NAG Library Function Document nag_imldwt_2d (c09edc)

1 Purpose

nag_imldwt_2d (c09edc) computes the inverse two-dimensional multi-level discrete wavelet transform (DWT). This function reconstructs data from (possibly filtered or otherwise manipulated) wavelet transform coefficients calculated by nag_mldwt_2d (c09ecc) from an original input matrix. The initialization function nag_wfilt_2d (c09abc) must be called first to set up the DWT options.

2 Specification

3 Description

nag_imldwt_2d (c09edc) performs the inverse operation of nag_mldwt_2d (c09ecc). That is, given a set of wavelet coefficients, computed up to level $n_{\rm fwd}$ by nag_mldwt_2d (c09ecc) using a DWT as set up by the initialization function nag_wfilt_2d (c09abc), on a real matrix, A, nag_imldwt_2d (c09edc) will reconstruct A. The reconstructed matrix is referred to as B in the following since it will not be identical to A when the DWT coefficients have been filtered or otherwise manipulated prior to reconstruction. If the original input matrix is level 0, then it is possible to terminate reconstruction at a higher level by specifying fewer than the number of levels used in the call to nag_mldwt_2d (c09ecc). This results in a partial reconstruction.

4 References

None.

5 Arguments

1: **nwlinv** – Integer

Inpu

On entry: the number of levels to be used in the inverse multi-level transform. The number of levels must be less than or equal to $n_{\rm fwd}$, which has the value of argument **nwl** as used in the computation of the wavelet coefficients using nag_mldwt_2d (c09ecc). The data will be reconstructed to level (**nwl** – **nwlinv**), where level 0 is the original input dataset provided to nag_mldwt_2d (c09ecc).

Constraint: $1 \le \text{nwlinv} \le \text{nwl}$, where nwl is the value used in a preceding call to nag_mldwt_2d (c09ecc).

2: **lenc** – Integer Input

On entry: the dimension of the array c.

Constraint: lenc $\geq n_{\rm ct}$, where $n_{\rm ct}$ is the total number of coefficients that correspond to a transform with **nwlinv** levels and is unchanged from the preceding call to nag mldwt 2d (c09ecc).

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3: **c**[lenc] – const double

Input

On entry: the coefficients of a multi-level wavelet transform of the original matrix, A, which may have been filtered or otherwise manipulated.

Let q(i) be the number of coefficients (of each type) at level i, for $i=n_{\text{fwd}}, n_{\text{fwd}}-1, \ldots, 1$. Then, setting $k_1=q(n_{\text{fwd}})$ and $k_{j+1}=k_j+q(n_{\text{fwd}}-\lceil j/3\rceil+1)$, for $j=1,2,\ldots,3n_{\text{fwd}}$, the coefficients are stored in ${\bf c}$ as follows:

$$\mathbf{c}[i-1], \text{ for } i = 1, 2, \dots, k_1$$

Contains the level n_{fwd} approximation coefficients, $a_{n_{\text{fwd}}}$.

$$\mathbf{c}[i-1], \text{ for } i = k_i + 1, \dots, k_{i+1}$$

Contains the level $n_{\text{fwd}} - \lceil j/3 \rceil + 1$ vertical, horizontal and diagonal coefficients. These are:

vertical coefficients if $j \mod 3 = 1$;

horizontal coefficients if $j \mod 3 = 2$;

diagonal coefficients if $j \mod 3 = 0$,

for
$$j = 1, ..., 3n_{\text{fwd}}$$
.

Note that the coefficients in **c** may be extracted according to level and type into two-dimensional arrays using nag wav 2d coeff ext (c09eyc), and inserted using nag wav 2d coeff ins (c09ezc).

4: **m** – Integer

Input

On entry: the number of elements, m, in the first dimension of the reconstructed matrix B. For a full reconstruction of **nwl** levels, where **nwl** is as supplied to nag_mldwt_2d (c09ecc), this must be the same as argument **m** used in the call to nag_mldwt_2d (c09ecc). For a partial reconstruction of **nwlinv** < **nwl** levels, this must be equal to **dwtlvm[nwlinv]**, as returned from nag_mldwt_2d (c09ecc).

5: \mathbf{n} – Integer

Input

On entry: the number of elements, n, in the second dimension of the reconstructed matrix B. For a full reconstruction of **nwl** levels, where **nwl** is as supplied to nag_mldwt_3d (c09fcc), this must be the same as argument **n** used in the call to nag_mldwt_2d (c09ecc). For a partial reconstruction of **nwlinv** < **nwl**, this must be equal to **dwtlvn**[**nwlinv**], as returned from nag_mldwt_2d (c09ecc).

6: $\mathbf{b}[\mathbf{ldb} \times \mathbf{n}] - \mathbf{double}$

Output

Note: the (i, j)th element of the matrix B is stored in $\mathbf{b}[(j-1) \times \mathbf{ldb} + i - 1]$.

On exit: the m by n reconstructed matrix, B, based on the input multi-level wavelet transform coefficients and the transform options supplied to the initialization function nag_wfilt_2d (c09abc).

7: **ldb** – Integer

Input

On entry: the stride separating matrix row elements in the array b.

Constraint: $ldb \ge m$.

8: **icomm**[180] – const Integer

Communication Array

On entry: contains details of the discrete wavelet transform and the problem dimension as setup in the call to the initialization function nag wfilt 2d (c09abc).

9: **fail** – NagError *

Input/Output

The NAG error argument (see Section 3.6 in the Essential Introduction).

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6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in the Essential Introduction for further information.

NE BAD PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE INITIALIZATION

Either the initialization function has not been called first or icomm has been corrupted.

Either the initialization function was called with **wtrans** = Nag_SingleLevel or **icomm** has been corrupted.

NE INT

```
On entry, lenc = \langle value \rangle.
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Constraint: **lenc** $\geq \langle value \rangle$, the total number of coefficients generated by the preceding call to nag mldwt 2d (c09ecc).

On entry, $\mathbf{m} = \langle value \rangle$.

Constraint: $\mathbf{m} \ge \langle value \rangle$, the number of coefficients in the first dimension at the required level of reconstruction.

On entry, $\mathbf{n} = \langle value \rangle$.

Constraint: $\mathbf{n} \ge \langle value \rangle$, the number of coefficients in the second dimension at the required level of reconstruction.

On entry, **nwlinv** = $\langle value \rangle$. Constraint: **nwlinv** > 1.

NE INT 2

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On entry, \mathbf{ldb} = \langle value \rangle and \mathbf{m} = \langle value \rangle.
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Constraint: $ldb \ge m$.

On entry, **nwlinv** = $\langle value \rangle$ and $n_{\text{fwd}} = \langle value \rangle$.

Constraint: **nwlinv** $\leq n_{\text{fwd}}$.

NE INTERNAL ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in the Essential Introduction for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly. See Section 3.6.5 in the Essential Introduction for further information.

7 Accuracy

The accuracy of the wavelet transform depends only on the floating-point operations used in the convolution and downsampling and should thus be close to *machine precision*.

8 Parallelism and Performance

Not applicable.

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9 Further Comments

None.

10 Example

See Section 10 in nag_mldwt_2d (c09ecc).

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