

## NAG Library Function Document

### nag\_summary\_stats\_onevar\_combine (g01auc)

#### 1 Purpose

nag\_summary\_stats\_onevar\_combine (g01auc) combines sets of summaries produced by nag\_summary\_stats\_onevar (g01atc).

#### 2 Specification

```
#include <nag.h>
#include <nagg01.h>

void nag_summary_stats_onevar_combine (Integer b, const double mrcomm[],
    Integer *pn, double *xmean, double *xsd, double *xskew, double *xkurt,
    double *xmin, double *xmax, double rcomm[], NagError *fail)
```

#### 3 Description

Assume a dataset containing  $n$  observations, denoted by  $x = \{x_i : i = 1, 2, \dots, n\}$  and a set of weights,  $w = \{w_i : i = 1, 2, \dots, n\}$ , has been split into  $b$  blocks, and each block summarised via a call to nag\_summary\_stats\_onevar (g01atc). Then nag\_summary\_stats\_onevar\_combine (g01auc) takes the  $b$  communication arrays returned by nag\_summary\_stats\_onevar (g01atc) and returns the mean ( $\bar{x}$ ), standard deviation ( $s_2$ ), coefficients of skewness ( $s_3$ ) and kurtosis ( $s_4$ ), and the maximum and minimum values for the whole dataset.

For a definition of  $\bar{x}$ ,  $s_2$ ,  $s_3$  and  $s_4$  see Section 3 in nag\_summary\_stats\_onevar (g01atc).

#### 4 References

West D H D (1979) Updating mean and variance estimates: An improved method *Comm. ACM* **22** 532–555

#### 5 Arguments

- 1: **b** – Integer *Input*  
*On entry:*  $b$ , the number of blocks the full dataset was split into.  
*Constraint:*  $b \geq 1$ .
- 2: **mrcomm**[ $20 \times b$ ] – const double *Communication Array*  
**Note:** where **MRCOMM**( $i, j$ ) appears in this document, it refers to the array element **mrcomm**[( $j - 1$ )  $\times$  20 +  $i - 1$ ].  
*On entry:* the  $j$ th column of **MRCOMM** must contain the information returned in **rcomm** from one of the runs of nag\_summary\_stats\_onevar (g01atc).
- 3: **pn** – Integer \* *Output*  
*On exit:* the number of valid observations, that is the number of observations with  $w_i > 0$ , for  $i = 1, 2, \dots, n$ .
- 4: **xmean** – double \* *Output*  
*On exit:*  $\bar{x}$ , the mean.

- 5: **xsd** – double \* *Output*  
*On exit:*  $s_2$ , the standard deviation.
- 6: **xskew** – double \* *Output*  
*On exit:*  $s_3$ , the coefficient of skewness.
- 7: **xkurt** – double \* *Output*  
*On exit:*  $s_4$ , the coefficient of kurtosis.
- 8: **xmin** – double \* *Output*  
*On exit:* the smallest value.
- 9: **xmax** – double \* *Output*  
*On exit:* the largest value.
- 10: **rcomm**[20] – double *Communication Array*  
*On exit:* an amalgamation of the information held in **mrcomm**. This is in the same format as **rcomm** from nag\_summary\_stats\_onevar (g01atc).  
 If **rcomm** is NULL, **rcomm** is not referenced.
- 11: **fail** – NagError \* *Input/Output*  
 The NAG error argument (see Section 3.6 in the Essential Introduction).

## 6 Error Indicators and Warnings

### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

### NE\_CASES\_ONE

On exit we were unable to calculate **xsd**, **xskew** or **xkurt**. A value of 0 has been returned.

### NE\_CASES\_ZERO

On entry, the number of valid observations is zero.

### NE\_ILLEGAL\_COMM

On entry, **mrcomm** is not in the expected format.

### NE\_INT

On entry, **b** =  $\langle value \rangle$ .  
 Constraint:  $b \geq 1$ .

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

### NE\_ZERO\_VARIANCE

On exit we were unable to calculate **xskew** or **xkurt**. A value of 0 has been returned.

## 7 Accuracy

Not applicable.

## 8 Parallelism and Performance

Not applicable.

## 9 Further Comments

The order that the  $b$  communication arrays are stored in **mrcomm** is arbitrary. Different orders can lead to slightly different results due to numerical accuracy of floating-point calculations.

Both `nag_summary_stats_onevar_combine` (g01auc) and `nag_summary_stats_onevar` (g01atc) consolidate results from multiple summaries. Whereas the former can only be used to combine summaries calculated sequentially, the latter combines summaries calculated in an arbitrary order allowing, for example, summaries calculated on different processing units to be combined.

## 10 Example

This example summarises some simulated data. The data is supplied in three blocks, the first consisting of 21 observations, the second 51 observations and the last 28 observations. Summaries are produced for each block of data separately and then an overall summary is produced.

### 10.1 Program Text

```

/* nag_summary_stats_onevar_combine (g01auc) Example Program.
 *
 * Copyright 2013 Numerical Algorithms Group.
 *
 * Mark 24, 2013.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagg01.h>

#define MRCOMM(I, J) mrcomm[(J)*20+(I)]

int main(void)
{
    /* Integer scalar and array declarations */
    Integer  b, i, iwt, j, nb, pn;
    Integer  exit_status = 0;

    /* NAG structures and types */
    NagError fail;

    /* Double scalar and array declarations */
    double   xkurt, xmax, xmean, xmin, xsd, xskew;
    double   rcomm[20];
    double   *mrcomm = 0, *wt = 0, *x = 0;

    /* Initialise the error structure */
    INIT_FAIL(fail);

    printf(
        "nag_summary_stats_onevar_combine (g01auc) Example Program Results\n\n");

    /* Skip heading in data file */
    scanf("%*[\n] ");

    /* Read in the number of block of data we have */
    scanf("%ld%*[\n] ", &b);

```

```

if (!(mrcomm = NAG_ALLOC(20*b, double)))
{
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
}

/* Loop over each block of data */
for (j = 0; j < b; j++)
{
    /* Read in the number of observations in this block and a flag indicating
       whether weights have been supplied (iwt = 1) or not (iwt = 0) */
    scanf("%ld%ld%*[\n] ", &nb, &iwt);

    /* Reallocate X to the required size */
    NAG_FREE(x);
    if (!(x = NAG_ALLOC(nb, double)))
    {
        printf("Allocation failure\n");
        exit_status = -2;
        goto END;
    }

    /* Read in the data for this block */
    if (iwt)
    {
        /* Weights supplied, so reallocate WT to the required size */
        NAG_FREE(wt);
        if (!(wt = NAG_ALLOC(nb, double)))
        {
            printf("Allocation failure\n");
            exit_status = -3;
            goto END;
        }
        for (i = 0; i < nb; i++)
            scanf("%lf%lf", &x[i], &wt[i]);
    }
    else
    {
        /* No weights */
        NAG_FREE(wt);
        wt = 0;

        for (i = 0; i < nb; i++)
            scanf("%lf", &x[i]);
    }
    scanf("%*[\n] ");

    /* Call nag_summary_stats_onevar (g01atc) to summarise
       this block of data */
    pn = 0;
    nag_summary_stats_onevar(nb, x, wt, &pn, &xmean, &xsd, &xskew, &xkurt,
                            &xmin, &xmax, rcomm, &fail);
    if (fail.code != NE_NOERROR && fail.code != NE_CASES_ONE &&
        fail.code != NE_ZERO_VARIANCE && fail.code != NE_CASES_ZERO)
    {
        printf("Error from nag_summary_stats_onevar (g01atc).\n%s\n",
              fail.message);
        exit_status = 1;
        goto END;
    }

    /* Save RCOMM for future reference */
    for (i = 0; i < 20; i++)
        MRCOMM(i,j) = rcomm[i];

    /* Display the results for this block */
    printf(" Summary for block %ld\n", j+1);
    if (fail.code == NE_CASES_ZERO)
        printf(" No valid observations supplied. All weights are zero.\n");
}

```

```

else
{
printf(" %ld valid observations\n", pn);
printf("   Mean           %13.2f\n", xmean);
if (fail.code == NE_CASES_ONE)
{
printf("   Unable to calculate the standard deviation,");
printf("skewness or kurtosis\n");
}
else
{
printf("   Std devn          %13.2f\n", xsd);
if (fail.code == NE_ZERO_VARIANCE)
printf("   Unable to calculate the skewness and kurtosis\n");
else
{
printf("   Skewness           %13.2f\n", xskew);
printf("   Kurtosis           %13.2f\n", xkurt);
}
}
printf("   Minimum           %13.2f\n", xmin);
printf("   Maximum           %13.2f\n", xmax);
}
}

/* Call nag_summary_stats_onevar_combine (g01auc) to combine the
summaries across all the blocks */
nag_summary_stats_onevar_combine(b, mrcomm, &pn, &xmean, &xsd, &xskew,
&xkurt, &xmin, &xmax, rcomm, &fail);
if (fail.code != NE_NOERROR)
{
printf("Error from nag_summary_stats_onevar_combine (g01auc).\n%s\n",
fail.message);
exit_status = 2;
goto END;
}

/* Display the combined results */
printf(" Summary for the combined data\n");
if (fail.code == NE_CASES_ZERO)
printf(" No valid observations supplied. All weights are zero.\n");
else
{
printf(" %ld valid observations\n", pn);
printf("   Mean           %13.2f\n", xmean);
if (fail.code == NE_CASES_ONE)
{
printf("   Unable to calculate the standard deviation,");
printf(" skewness or kurtosis\n");
}
else
{
printf("   Std devn          %13.2f\n", xsd);
if (fail.code == NE_ZERO_VARIANCE)
printf("   Unable to calculate the skewness and kurtosis\n");
else
{
printf("   Skewness           %13.2f\n", xskew);
printf("   Kurtosis           %13.2f\n", xkurt);
}
}
printf("   Minimum           %13.2f\n", xmin);
printf("   Maximum           %13.2f\n", xmax);
}
}

END:
NAG_FREE(x);
NAG_FREE(wt);
NAG_FREE(mrcomm);

return(exit_status);

```

}

## 10.2 Program Data

```
nag_summary_stats_onevar_combine (g01auc) Example Program Data
3                                     :: b
21 1                                 :: nb,iwt (1st block)
-0.62 4.91      -1.92 0.25
-1.72 3.90      -6.35 3.75
 2.00 1.17       7.65 3.19
 6.15 2.66       3.81 0.02
 4.87 3.59      -0.51 3.63
 6.88 4.83      -5.85 3.72
-0.72 1.72       0.66 0.78
 2.23 4.74      -1.61 1.72
-0.15 3.94      -1.15 1.33
-8.74 0.51      -3.94 2.40
 3.61 3.90                                     :: End of x,wt for 1st block
51 0                                     :: nb,iwt (2nd block)
-0.66 -2.39 -6.25  1.23  2.27 -2.27
10.12  8.29 -2.99  8.71 -0.74  0.02
 1.22  1.70  4.30  2.99 -0.83 -1.00
 6.57  2.32 -3.47 -1.41 -5.26  0.53
 1.80  4.79 -3.04  1.20 -3.21 -3.75
 0.86  1.27 -5.95 -5.27  1.63  3.59
-0.01 -1.38 -4.71 -4.82  3.55  0.46
 2.57  1.76 -4.05  1.23 -1.99  3.20
-0.65  8.42 -6.01                                     :: End of x for 2nd block
28 0                                     :: nb,iwt (3rd block)
 1.13 -8.86  5.92 -1.71 -3.99  6.57
-2.01 -2.29 -1.11  7.14  4.84 -4.44
-3.32 10.25 -2.11  8.02 -7.31  2.80
-1.20  1.01  1.37 -2.28  1.28 -3.95
 3.43 -0.61  4.85 -0.11                                     :: End of x for 3rd block
```

## 10.3 Program Results

nag\_summary\_stats\_onevar\_combine (g01auc) Example Program Results

```
Summary for block 1
21 valid observations
  Mean                0.73
  Std devn            4.40
  Skewness            -0.05
  Kurtosis            -1.00
  Minimum             -8.74
  Maximum              7.65
```

```
Summary for block 2
51 valid observations
  Mean                0.28
  Std devn            3.96
  Skewness            0.46
  Kurtosis            -0.16
  Minimum             -6.25
  Maximum             10.12
```

```
Summary for block 3
28 valid observations
  Mean                0.48
  Std devn            4.65
  Skewness            0.19
  Kurtosis            -0.58
  Minimum             -8.86
  Maximum             10.25
```

```
Summary for the combined data
100 valid observations
  Mean                0.51
  Std devn            4.24
```

Skewness	0.18
Kurtosis	-0.59
Minimum	-8.86
Maximum	10.25

---