

# NAG Library Routine Document

## F06PDF (DSBMV)

**Note:** before using this routine, please read the Users' Note for your implementation to check the interpretation of ***bold italicised*** terms and other implementation-dependent details.

### 1 Purpose

F06PDF (DSBMV) computes the matrix-vector product for a real symmetric band matrix.

### 2 Specification

```
SUBROUTINE F06PDF (UPLO, N, K, ALPHA, A, LDA, X, INCX, BETA, Y, INCY)
INTEGER           N, K, LDA, INCX, INCY
REAL (KIND=nag_wp) ALPHA, A(LDA,*), X(*), BETA, Y(*)
CHARACTER(1)      UPLO
```

The routine may be called by its BLAS name ***dsbmv***.

### 3 Description

F06PDF (DSBMV) performs the matrix-vector operation

$$y \leftarrow \alpha Ax + \beta y,$$

where  $A$  is an  $n$  by  $n$  real symmetric band matrix with  $k$  subdiagonals and  $k$  superdiagonals,  $x$  and  $y$  are  $n$ -element real vectors, and  $\alpha$  and  $\beta$  are real scalars.

### 4 References

None.

### 5 Arguments

- |  |              |
|--|--------------|
| <p>1: UPLO – CHARACTER(1)</p> <p><i>On entry:</i> specifies whether the upper or lower triangular part of <math>A</math> is stored.</p> <p>UPLO = 'U'<br/>The upper triangular part of <math>A</math> is stored.</p> <p>UPLO = 'L'<br/>The lower triangular part of <math>A</math> is stored.</p> <p><i>Constraint:</i> UPLO = 'U' or 'L'.</p> | <i>Input</i> |
| <p>2: N – INTEGER</p> <p><i>On entry:</i> <math>n</math>, the order of the matrix <math>A</math>.</p> <p><i>Constraint:</i> <math>N \geq 0</math>.</p>   | <i>Input</i> |
| <p>3: K – INTEGER</p> <p><i>On entry:</i> <math>k</math>, the number of subdiagonals or superdiagonals of the matrix <math>A</math>.</p> <p><i>Constraint:</i> <math>K \geq 0</math>.</p>  | <i>Input</i> |
| <p>4: ALPHA – REAL (KIND=nag_wp)</p> <p><i>On entry:</i> the scalar <math>\alpha</math>.</p>   | <i>Input</i> |

5:	$A(LDA, \cdot)$ – REAL (KIND=nag_wp) array	<i>Input</i>
<b>Note:</b> the second dimension of the array $A$ must be at least $N$ .		
<i>On entry:</i> the $n$ by $n$ symmetric band matrix $A$ .		
The matrix is stored in rows 1 to $k + 1$ , more precisely,		
	if $\text{UPLO} = 'U'$ , the elements of the upper triangle of $A$ within the band must be stored with element $A_{ij}$ in $A(k + 1 + i - j, j)$ for $\max(1, j - k) \leq i \leq j$ ;	
	if $\text{UPLO} = 'L'$ , the elements of the lower triangle of $A$ within the band must be stored with element $A_{ij}$ in $A(1 + i - j, j)$ for $j \leq i \leq \min(n, j + k)$ .	
6:	$LDA$ – INTEGER	<i>Input</i>
<i>On entry:</i> the first dimension of the array $A$ as declared in the (sub)program from which F06PDF (DSBMV) is called.		
<i>Constraint:</i> $LDA \geq K + 1$ .		
7:	$X(\cdot)$ – REAL (KIND=nag_wp) array	<i>Input</i>
<b>Note:</b> the dimension of the array $X$ must be at least $\max(1, 1 + (N - 1) \times  \text{INCX} )$ .		
<i>On entry:</i> the $n$ -element vector $x$ .		
If $\text{INCX} > 0$ , $x_i$ must be stored in $X(1 + (i - 1) \times \text{INCX})$ , for $i = 1, 2, \dots, N$ .		
If $\text{INCX} < 0$ , $x_i$ must be stored in $X(1 - (N - i) \times \text{INCX})$ , for $i = 1, 2, \dots, N$ .		
Intermediate elements of $X$ are not referenced.		
8:	$\text{INCX}$ – INTEGER	<i>Input</i>
<i>On entry:</i> the increment in the subscripts of $X$ between successive elements of $x$ .		
<i>Constraint:</i> $\text{INCX} \neq 0$ .		
9:	$\text{BETA}$ – REAL (KIND=nag_wp)	<i>Input</i>
<i>On entry:</i> the scalar $\beta$ .		
10:	$Y(\cdot)$ – REAL (KIND=nag_wp) array	<i>Input/Output</i>
<b>Note:</b> the dimension of the array $Y$ must be at least $\max(1, 1 + (N - 1) \times  \text{INCY} )$ .		
<i>On entry:</i> the $n$ -element vector $y$ , if $\text{BETA} = 0.0$ $Y$ need not be set.		
If $\text{INCY} > 0$ , $y_i$ must be stored in $Y(1 + (i - 1) \times \text{INCY})$ , for $i = 1, 2, \dots, N$ .		
If $\text{INCY} < 0$ , $y_i$ must be stored in $Y(1 - (N - i) \times \text{INCY})$ , for $i = 1, 2, \dots, N$ .		
<i>On exit:</i> the updated vector $y$ stored in the array elements used to supply the original vector $y$ .		
11:	$\text{INCY}$ – INTEGER	<i>Input</i>
<i>On entry:</i> the increment in the subscripts of $Y$ between successive elements of $y$ .		
<i>Constraint:</i> $\text{INCY} \neq 0$ .		

## 6 Error Indicators and Warnings

None.

## 7 Accuracy

Not applicable.

## **8 Parallelism and Performance**

F06PDF (DSBMV) is not threaded in any implementation.

## **9 Further Comments**

None.

## **10 Example**

None.

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