

## NAG Toolbox

### nag\_rand\_dist\_beta (g05sb)

#### 1 Purpose

nag\_rand\_dist\_beta (g05sb) generates a vector of pseudorandom numbers taken from a beta distribution with parameters  $a$  and  $b$ .

#### 2 Syntax

```
[state, x, ifail] = nag_rand_dist_beta(n, a, b, state)
```

```
[state, x, ifail] = g05sb(n, a, b, state)
```

#### 3 Description

The beta distribution has PDF (probability density function)

$$f(x) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} x^{a-1} (1-x)^{b-1} \quad \text{if } 0 \leq x \leq 1; a, b > 0,$$

$$f(x) = 0 \quad \text{otherwise.}$$

One of four algorithms is used to generate the variates depending on the values of  $a$  and  $b$ . Let  $\alpha$  be the maximum and  $\beta$  be the minimum of  $a$  and  $b$ . Then the algorithms are as follows:

- (i) if  $\alpha < 0.5$ , Johnk's algorithm is used, see for example Dagpunar (1988). This generates the beta variate as  $u_1^{1/a} / (u_1^{1/a} + u_2^{1/b})$ , where  $u_1$  and  $u_2$  are uniformly distributed random variates;
- (ii) if  $\beta > 1$ , the algorithm BB given by Cheng (1978) is used. This involves the generation of an observation from a beta distribution of the second kind by the envelope rejection method using a log-logistic target distribution and then transforming it to a beta variate;
- (iii) if  $\alpha > 1$  and  $\beta < 1$ , the switching algorithm given by Atkinson (1979) is used. The two target distributions used are  $f_1(x) = \beta x^\beta$  and  $f_2(x) = \alpha(1-x)^{\beta-1}$ , along with the approximation to the switching argument of  $t = (1-\beta)/(\alpha+1-\beta)$ ;
- (iv) in all other cases, Cheng's BC algorithm (see Cheng (1978)) is used with modifications suggested by Dagpunar (1988). This algorithm is similar to BB, used when  $\beta > 1$ , but is tuned for small values of  $a$  and  $b$ .

One of the initialization functions nag\_rand\_init\_repeat (g05kf) (for a repeatable sequence if computed sequentially) or nag\_rand\_init\_nonrepeat (g05kg) (for a non-repeatable sequence) must be called prior to the first call to nag\_rand\_dist\_beta (g05sb).

#### 4 References

Atkinson A C (1979) A family of switching algorithms for the computer generation of beta random variates *Biometrika* **66** 141–5

Cheng R C H (1978) Generating beta variates with nonintegral shape parameters *Comm. ACM* **21** 317–322

Dagpunar J (1988) *Principles of Random Variate Generation* Oxford University Press

Hastings N A J and Peacock J B (1975) *Statistical Distributions* Butterworth

## 5 Parameters

### 5.1 Compulsory Input Parameters

1: **n** – INTEGER

$n$ , the number of pseudorandom numbers to be generated.

*Constraint:*  $n \geq 0$ .

2: **a** – REAL (KIND=nag\_wp)

$a$ , the parameter of the beta distribution.

*Constraint:*  $a > 0.0$ .

3: **b** – REAL (KIND=nag\_wp)

$b$ , the parameter of the beta distribution.

*Constraint:*  $b > 0.0$ .

4: **state(:)** – INTEGER array

**Note:** the actual argument supplied **must** be the array **state** supplied to the initialization routines nag\_rand\_init\_repeat (g05kf) or nag\_rand\_init\_nonrepeat (g05kg).

Contains information on the selected base generator and its current state.

### 5.2 Optional Input Parameters

None.

### 5.3 Output Parameters

1: **state(:)** – INTEGER array

Contains updated information on the state of the generator.

2: **x(n)** – REAL (KIND=nag\_wp) array

The  $n$  pseudorandom numbers from the specified beta distribution.

3: **ifail** – INTEGER

**ifail** = 0 unless the function detects an error (see Section 5).

## 6 Error Indicators and Warnings

Errors or warnings detected by the function:

**ifail** = 1

*Constraint:*  $n \geq 0$ .

**ifail** = 2

*Constraint:*  $a > 0.0$ .

**ifail** = 3

*Constraint:*  $b > 0.0$ .

**ifail** = 4

On entry, **state** vector has been corrupted or not initialized.

**ifail** = -99

An unexpected error has been triggered by this routine. Please contact NAG.

**ifail** = -399

Your licence key may have expired or may not have been installed correctly.

**ifail** = -999

Dynamic memory allocation failed.

## 7 Accuracy

Not applicable.

## 8 Further Comments

To generate an observation,  $y$ , from the beta distribution of the second kind from an observation,  $x$ , generated by `nag_rand_dist_beta` (g05sb) the transformation,  $y = x/(1 - x)$ , may be used.

## 9 Example

This example prints a set of five pseudorandom numbers from a beta distribution with parameters  $a = 2.0$  and  $b = 2.0$ , generated by a single call to `nag_rand_dist_beta` (g05sb), after initialization by `nag_rand_init_repeat` (g05kf).

### 9.1 Program Text

```
function g05sb_example

fprintf('g05sb example results\n\n');

% Initialize the base generator to a repeatable sequence
seed = [nag_int(1762543)];
genid = nag_int(1);
subid = nag_int(1);
[state, ifail] = g05kf( ...
                    genid, subid, seed);

% Number of variates
n = nag_int(5);

% Parameters
a = 2;
b = 2;

% Generate variates from beta distribution
[state, x, ifail] = g05sb( ...
                        n, a, b, state);

disp('Variates');
disp(x);
```

### 9.2 Program Results

```
g05sb example results

Variates
    0.5977
    0.6818
    0.1797
    0.4174
    0.4987
```