

NAG Library Function Document

nag_tsa_diff (g13aac)

1 Purpose

nag_tsa_diff (g13aac) carries out non-seasonal and seasonal differencing on a time series. Information which allows the original series to be reconstituted from the differenced series is also produced. This information is required in time series forecasting.

2 Specification

```
#include <nag.h>
#include <naggl3.h>
void nag_tsa_diff (const double x[], Integer nx, Integer d, Integer ds,
                  Integer s, double xd[], Integer *nxd, NagError *fail)
```

3 Description

Let $\nabla^d \nabla_s^D x_i$ be the i th value of a time series x_i , for $i = 1, 2, \dots, n$ after non-seasonal differencing of order d and seasonal differencing of order D (with period or seasonality s). In general,

$$\begin{aligned} \nabla^d \nabla_s^D x_i &= \nabla^{d-1} \nabla_s^D x_{i+1} - \nabla^{d-1} \nabla_s^D x_i & d > 0 \\ \nabla^d \nabla_s^D x_i &= \nabla^d \nabla_s^{D-1} x_{i+s} - \nabla^d \nabla_s^{D-1} x_i & D > 0 \end{aligned}$$

Non-seasonal differencing up to the required order d is obtained using

$$\begin{aligned} \nabla^1 x_i &= x_{i+1} - x_i & \text{for } i = 1, 2, \dots, (n-1) \\ \nabla^2 x_i &= \nabla^1 x_{i+1} - \nabla^1 x_i & \text{for } i = 1, 2, \dots, (n-2) \\ &\vdots \\ \nabla^d x_i &= \nabla^{d-1} x_{i+1} - \nabla^{d-1} x_i & \text{for } i = 1, 2, \dots, (n-d) \end{aligned}$$

Seasonal differencing up to the required order D is then obtained using

$$\begin{aligned} \nabla^d \nabla_s^1 x_i &= \nabla^d x_{i+s} - \nabla^d x_i & \text{for } i = 1, 2, \dots, (n-d-s) \\ \nabla^d \nabla_s^2 x_i &= \nabla^d \nabla_s^1 x_{i+s} - \nabla^d \nabla_s^1 x_i & \text{for } i = 1, 2, \dots, (n-d-2s) \\ &\vdots \\ \nabla^d \nabla_s^D x_i &= \nabla^d \nabla_s^{D-1} x_{i+s} - \nabla^d \nabla_s^{D-1} x_i & \text{for } i = 1, 2, \dots, (n-d-D \times s) \end{aligned}$$

Mathematically, the sequence in which the differencing operations are performed does not affect the final resulting series of $m = n - d - D \times s$ values.

4 References

None.

5 Arguments

1: **x[nx]** – const double *Input*
On entry: the undifferenced time series, x_i , for $i = 1, 2, \dots, n$.

- 2: **nx** – Integer *Input*
On entry: n , the number of values in the undifferenced time series.
Constraint: $\mathbf{nx} > \mathbf{d} + (\mathbf{ds} \times \mathbf{s})$.
- 3: **d** – Integer *Input*
On entry: d , the order of non-seasonal differencing.
Constraint: $\mathbf{d} \geq 0$.
- 4: **ds** – Integer *Input*
On entry: D , the order of seasonal differencing.
Constraint: $\mathbf{ds} \geq 0$.
- 5: **s** – Integer *Input*
On entry: s , the seasonality.
Constraints:
 if $\mathbf{ds} > 0$, $\mathbf{s} > 0$;
 if $\mathbf{ds} = 0$, $\mathbf{s} \geq 0$.
- 6: **xd[nx]** – double *Output*
On exit: the differenced values in elements 0 to $\mathbf{nxd} - 1$, and reconstitution data in the remainder of the array.
- 7: **nxd** – Integer * *Output*
On exit: the number of differenced values in the array **xd**.
- 8: **fail** – NagError * *Input/Output*
 The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_INT

On entry, $\mathbf{d} = \langle value \rangle$.

Constraint: $\mathbf{d} \geq 0$.

On entry, $\mathbf{ds} = \langle value \rangle$.

Constraint: $\mathbf{ds} \geq 0$.

On entry, $\mathbf{s} = \langle value \rangle$.

Constraint: $\mathbf{s} \geq 0$.

NE_INT_2

On entry, $\mathbf{ds} = \langle value \rangle$.

Constraint: if $\mathbf{s} = 0$, $\mathbf{ds} \leq 0$.

NE_INT_4

On entry, $\mathbf{nx} = \langle value \rangle$, $\mathbf{d} = \langle value \rangle$, $\mathbf{ds} = \langle value \rangle$ and $\mathbf{s} = \langle value \rangle$.

Constraint: $\mathbf{nx} > \mathbf{d} + (\mathbf{ds} \times \mathbf{s})$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

7 Accuracy

The computations are believed to be stable.

8 Parallelism and Performance

Not applicable.

9 Further Comments

The time taken by `nag_tsa_diff` (g13aac) is approximately proportional to $(\mathbf{d} + \mathbf{ds}) \times \mathbf{nx}$.

10 Example

This example reads in a set of data consisting of 20 observations from a time series. Non-seasonal differencing of order 2 and seasonal differencing of order 1 (with seasonality of 4) are applied to the input data, giving an output array holding 14 differenced values and 6 values which can be used to reconstitute the output array.

10.1 Program Text

```

/* nag_tsa_diff (g13aac) Example Program.
 *
 * Copyright 2002 Numerical Algorithms Group.
 *
 * Mark 7, 2002.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagg13.h>

int main(void)
{
    /* Scalars */
    Integer  exit_status, i, d, ds, s, nx, nxd;
    NagError fail;

    /* Arrays */
    double   *x = 0, *xd = 0;

    INIT_FAIL(fail);

    exit_status = 0;
    printf("nag_tsa_diff (g13aac) Example Program Results\n");

    /* Skip heading in data file */
    scanf("%*[^\\n] ");
    scanf("%ld%ld%ld%ld%*[^\\n] ", &nx, &d,
        &ds, &s);

    if (nx > 0)
    {
        /* Allocate memory */
        if (!(x = NAG_ALLOC(nx, double)) ||
            !(xd = NAG_ALLOC(nx, double)))
        {
            printf("Allocation failure\n");
            exit_status = -1;
        }
    }
}

```

```

        goto END;
    }

    for (i = 1; i <= nx; ++i)
        scanf("%lf", &x[i-1]);
    scanf("%*[^\\n] ");

    printf("\\n");
    printf("Non-seasonal differencing of order %ld "
           "and seasonal differencing\\nof order %ld "
           "with seasonality %ld are applied\\n", d, ds, s);

    /* nag_tsa_diff (g13aac).
     * Univariate time series, seasonal and non-seasonal
     * differencing
     */
    nag_tsa_diff(x, nx, d, ds, s, xd, &nxd, &fail);
    if (fail.code != NE_NOERROR)
    {
        printf("Error from nag_tsa_diff (g13aac).\\n%s\\n",
              fail.message);
        exit_status = 1;
        goto END;
    }

    printf("\\n");
    printf("The output array holds %2ld values, of which the "
           "first %2ld are differenced values\\n\\n", nx, nxd);

    for (i = 1; i <= nx; ++i)
    {
        printf("%10.1f", xd[i-1]);
        if (i % 5 == 0 || i == nx)
            printf("\\n");
    }
}

END:
    NAG_FREE(x);
    NAG_FREE(xd);

    return exit_status;
}

```

10.2 Program Data

```

nag_tsa_diff (g13aac) Example Program Data
20 2 1 4
120.0 108.0 98.0 118.0 135.0
131.0 118.0 125.0 121.0 100.0
82.0 82.0 89.0 88.0 86.0
96.0 108.0 110.0 99.0 105.0

```

10.3 Program Results

```

nag_tsa_diff (g13aac) Example Program Results

```

Non-seasonal differencing of order 2 and seasonal differencing of order 1 with seasonality 4 are applied

The output array holds 20 values, of which the first 14 are differenced values

-11.0	-10.0	-8.0	4.0	12.0
-2.0	18.0	9.0	-4.0	-6.0
-5.0	-2.0	-12.0	5.0	2.0
-10.0	-13.0	17.0	6.0	105.0
