NAG Library Routine Document

F06QSF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of ***bold italicised*** terms and other implementation-dependent details.

1 Purpose

F06QSF performs a QR or RQ factorization (as a sequence of plane rotations) of a real upper spiked matrix.

2 Specification

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SUBROUTINE F06QSF (SIDE, N, K1, K2, C, S, A, LDA)
INTEGER            N, K1, K2, LDA
REAL (KIND=nag_wp) C(K2-1), S(*), A(LDA,*)
CHARACTER(1)       SIDE
```

3 Description

F06QSF transforms an n by n real upper spiked matrix H to upper triangular form R by applying a real orthogonal matrix P from the left or the right. P is formed as a sequence of plane rotations in planes k_1 to k_2.

If SIDE = 'L', H is assumed to have a row spike, with nonzero elements $h_{k_2,k}$, for $k = k_1, \ldots, k_2 - 1$. The rotations are applied from the left:

$$PH = R,$$

where $P = P_{k_2-1} \cdots P_{k_1+1} P_{k_1}$ and P_k is a rotation in the (k, k_2) plane.

If SIDE = 'R', H is assumed to have a column spike, with nonzero elements h_{k+1,k_1}, for $k = k_1, \ldots, k_2 - 1$. The rotations are applied from the right:

$$HP^{\mathrm{T}} = R,$$

where $P = P_{k_1} P_{k_1+1} \cdots P_{k_2-1}$ and P_k is a rotation in the $(k_1, k+1)$ plane.

The 2 by 2 plane rotation part of P_k has the form

$$\begin{pmatrix} c_k & s_k \\ -s_k & c_k \end{pmatrix}.$$

4 References

None.

5 Arguments

1: SIDE – CHARACTER(1) *Input*

On entry: specifies whether H is operated on from the left or the right.

SIDE = 'L'
H is pre-multiplied from the left.

SIDE = 'R'
H is post-multiplied from the right.

Constraint: SIDE = 'L' or 'R'.

2: N – INTEGER *Input*

On entry: n, the order of the matrix H.

Constraint: N ≥ 0.

3: K1 – INTEGER *Input*

4: K2 – INTEGER *Input*

On entry: the values k_1 and k_2.

If K1 < 1 or K2 $\leq$ K1 or K2 $>$ N, an immediate return is effected.

5: C(K2 $-$ 1) – REAL (KIND=nag_wp) array *Output*

On exit: C(k) holds c_k, the cosine of the rotation P_k, for $k = k_1, \ldots, k_2 - 1$.

6: S$(*)$ – REAL (KIND=nag_wp) array *Input/Output*

Note: the dimension of the array S must be at least K2 $-$ K1.

On entry: the nonzero elements of the spike of H: S(k) must hold $h_{k_2,k}$ if SIDE = 'L', and h_{k+1,k_1} if SIDE = 'R', for $k = k_1, \ldots, k_2 - 1$.

On exit: S(k) holds s_k, the sine of the rotation P_k, for $k = k_1, \ldots, k_2 - 1$.

7: A(LDA, $*$) – REAL (KIND=nag_wp) array *Input/Output*

Note: the second dimension of the array A must be at least N.

On entry: the upper triangular part of the n by n upper spiked matrix H.

On exit: the upper triangular matrix R.

8: LDA – INTEGER *Input*

On entry: the first dimension of the array A as declared in the (sub)program from which F06QSF is called.

Constraint: LDA $\geq \max(1, \text{N})$.

6 Error Indicators and Warnings

None.

7 Accuracy

Not applicable.

8 Parallelism and Performance

F06QSF is not threaded in any implementation.

9 Further Comments

None.

10 Example

None.