

NAG Toolbox

nag_ode_dae_dassl_linalg (d02np)

1 Purpose

nag_ode_dae_dassl_linalg (d02np) is a setup function which you must call prior to nag_ode_dae_dassl_gen (d02ne) and after a call to nag_ode_dae_dassl_setup (d02mw), if the Jacobian is to be considered as having a banded structure.

2 Syntax

```
[icom, ifail] = nag_ode_dae_dassl_linalg(neq, ml, mu, icom, 'licom', licom)
[icom, ifail] = d02np(neq, ml, mu, icom, 'licom', licom)
```

3 Description

A call to nag_ode_dae_dassl_linalg (d02np) specifies that the Jacobian to be used is banded in structure. If nag_ode_dae_dassl_linalg (d02np) is not called before a call to nag_ode_dae_dassl_gen (d02ne) then the Jacobian is assumed to be full.

4 References

None.

5 Parameters

5.1 Compulsory Input Parameters

- 1: **neq** – INTEGER
The number of differential-algebraic equations to be solved.
Constraint: $1 \leq \mathbf{neq}$.
- 2: **ml** – INTEGER
 m_L , the number of subdiagonals in the band.
Constraint: $0 \leq \mathbf{ml} \leq \mathbf{neq} - 1$.
- 3: **mu** – INTEGER
 m_U , the number of superdiagonals in the band.
Constraint: $0 \leq \mathbf{mu} \leq \mathbf{neq} - 1$.
- 4: **icom(licom)** – INTEGER array
icom is used to communicate details of the integration from nag_ode_dae_dassl_setup (d02mw) and details of the banded structure of the Jacobian to nag_ode_dae_dassl_gen (d02ne).

5.2 Optional Input Parameters

- 1: **licom** – INTEGER
Default: the dimension of the array **icom**.

The dimension of the array **icom**.

Constraint: $\text{icom} \geq 50 + \text{neq}$.

5.3 Output Parameters

1: **icom**(**icom**) – INTEGER array

2: **ifail** – INTEGER

ifail = 0 unless the function detects an error (see Section 5).

6 Error Indicators and Warnings

Errors or warnings detected by the function:

ifail = 1

Constraint: $\text{neq} \geq 1$.

ifail = 2

Constraint: $\text{ml} \leq \text{neq} - 1$.

Constraint: $\text{ml} \geq 0$.

ifail = 3

Constraint: $\text{mu} \leq \text{neq} - 1$.

Constraint: $\text{mu} \geq 0$.

ifail = 4

Either the initialization function has not been called prior to the first call of this function or the communication array has become corrupted.

ifail = 5

On entry, **licom** is too small.

ifail = -99

An unexpected error has been triggered by this routine. Please contact NAG.

ifail = -399

Your licence key may have expired or may not have been installed correctly.

ifail = -999

Dynamic memory allocation failed.

7 Accuracy

Not applicable.

8 Further Comments

None.

9 Example

See Section 10 in nag_ode_dae_dassl_gen (d02ne) and nag_ode_dae_dassl_setup (d02mw).

9.1 Program Text

```

function d02np_example

fprintf('d02np example results\n\n');

% Initialize the problem, specifying that the Jacobian is to be
% evaluated analytically using the provided routine jac.

neq    = nag_int(3);
maxord = nag_int(5);
jceval = 'Analytic';
hmax   = 0;
h0     = 0;
itol   = nag_int(1);
lcom   = nag_int(200);
[icom, com, ifail] = d02mw(neq, maxord, jceval, hmax, h0, itol, lcom);

% Specify that the Jacobian is banded
mu = nag_int(2);
ml = nag_int(1);
[icom, ifail] = d02np(neq, ml, mu, icom);

% Set initial values
rtol = [1e-3; 1e-3; 1e-3];
atol = [1e-6; 1e-6; 1e-6];
y     = [1; 0; 0];
ydot  = zeros(neq,1);
t     = 0;
tout  = 0.02;

% Use the user parameter to pass the band dimensions through to jac.
% An alternative would be to hard code values for ml and mu in jac.
user = {ml, mu};

fprintf('\n      t           y(1)           y(2)           y(3)      \n');
fprintf(' %8.4f    %12.6f %12.6f %12.6f\n', t, y);

itask = nag_int(0);
% Obtain the solution at 5 equally spaced values of T.
for j = 1:5
    if ifail == 0
        [t, y, ydot, rtol, atol, itask, icom, com, user, ifail] = ...
            d02ne(t, tout, ...
                y, ydot, rtol, atol, itask, @res, @jac, icom, com, 'user', user);
        fprintf(' %8.4f    %12.6f %12.6f %12.6f\n', t, y);
        tout = tout + 0.02;
        icom = d02mc(icom);
    end
end

fprintf('\nThe integrator completed task, ITASK = %d\n', itask);

function [pd, user] = jac(neq, t, y, ydot, pd, cj, user)
    ml = user{1};
    mu = user{2};

    stride = 2*ml+mu+1;
    % Main diagonal pdfull(i,i), i=1,neq
    md = mu + ml + 1;
    pd(md) = -0.04 - cj;
    pd(md+stride) = -1.0e4*y(3) - 6.0e7*y(2) - cj;
    pd(md+2*stride) = -cj;
    % 1 sub-diagonal pdfull(i+1:i), i=1,neq-1
    ms = md + 1;
    pd(ms) = 0.04;
    pd(ms+stride) = 6.0e7*y(2);
    % First super-diagonal pdfull(i-1,i), i=2, neq
    ms = md - 1;
    pd(ms+stride) = 1.0e4*y(3);
    pd(ms+2*stride) = -1.0e4*y(2);

```

```
% Second super-diagonal pdfull(i-2,i), i=3, neq
ms = md - 2;
pd(ms+2*stride) = 1.0e4*y(2);

function [r, ires, user] = res(neq, t, y, ydot, ires, user)
r = zeros(neq, 1);
r(1) = -0.04*y(1) + 1.0e4*y(2)*y(3) - ydot(1);
r(2) = 0.04*y(1) - 1.0e4*y(2)*y(3) - 3.0e7*y(2)*y(2) - ydot(2);
r(3) = 3.0e7*y(2)*y(2) - ydot(3);
```

9.2 Program Results

d02np example results

t	y(1)	y(2)	y(3)
0.0000	1.000000	0.000000	0.000000
0.0200	0.999204	0.000036	0.000760
0.0400	0.998415	0.000036	0.001549
0.0600	0.997631	0.000036	0.002333
0.0800	0.996852	0.000036	0.003112
0.1000	0.996080	0.000036	0.003884

The integrator completed task, ITASK = 3
