NAG Library Routine Document F07NWF (ZSYTRI)

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

F07NWF (ZSYTRI) computes the inverse of a complex symmetric matrix A, where A has been factorized by F07NRF (ZSYTRF).

2 Specification

```
SUBROUTINE F07NWF (UPLO, N, A, LDA, IPIV, WORK, INFO)

INTEGER

N, LDA, IPIV(*), INFO

COMPLEX (KIND=nag_wp) A(LDA,*), WORK(2*N)

CHARACTER(1)

UPLO
```

The routine may be called by its LAPACK name zsytri.

3 Description

F07NWF (ZSYTRI) is used to compute the inverse of a complex symmetric matrix A, the routine must be preceded by a call to F07NRF (ZSYTRF), which computes the Bunch–Kaufman factorization of A.

```
If UPLO = 'U', A = PUDU^TP^T and A^{-1} is computed by solving U^TP^TXPU = D^{-1} for X.
 If UPLO = 'L', A = PLDL^TP^T and A^{-1} is computed by solving L^TP^TXPL = D^{-1} for X.
```

4 References

Du Croz J J and Higham N J (1992) Stability of methods for matrix inversion *IMA J. Numer. Anal.* 12 1-19

5 Parameters

1: UPLO – CHARACTER(1)

Input

On entry: specifies how A has been factorized.

```
UPLO = 'U'
A = PUDU^{T}P^{T}, \text{ where } U \text{ is upper triangular.}
UPLO = 'L'
A = PLDL^{T}P^{T}, \text{ where } L \text{ is lower triangular.}
```

2: N – INTEGER Input

On entry: n, the order of the matrix A.

Constraint: UPLO = 'U' or 'L'.

Constraint: $N \geq 0$.

3: A(LDA,*) - COMPLEX (KIND=nag_wp) array Input/Output

Note: the second dimension of the array A must be at least max(1, N).

On entry: details of the factorization of A, as returned by F07NRF (ZSYTRF).

Mark 24 F07NWF.1

On exit: the factorization is overwritten by the n by n symmetric matrix A^{-1} .

If UPLO = 'U', the upper triangle of A^{-1} is stored in the upper triangular part of the array.

If UPLO = 'L', the lower triangle of A^{-1} is stored in the lower triangular part of the array.

4: LDA – INTEGER Input

On entry: the first dimension of the array A as declared in the (sub)program from which F07NWF (ZSYTRI) is called.

Constraint: LDA $\geq \max(1, N)$.

5: IPIV(∗) − INTEGER array

Input

Note: the dimension of the array IPIV must be at least max(1, N).

On entry: details of the interchanges and the block structure of D, as returned by F07NRF (ZSYTRF).

6: $WORK(2 \times N) - COMPLEX (KIND=nag_wp) array$

Workspace

7: INFO – INTEGER Output

On exit: INFO = 0 unless the routine detects an error (see Section 6).

6 Error Indicators and Warnings

Errors or warnings detected by the routine:

INFO < 0

If INFO = -i, the *i*th parameter had an illegal value. An explanatory message is output, and execution of the program is terminated.

INFO > 0

If INFO = i, d(i, i) is exactly zero; D is singular and the inverse of A cannot be computed.

7 Accuracy

The computed inverse X satisfies a bound of the form

if UPLO = 'U',
$$|DU^{T}P^{T}XPU - I| \le c(n)\epsilon(|D||U^{T}|P^{T}|X|P|U| + |D||D^{-1}|)$$
;
if UPLO = 'L', $|DL^{T}P^{T}XPL - I| \le c(n)\epsilon(|D||L^{T}|P^{T}|X|P|L| + |D||D^{-1}|)$,

c(n) is a modest linear function of n, and ϵ is the machine precision.

8 Further Comments

The total number of real floating point operations is approximately $\frac{8}{3}n^3$.

The real analogue of this routine is F07MJF (DSYTRI).

F07NWF.2 Mark 24

9 Example

This example computes the inverse of the matrix A, where

$$A = \begin{pmatrix} -0.39 - 0.71i & 5.14 - 0.64i & -7.86 - 2.96i & 3.80 + 0.92i \\ 5.14 - 0.64i & 8.86 + 1.81i & -3.52 + 0.58i & 5.32 - 1.59i \\ -7.86 - 2.96i & -3.52 + 0.58i & -2.83 - 0.03i & -1.54 - 2.86i \\ 3.80 + 0.92i & 5.32 - 1.59i & -1.54 - 2.86i & -0.56 + 0.12i \end{pmatrix}.$$

Here A is symmetric and must first be factorized by F07NRF (ZSYTRF).

9.1 Program Text

```
Program f07nwfe
     FO7NWF Example Program Text
!
     Mark 24 Release. NAG Copyright 2012.
      .. Use Statements ..
     Use nag_library, Only: nag_wp, x04dbf, zsytrf, zsytri
      .. Implicit None Statement ..
     Implicit None
      .. Parameters ..
                                        :: nin = 5, nout = 6
     Integer, Parameter
      .. Local Scalars ..
!
     Integer
                                        :: i, ifail, info, lda, lwork, n
     Character (1)
                                        :: uplo
     .. Local Arrays ..
     Complex (Kind=nag_wp), Allocatable :: a(:,:), work(:)
     Integer, Allocatable :: ipiv(:)
     Character (1)
                                        :: clabs(1), rlabs(1)
!
      .. Executable Statements ..
     Write (nout,*) 'F07NWF Example Program Results'
     Skip heading in data file
     Read (nin,*)
     Read (nin,*) n
      lda = n
     lwork = 64*n
     Allocate (a(lda,n),work(lwork),ipiv(n))
     Read A from data file
     Read (nin,*) uplo
      If (uplo=='U') Then
        Read (nin,*)(a(i,i:n),i=1,n)
     Else If (uplo=='L') Then
       Read (nin, *)(a(i, 1:i), i=1, n)
     End If
      Factorize A
     The NAG name equivalent of zsytrf is f07nrf
!
      Call zsytrf(uplo,n,a,lda,ipiv,work,lwork,info)
     Write (nout,*)
     Flush (nout)
     If (info==0) Then
!
        Compute inverse of A
        The NAG name equivalent of zsytri is f07nwf
!
        Call zsytri(uplo,n,a,lda,ipiv,work,info)
!
        Print inverse
1
        ifail: behaviour on error exit
               =0 for hard exit, =1 for quiet-soft, =-1 for noisy-soft
1
        ifail = 0
        Call x04dbf(uplo,'Nonunit',n,n,a,lda,'Bracketed','F7.4','Inverse', &
    'Integer',rlabs,'Integer',clabs,80,0,ifail)
```

Mark 24 F07NWF.3

F07NWF NAG Library Manual

```
Else
    Write (nout,*) 'The factor D is singular'
End If
End Program f07nwfe
```

9.2 Program Data

9.3 Program Results

FO7NWF Example Program Results

```
Inverse

1 2 3 4

1 (-0.1562,-0.1014)
2 (0.0400, 0.1527) (0.0946,-0.1475)
3 (0.0550, 0.0845) (-0.0326,-0.1370) (-0.1320,-0.0102)
4 (0.2162,-0.0742) (-0.0995,-0.0461) (-0.1793, 0.1183) (-0.2269, 0.2383)
```

F07NWF.4 (last)

Mark 24