# NAG Library Routine Document

# G13DLF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

## 1 Purpose

G13DLF differences and/or transforms a multivariate time series. It is intended to be used prior to G13DDF to fit a vector autoregressive moving average (VARMA) model to the differenced/transformed series.

# 2 Specification

```
SUBROUTINE G13DLF (K, N, Z, KMAX, TR, ID, DELTA, W, ND, WORK, IFAIL)
INTEGER K, N, KMAX, ID(K), ND, IFAIL
REAL (KIND=nag_wp) Z(KMAX,N), DELTA(KMAX,*), W(KMAX,*), WORK(K*N)
CHARACTER(1) TR(K)
```

# **3** Description

For certain time series it may first be necessary to difference the original data to obtain a stationary series before calculating autocorrelations, etc. This routine also allows you to apply either a square root or a log transformation to the original time series to stabilize the variance if required.

If the order of differencing required for the *i*th series is  $d_i$ , then the differencing operator is defined by  $\delta_i(B) = 1 - \delta_{i1}B - \delta_{i2}B^2 - \cdots - \delta_{id_i}B^{d_i}$ , where B is the backward shift operator; that is,  $BZ_t = Z_{t-1}$ . Let d denote the maximum of the orders of differencing,  $d_i$ , over the k series. The routine computes values of the differenced/transformed series  $W_t = (w_{1t}, w_{2t}, \dots, w_{kt})^T$ , for  $t = d + 1, \dots, n$ , as follows:

$$w_{it} = \delta_i(B) z_{it}^*, \quad i = 1, 2, \dots, k$$

where  $z_{it}^*$  are the transformed values of the original k-dimensional time series  $Z_t = (z_{1t}, z_{2t}, \dots, z_{kt})^T$ . The differencing parameters  $\delta_{ij}$ , for  $i = 1, 2, \dots, k$  and  $j = 1, 2, \dots, d_i$ , must be supplied by you. If the *i*th series does not require differencing, then  $d_i = 0$ .

# 4 References

Box G E P and Jenkins G M (1976) *Time Series Analysis: Forecasting and Control* (Revised Edition) Holden–Day

Wei W W S (1990) Time Series Analysis: Univariate and Multivariate Methods Addison-Wesley

# **5** Parameters

1: K – INTEGER

On entry: k, the dimension of the multivariate time series. Constraint:  $K \ge 1$ .

### 2: N – INTEGER

On entry: n, the number of observations in the series, prior to differencing. Constraint:  $N \ge 1$ . Input

Input

3:	Z(KMAX, N) – REAL (KIND=nag_wp) array Input						
	On entry: $Z(i, t)$ must contain, $z_{it}$ , the <i>i</i> th component of $Z_t$ , for $i = 1, 2,, k$ and $t = 1, 2,, n$ .						
	Constraints:						
	if $\text{TR}(i) = \text{'L'}$ , $Z(i, t) > 0.0$ ; if $\text{TR}(i) = \text{'S'}$ , $Z(i, t) \ge 0.0$ , for $i = 1, 2,, k$ and $t = 1, 2,, n$ .						
4:	KMAX – INTEGER Input						
	<i>On entry</i> : the first dimension of the arrays Z, DELTA and W as declared in the (sub)program from which G13DLF is called.						
	Constraint: $KMAX \ge K$ .						
5:	TR(K) – CHARACTER(1) array Input						
	On entry: $TR(i)$ indicates whether the <i>i</i> th time series is to be transformed, for $i = 1, 2,, k$ .						
	$\mathrm{TR}(i) = '\mathrm{N}'$						
	No transformation is used. TR(i) = 'L'						
	$A \log$ transformation is used.						
	TR(i) = 'S'						
	A square root transformation is used. Constraint: $TR(i) = 'N'$ , 'L' or 'S', for $i = 1, 2,, k$ .						
6:	ID(K) – INTEGER array Input						
	On entry: the order of differencing for each series, $d_1, d_2, \ldots, d_k$ . Constraint: $0 \le ID(i) < N$ , for $i = 1, 2, \ldots, K$ .						
7:	DELTA(KMAX,*) – REAL (KIND=nag_wp) array Input						
	Note: the second dimension of the array DELTA must be at least $\max(1, d)$ , where $d = \max(\text{ID}(i))$ .						
	On entry: if $ID(i) > 0$ , then $DELTA(i, j)$ must be set equal to $\delta_{ij}$ , for $j = 1, 2,, d_i$ and $i = 1, 2,, k$ .						
	If $d = 0$ , then DELTA is not referenced.						
8:	W(KMAX,*) – REAL (KIND=nag_wp) array Output						
	Note: the second dimension of the array W must be at least $N - d$ , where $d = \max(ID(i))$ .						
	On exit: $W(i, t)$ contains the value of $w_{i,t+d}$ , for $i = 1, 2,, k$ and $t = 1, 2,, n - d$ .						
9:	ND – INTEGER Output						
	On exit: the number of differenced values, $n - d$ , in the series, where $d = \max(ID(i))$ .						
10:	$WORK(K \times N) - REAL (KIND=nag_wp) array Workspace$						
11:	IFAIL – INTEGER Input/Output						
	On entry: IFAIL must be set to 0, $-1$ or 1. If you are unfamiliar with this parameter you shoul refer to Section 3.3 in the Essential Introduction for details.						
	For environments where it might be inappropriate to halt program execution when an error is detected, the value $-1$ or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this parameter, the						

recommended value is 0. When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.

On exit: IFAIL = 0 unless the routine detects an error or a warning has been flagged (see Section 6).

# 6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

IFAIL = 2

On entry, ID(i) < 0, for some i = 1, 2, ..., k, or  $ID(i) \ge N$ , for some i = 1, 2, ..., k.

#### IFAIL = 3

On entry, at least one of the first k elements of TR is not equal to 'N', 'L' or 'S'.

#### IFAIL = 4

On entry, one or more of the elements of Z is invalid, for the transformation requested; that is, you may be trying to log or square root a series, some of whose values are negative.

#### IFAIL = -99

An unexpected error has been triggered by this routine. Please contact NAG.

See Section 3.8 in the Essential Introduction for further information.

IFAIL = -399

Your licence key may have expired or may not have been installed correctly.

See Section 3.7 in the Essential Introduction for further information.

### IFAIL = -999

Dynamic memory allocation failed.

See Section 3.6 in the Essential Introduction for further information.

### 7 Accuracy

The computations are believed to be stable.

### 8 Parallelism and Performance

G13DLF is not threaded by NAG in any implementation.

G13DLF makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this routine. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

### **9** Further Comments

The same differencing operator does not have to be applied to all the series. For example, suppose we have k = 2, and wish to apply the second-order differencing operator  $\nabla^2$  to the first series and the first-order differencing operator  $\nabla$  to the second series:

$$w_{1t} = \nabla^2 z_{1t} = (1-B)^2 z_{1t} = (1-2B+B^2)z_{1t},$$
 and  
 $w_{2t} = \nabla z_{2t} = (1-B)z_{2t}.$ 

Then  $d_1 = 2, d_2 = 1, d = \max(d_1, d_2) = 2$ , and

$$DELTA = \begin{bmatrix} \delta_{11} & \delta_{12} \\ \delta_{21} \end{bmatrix} = \begin{bmatrix} 2 & -1 \\ 1 \end{bmatrix}$$

### 10 Example

A program to difference (non-seasonally) each of two time series of length 48. No transformation is to be applied to either of the series.

#### 10.1 Program Text

```
Program g13dlfe
      G13DLF Example Program Text
1
1
     Mark 25 Release. NAG Copyright 2014.
1
      .. Use Statements ..
     Use nag_library, Only: g13dlf, nag_wp
     .. Implicit None Statement ..
1
     Implicit None
!
      .. Parameters ..
     Integer, Parameter
                                       :: nin = 5, nout = 6
      .. Local Scalars ..
1
     Integer
                                        :: d, i, ifail, k, kmax, n, nd, tddelta
1
      .. Local Arrays ..
     Real (Kind=nag_wp), Allocatable :: delta(:,:), w(:,:), work(:), z(:,:)
     Integer, Allocatable
                                       :: id(:)
                                       :: tr(:)
     Character (1), Allocatable
1
      .. Intrinsic Procedures ..
     Intrinsic
                                        :: max, maxval
!
      .. Executable Statements ..
     Write (nout,*) 'G13DLF Example Program Results'
     Write (nout,*)
1
     Skip heading in data file
     Read (nin,*)
1
     Read in problem size
     Read (nin,*) k, n
     Allocate (id(k))
     Read in differencing
1
     Read (nin,*) id(1:k)
     d = maxval(id(1:k))
     tddelta = max(d, 1)
     nd = n - d
     kmax = k
     Allocate (z(kmax,n),tr(k),delta(kmax,tddelta),w(kmax,nd),work(k*n))
```

```
!
     Read in series and the transformation flag
     Read (nin,*)(z(i,1:n),i=1,k)
     Read (nin,*) tr(1:k)
1
     If required, read in delta
     If (d>0) Then
       Read (nin,*)(delta(i,1:id(i)),i=1,k)
     End If
!
     Difference and / or transform series
     ifail = 0
     Call g13dlf(k,n,z,kmax,tr,id,delta,w,nd,work,ifail)
1
     Display results
     Write (nout,*) ' Transformed/Differenced series'
     Write (nout,*) ' ------'
     Do i = 1, k
       Write (nout,*)
       Write (nout, 99999) ' Series ', i
       Write (nout,*) ' -----'
       Write (nout,*)
       Write (nout, 99998) ' Number of differenced values = ', nd
       Write (nout,*)
       Write (nout,99997) w(i,1:nd)
     End Do
99999 Format (1X,A,I2)
99998 Format (1X,A,I6)
99997 Format (1X,8F9.3)
   End Program g13dlfe
```

#### 10.2 Program Data

G13DLF Example Program Data :: K,N 2 48 1 :: ID 1 1 -1.490 -1.620 5.200 6.230 6.210 5.860 4.090 3.180 2.620 1.490 1.170 0.850 -0.350 0.240 2.440 2.580 2.040 0.400 2.260 3.340 5.090 5.000 4.780 4.110 3.450 1.650 1.290 4.090 6.320 7.500 3.890 1.580 5.2105.2504.9307.3805.8705.8109.6809.0707.2907.8407.5507.3207.9707.7607.0008.3507.3406.3506.9608.5406.6204.9704.5504.810 4.750 4.760 10.880 10.010 11.620 10.360 6.400 6.240 7.9304.0403.7305.6005.3506.8108.2707.6806.6506.08010.2509.14017.75013.3009.6306.8004.0805.0604.9406.6507.94010.76011.8905.850 9.010 7.500 10.020 10.380 8.150 8.370 10.730 12.140 :: End of Z 'N' 'N' :: TR 1.0 1.0 :: End of DELTA

#### **10.3 Program Results**

G13DLF Example Program Results

Transformed/Differenced series Series 1 \_\_\_\_\_ Number of differenced values = 47 -0.130 6.820 1.030 -0.020 -0.350 -1.770 -0.910 -0.560 -1.200 0.140 -1.130 -0.320 -0.320 0.590 2.200 -0.540 -1.640 1.860 1.080 1.750 -0.090 -0.220 -0.670 -0.660 -0.360 2.800 2.230 1.180 -3.610 -1.800 -2.310 3.630 -0.320 2.450 -1.510 -0.060 3.870 -0.610 0.040 -1.780

0.550	-0.290	-0.230	0.650	-0.210	-0.760	1.350				
Series 2										
Number of differenced values = 47										
-0.990 0.010 -3.890 -0.570 0.980 -1.510	0.610 6.120 -0.310 4.170 -0.120 2.520	1.580 -0.870 1.870 -1.110 1.710 0.360	-1.920 1.610 -0.250 8.610 1.290 -2.230	-1.650 -1.260 1.460 -4.450 2.820 0.220	-0.420 -3.960 1.460 -3.670 1.130 2.360	0.260 -0.160 -0.590 -2.830 -6.040 1.410	-0.060 1.690 -1.030 -2.720 3.160			