

## NAG Toolbox

### nag\_ode\_ivp\_stiff\_integ\_diag (d02ny)

#### 1 Purpose

nag\_ode\_ivp\_stiff\_integ\_diag (d02ny) is a diagnostic function which you may call either after any user-specified exit or after a mid-integration error exit from any of those integrators in Sub-chapter D02M–N that use methods set up by calls to nag\_ode\_ivp\_stiff\_dassl (d02mv), nag\_ode\_ivp\_stiff\_bdf (d02nv) or nag\_ode\_ivp\_stiff\_blend (d02nw).

#### 2 Syntax

```
[hu, h, tcur, tolsf, nst, nre, nje, nqu, nq, niter, imxer, algequ, ifail] =
nag_ode_ivp_stiff_integ_diag(neq, neqmax, rwork, inform)
```

```
[hu, h, tcur, tolsf, nst, nre, nje, nqu, nq, niter, imxer, algequ, ifail] =
d02ny(neq, neqmax, rwork, inform)
```

#### 3 Description

nag\_ode\_ivp\_stiff\_integ\_diag (d02ny) permits you to inspect statistics produced by any integrator in this sub-chapter that has been set up a call to one of nag\_ode\_ivp\_stiff\_dassl (d02mv), nag\_ode\_ivp\_stiff\_bdf (d02nv) or nag\_ode\_ivp\_stiff\_blend (d02nw). These statistics concern the integration only.

#### 4 References

See the D02M–N Sub-chapter Introduction.

#### 5 Parameters

##### 5.1 Compulsory Input Parameters

- 1: **neq** – INTEGER  
The value used for the argument **neq** when calling the integrator.  
*Constraint:*  $\text{neq} \geq 1$ .
- 2: **neqmax** – INTEGER  
The value used for the argument **neqmax** when calling the integrator.  
*Constraint:*  $\text{neqmax} \geq \text{neq}$ .
- 3: **rwork**( $50 + 4 \times \text{neq}$ ) – REAL (KIND=nag\_wp) array  
Contains information supplied by the integrator.
- 4: **inform**(23) – INTEGER array  
Contains information supplied by the integrator.

##### 5.2 Optional Input Parameters

None.

### 5.3 Output Parameters

- 1: **hu** – REAL (KIND=nag\_wp)  
The last successful step size.
- 2: **h** – REAL (KIND=nag\_wp)  
The proposed next step size for continuing the integration.
- 3: **tcur** – REAL (KIND=nag\_wp)  
 $t$ , the value of the independent variable which the integrator has actually reached. **tcur** will always be at least as far as the output value of the argument  $t$  in the direction of integration, but may be further (if overshooting and interpolation at **tout** was specified, e.g., see nag\_ode\_ivp\_stiff\_exp\_fulljac (d02nb)).
- 4: **tolsf** – REAL (KIND=nag\_wp)  
A tolerance scale factor, **tolsf**  $\geq$  1.0, which is computed when a request for too much accuracy is detected by the integrator (indicated by a return with **ifail** = 3 or 14). If **itol** is left unaltered but **rtol** and **atol** are uniformly scaled up by a factor of **tolsf** the next call to the integrator is deemed likely to succeed.
- 5: **nst** – INTEGER  
The number of steps taken in the integration so far.
- 6: **nre** – INTEGER  
The number of function or residual evaluations (**fcn** (e.g., see nag\_ode\_ivp\_stiff\_exp\_fulljac (d02nb)) or **resid** (e.g., see nag\_ode\_ivp\_stiff\_imp\_fulljac (d02ng)) calls) used in the integration so far.
- 7: **nje** – INTEGER  
The number of Jacobian evaluations used in the integration so far. This equals the number of matrix  $LU$  decompositions.
- 8: **nqu** – INTEGER  
The order of the method last used (successfully) in the integration.
- 9: **nq** – INTEGER  
The proposed order of the method for continuing the integration.
- 10: **niter** – INTEGER  
The number of iterations performed in the integration so far by the nonlinear equation solver.
- 11: **imxer** – INTEGER  
The index of the component of largest magnitude in the weighted local error vector  $(e_i/w_i)$ , for  $i = 1, 2, \dots, \mathbf{neq}$ .
- 12: **algequ(neq)** – LOGICAL array  
**algequ**( $i$ ) = *true* if the  $i$ th equation integrated was detected to be algebraic, otherwise **algequ**( $i$ ) = *false*. Note that when the integrators for explicit equations are being used, then **algequ**( $i$ ) = *false*, for  $i = 1, 2, \dots, \mathbf{neq}$ .

13: **ifail** – INTEGER

**ifail** = 0 unless the function detects an error (see Section 5).

## 6 Error Indicators and Warnings

Errors or warnings detected by the function:

**ifail** = 1

On entry, **neq** < 1,  
or **neqmax** < 1,  
or **neq** > **neqmax**.

**ifail** = -99

An unexpected error has been triggered by this routine. Please contact NAG.

**ifail** = -399

Your licence key may have expired or may not have been installed correctly.

**ifail** = -999

Dynamic memory allocation failed.

## 7 Accuracy

Not applicable.

## 8 Further Comments

Statistics for sparse matrix linear algebra calls (if appropriate) may be determined by a call to `nag_ode_ivp_stiff_sparjac_diag` (d02nx).

## 9 Example

See Section 10 in `nag_ode_ivp_stiff_exp_fulljac` (d02nb).

### 9.1 Program Text

```
function d02ny_example
fprintf('d02ny example results\n\n');

% Initialize integration method setup variables and arrays.
neq = nag_int(3);
neqmax = nag_int(neq);
nwkjac = nag_int(neqmax*(neqmax + 1));
maxord = nag_int(5);
sdysav = nag_int(maxord+1);
maxstp = nag_int(200);
mxhnil = nag_int(5);

h0 = 0;
hmax = 10;
hmin = 1.0e-10;
tcrit = 20;
petzld = false;

const = zeros(6, 1);
rwork = zeros(50+4*neqmax, 1);

[const, rwork, ifail] = d02nv(neqmax, sdysav, maxord, 'Newton', petzld, ...
```

```

const, tcrit, hmin, hmax, h0, maxstp, ...
mxhnil, 'Average-L2', rwork);

% Setup for numerical Jacobian using d02ns
nwkjac = nag_int(neq*(neq+1));
[rwork, ifail] = d02ns( ...
    neq, neq, 'Numerical', nwkjac, rwork);

% Initialize variables and arrays for integration
t      = 0;
tout   = 10;
y      = [1; 0; 0];
rtol   = [0.0001];
atol   = [1e-07];
itol   = nag_int(1);
inform = zeros(23, 1, nag_int_name);
ysave  = zeros(neq, sdysav);
wkjac  = zeros(nwkjac, 1);
itask  = nag_int(4);
itrace = nag_int(0);

% Integrate ODE from t=0 to t=tout, no monitoring, using d02nb
[t, y, ydot, rwork, inform, ysave, wkjac, ifail] = ...
    d02nb( ...
        t, tout, y, rwork, rtol, atol, itol, inform, @fcn, ysave, ...
        @jac, wkjac, 'd02nby', itask, itrace);

% Get diagnostics
[hu, h, tcur, tolsf, nst, nre, nje, nqu, nq, nit, imxer, algequ, ifail] = ...
    d02ny( ...
        neq, neqmax, rwork, inform);

% Get solution at tout
[y, ifail] = d02mz( ...
    tout, neq, neq, ysave, rwork);

% Print solution and diagnostics
fprintf(' At t = %8.3f, y(1:3) = %5.1f, %5.1f, %5.1f\n', t, y);
fprintf('\nDiagnostic information\n integration status:\n');
fprintf('   last and next step sizes = %8.5f, %8.5f\n', hu, h);
fprintf('   integration stopped at x = %8.5f\n', tcur);
fprintf('   algorithm statistics:\n');
fprintf('   number of time-steps and Newton iterations = %5d %5d\n', nst, nit);
fprintf('   number of residual and jacobian evaluations = %5d %5d\n', nre, nje);
fprintf('   order of method last used and next to use = %5d %5d\n', nqu, nq);
fprintf('   component with largest error = %5d\n', imxer);

function [f, ires] = fcn(neq, t, y, ires)
    % Evaluate derivative vector.
    f = zeros(3,1);
    f(1) = -0.04d0*y(1) + 1.0d4*y(2)*y(3);
    f(2) = 0.04d0*y(1) - 1.0d4*y(2)*y(3) - 3.0d7*y(2)*y(2);
    f(3) = 3.0d7*y(2)*y(2);

function p = jac(neq, t, y, h, d, p)
    % Evaluate the Jacobian.
    p = zeros(neq, neq);
    hxd = h*d;
    p(1,1) = 1.0d0 - hxd*(-0.04d0);
    p(1,2) = -hxd*(1.0d4*y(3));
    p(1,3) = -hxd*(1.0d4*y(2));
    p(2,1) = -hxd*(0.04d0);
    p(2,2) = 1.0d0 - hxd*(-1.0d4*y(3)-6.0d7*y(2));
    p(2,3) = -hxd*(-1.0d4*y(2));
    p(3,2) = -hxd*(6.0d7*y(2));
    p(3,3) = 1.0d0 - hxd*(0.0d0);

```

## 9.2 Program Results

d02ny example results

At t = 10.000, y(1:3) = 0.8, 0.0, 0.2

Diagnostic information

integration status:

last and next step sizes = 0.90178, 0.90178

integration stopped at x = 10.76621

algorithm statistics:

number of time-steps and Newton iterations = 55 78

number of residual and jacobian evaluations = 128 16

order of method last used and next to use = 4 4

component with largest error = 3

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