 14: **s**[*dim*] – double *Output*
Note: the dimension, *dim*, of the array **s** must be at least
mm when **job** = Nag_EigVals or Nag_DoBoth;
 otherwise **s** may be **NULL**.
On exit: if **job** = Nag_EigVals or Nag_DoBoth, the reciprocal condition numbers of the selected eigenvalues, stored in consecutive elements of the array.
 If **job** = Nag_EigVecs, **s** is not referenced and may be **NULL**.
- 15: **dif**[*dim*] – double *Output*
Note: the dimension, *dim*, of the array **dif** must be at least
mm when **job** = Nag_EigVecs or Nag_DoBoth;
 otherwise **dif** may be **NULL**.
On exit: if **job** = Nag_EigVecs or Nag_DoBoth, the estimated reciprocal condition numbers of the selected eigenvectors, stored in consecutive elements of the array. If the eigenvalues cannot be

reordered to compute $\mathbf{dif}[j-1]$, $\mathbf{dif}[j-1]$ is set to 0; this can only occur when the true value would be very small anyway.

If $\mathbf{job} = \text{Nag_EigVals}$, \mathbf{dif} is not referenced and may be **NULL**.

16: **mm** – Integer

Input

On entry: the number of elements in the arrays **s** and **dif**.

Constraints:

if **how_many** = Nag_ComputeAll, $\mathbf{mm} \geq \mathbf{n}$;
otherwise $\mathbf{mm} \geq$ the number of selected eigenvalues.

17: **m** – Integer *

Output

On exit: the number of elements of the arrays **s** and **dif** used to store the specified condition numbers; for each selected eigenvalue one element is used.

If **how_many** = Nag_ComputeAll, **m** is set to **n**.

18: **fail** – NagError *

Input/Output

The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in the Essential Introduction for further information.

NE_BAD_PARAM

On entry, argument $\langle \text{value} \rangle$ had an illegal value.

NE_ENUM_INT_2

On entry, **how_many** = $\langle \text{value} \rangle$, **n** = $\langle \text{value} \rangle$ and **mm** = $\langle \text{value} \rangle$.

Constraint: if **how_many** = Nag_ComputeAll, $\mathbf{mm} \geq \mathbf{n}$;
otherwise $\mathbf{mm} \geq$ the number of selected eigenvalues.

On entry, **job** = $\langle \text{value} \rangle$, **pdvl** = $\langle \text{value} \rangle$, **mm** = $\langle \text{value} \rangle$.

Constraint: if **job** = Nag_EigVals or Nag_DoBoth, $\mathbf{pdvl} \geq \mathbf{mm}$.

On entry, **job** = $\langle \text{value} \rangle$, **pdvl** = $\langle \text{value} \rangle$ and **n** = $\langle \text{value} \rangle$.

Constraint: if **job** = Nag_EigVals or Nag_DoBoth, $\mathbf{pdvl} \geq \mathbf{n}$.

On entry, **job** = $\langle \text{value} \rangle$, **pdvr** = $\langle \text{value} \rangle$, **mm** = $\langle \text{value} \rangle$.

Constraint: if **job** = Nag_EigVals or Nag_DoBoth, $\mathbf{pdvr} \geq \mathbf{mm}$.

On entry, **job** = $\langle \text{value} \rangle$, **pdvr** = $\langle \text{value} \rangle$ and **n** = $\langle \text{value} \rangle$.

Constraint: if **job** = Nag_EigVals or Nag_DoBoth, $\mathbf{pdvr} \geq \mathbf{n}$.

NE_INT

On entry, **n** = $\langle \text{value} \rangle$.

Constraint: $\mathbf{n} > 0$.

On entry, **n** = $\langle \text{value} \rangle$.

Constraint: $\mathbf{n} \geq 0$.

On entry, **pda** = $\langle \text{value} \rangle$.

Constraint: $\mathbf{pda} > 0$.

On entry, **pdb** = $\langle \text{value} \rangle$.

Constraint: $\mathbf{pdb} > 0$.

On entry, **pdvl** = $\langle value \rangle$.

Constraint: **pdvl** > 0.

On entry, **pdvr** = $\langle value \rangle$.

Constraint: **pdvr** > 0.

NE_INT_2

On entry, **pda** = $\langle value \rangle$ and **n** = $\langle value \rangle$.

Constraint: **pda** ≥ **n**.

On entry, **pdb** = $\langle value \rangle$ and **n** = $\langle value \rangle$.

Constraint: **pdb** ≥ **n**.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.
See Section 3.6.6 in the Essential Introduction for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.
See Section 3.6.5 in the Essential Introduction for further information.

7 Accuracy

None.

8 Parallelism and Performance

nag_ztgsna (f08yyc) is not threaded by NAG in any implementation.

nag_ztgsna (f08yyc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

An approximate asymptotic error bound on the chordal distance between the computed eigenvalue $\tilde{\lambda}$ and the corresponding exact eigenvalue λ is

$$\chi(\tilde{\lambda}, \lambda) \leq \epsilon \|(A, B)\|_F / S(\lambda)$$

where ϵ is the *machine precision*.

An approximate asymptotic error bound for the right or left computed eigenvectors \tilde{x} or \tilde{y} corresponding to the right and left eigenvectors x and y is given by

$$\theta(\tilde{z}, z) \leq \epsilon \|(A, B)\|_F / \text{Dif}.$$

The real analogue of this function is nag_dtgsna (f08ylc).

10 Example

This example estimates condition numbers and approximate error estimates for all the eigenvalues and right eigenvectors of the pair (S, T) given by

$$S = \begin{pmatrix} 4.0 + 4.0i & 1.0 + 1.0i & 1.0 + 1.0i & 2.0 - 1.0i \\ 0 & 2.0 + 1.0i & 1.0 + 1.0i & 1.0 + 1.0i \\ 0 & 0 & 2.0 - 1.0i & 1.0 + 1.0i \\ 0 & 0 & 0 & 6.0 - 2.0i \end{pmatrix}$$

and

$$T = \begin{pmatrix} 2.0 & 1.0 + 1.0i & 1.0 + 1.0i & 3.0 - 1.0i \\ 0 & 1.0 & 2.0 + 1.0i & 1.0 + 1.0i \\ 0 & 0 & 1.0 & 1.0 + 1.0i \\ 0 & 0 & 0 & 2.0 \end{pmatrix}.$$

The eigenvalues and eigenvectors are computed by calling `nag_ztgevc` (f08yxc).

10.1 Program Text

```

/* nag_ztgsna (f08yyc) Example Program.
 *
 * Copyright 2014 Numerical Algorithms Group.
 *
 * Mark 23, 2011.
 */

#include <stdio.h>
#include <math.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagx02.h>
#include <nagf08.h>
#include <nagf16.h>

int main(void)
{
    /* Scalars */
    double      eps, snorm, stnrm, tnorm, tol;
    Integer     i, j, m, n, pds, pdt, pdvl, pdvr;
    Integer     exit_status = 0;

    /* Arrays */
    Complex     *s = 0, *t = 0, *vl = 0, *vr = 0;
    double     *dif = 0, *scon = 0;

    /* Nag Types */
    NagError    fail;
    Nag_OrderType order;

#ifdef NAG_COLUMN_MAJOR
#define S(I, J) s[(J-1)*pds + I - 1]
#define T(I, J) t[(J-1)*pdt + I - 1]
    order = Nag_ColMajor;
#else
#define S(I, J) s[(I-1)*pds + J - 1]
#define T(I, J) t[(I-1)*pdt + J - 1]
    order = Nag_RowMajor;
#endif

    INIT_FAIL(fail);

    printf("nag_ztgsna (f08yyc) Example Program Results\n\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n]");
#else

```

```

    scanf("%*[\n]");
#endif
#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%*[\n]", &n);
#else
    scanf("%"NAG_IFMT"%*[\n]", &n);
#endif
    if (n < 0)
    {
        printf("Invalid n\n");
        exit_status = 1;
        goto END;
    }
    m = n;
    pds = n;
    pdt = n;
    pdvl = n;
    pdvr = n;

    /* Allocate memory */
    if (!(dif = NAG_ALLOC(n, double)) ||
        !(scon = NAG_ALLOC(n, double)) ||
        !(s = NAG_ALLOC(n*n, Complex)) ||
        !(t = NAG_ALLOC(n*n, Complex)) ||
        !(vl = NAG_ALLOC(n*m, Complex)) ||
        !(vr = NAG_ALLOC(n*m, Complex)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    /* Read S and T from data file */
    for (i = 1; i <= n; ++i)
        for (j = 1; j <= n; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &S(i, j).re, &S(i, j).im);
#else
            scanf(" ( %lf , %lf )", &S(i, j).re, &S(i, j).im);
#endif
#ifdef _WIN32
            scanf_s("%*[\n]");
#else
            scanf("%*[\n]");
#endif
        for (i = 1; i <= n; ++i)
            for (j = 1; j <= n; ++j)
#ifdef _WIN32
                scanf_s(" ( %lf , %lf )", &T(i, j).re, &T(i, j).im);
#else
                scanf(" ( %lf , %lf )", &T(i, j).re, &T(i, j).im);
#endif
#ifdef _WIN32
            scanf_s("%*[\n]");
#else
            scanf("%*[\n]");
#endif

    /* Calculate the left and right generalized eigenvectors of the
     * matrix pair (S,T) using nag_ztgevc (f08yyc).
     * NULL may be passed here in place of the select array since all
     * eigenvectors are requested.
     */
    nag_ztgevc(order, Nag_BothSides, Nag_ComputeAll, NULL, n, s, pds, t, pdt,
              vl, pdvl, vr, pdvr, n, &m, &fail);
    if (fail.code != NE_NOERROR)
    {
        printf("Error from nag_ztgevc (f08yyc).\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }
}

```



```

/* Estimate condition numbers for all the generalized eigenvalues and right
 * eigenvectors of the pair (S,T) using nag_ztgsna (f08yyc).
 * NULL may be passed here in place of the select array since all
 * eigenvectors are requested.
 */
nag_ztgsna(order, Nag_DoBoth, Nag_ComputeAll, NULL, n, s, pds, t, pdt,
          vl, pdvl, vr, pdvr, scon, dif, n, &m, &fail);
if (fail.code != NE_NOERROR)
{
    printf("Error from nag_ztgsna (f08yyc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Print condition numbers of eigenvalues and right eigenvectors */
printf("Condition numbers of eigenvalues (scon) and right eigenvectors "
      "(dif),\n");
printf("scon:  ");
for (i = 0; i < m; ++i)
    printf(" %10.1e%s", scon[i], i%7 == 6?"\n      ":"");
printf("\ndif:  ");
for (i = 0; i < m; ++i)
    printf(" %10.1e%s", dif[i], i%7 == 6?"\n      ":"");

/* Compute the norm of (S,T) using nag_zge_norm (f16uac). */
eps = nag_machine_precision;
nag_zge_norm(order, Nag_OneNorm, n, n, s, pds, &snorm, &fail);
nag_zge_norm(order, Nag_OneNorm, n, n, t, pdt, &tnorm, &fail);
if (fail.code != NE_NOERROR)
{
    printf("Error from nag_zge_norm (f16uac).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

if (snorm == 0.0)
    stnorm = ABS(tnorm);
else if (tnorm == 0.0)
    stnorm = ABS(snorm);
else if (ABS(snorm) >= ABS(tnorm))
    stnorm = ABS(snorm)*sqrt(1.0+(tnorm/snorm)*(tnorm/snorm));
else
    stnorm = ABS(tnorm)*sqrt(1.0+(snorm/tnorm)*(snorm/tnorm));

printf("\nApproximate error estimates for eigenvalues of (S,T)\n");

/* Calculate approximate error estimates */
tol = eps*stnorm;

printf("\n\nError estimates for eigenvalues (errval) and right eigenvectors"
      " (errvec),\n");
printf("errval: ");
for (i = 0; i < m; ++i)
    printf(" %10.1e%s", tol/scon[i], i%7 == 6?"\n      ":"");
printf("\nerrvec: ");
for (i = 0; i < m; ++i)
    printf(" %10.1e%s", tol/dif[i], i%7 == 6?"\n      ":"");
printf("\n");

END:
NAG_FREE(dif);
NAG_FREE(scon);
NAG_FREE(s);
NAG_FREE(t);
NAG_FREE(vl);
NAG_FREE(vr);

return exit_status;
}

```

10.2 Program Data

nag_ztgsna (f08yyc) Example Program Data

```

4                                     : n
( 4.0, 4.0) ( 1.0, 1.0) ( 1.0, 1.0) ( 2.0,-1.0)
( 0.0, 0.0) ( 2.0, 1.0) ( 1.0, 1.0) ( 1.0, 1.0)
( 0.0, 0.0) ( 0.0, 0.0) ( 2.0,-1.0) ( 1.0, 1.0)
( 0.0, 0.0) ( 0.0, 0.0) ( 0.0, 0.0) ( 6.0,-2.0)   : matrix S

( 2.0, 0.0) ( 1.0, 1.0) ( 1.0, 1.0) ( 3.0,-1.0)
( 0.0, 0.0) ( 1.0, 0.0) ( 2.0, 1.0) ( 1.0, 1.0)
( 0.0, 0.0) ( 0.0, 0.0) ( 1.0, 0.0) ( 1.0, 1.0)
( 0.0, 0.0) ( 0.0, 0.0) ( 0.0, 0.0) ( 2.0, 0.0)   : matrix T

```

10.3 Program Results

nag_ztgsna (f08yyc) Example Program Results

Condition numbers of eigenvalues (scon) and right eigenvectors (diff),

scon:	1.0e+00	8.2e-01	7.2e-01	8.2e-01
dif:	3.2e-01	3.6e-01	5.5e-01	2.8e-01

Approximate error estimates for eigenvalues of (S,T)

Error estimates for eigenvalues (errval) and right eigenvectors (errvec),

errval:	1.5e-15	1.9e-15	2.1e-15	1.9e-15
errvec:	4.8e-15	4.3e-15	2.8e-15	5.5e-15
