NAG Library Routine Document

G13BJF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of ***bold italicised*** terms and other implementation-dependent details.

1 Purpose

G13BJF produces forecasts of a time series (the output series) which depends on one or more other (input) series via a previously estimated multi-input model for which the state set information is not available. The future values of the input series must be supplied. In contrast with G13BHF the original past values of the input and output series are required. Standard errors of the forecasts are produced. If future values of some of the input series have been obtained as forecasts using ARIMA models for those series, this may be allowed for in the calculation of the standard errors.

2 Specification

```
SUBROUTINE G13BJF (MR, NSER, MT, PARA, NPARA, KFC, NEV, NFV, XXY, LDXXY,    &
                   KZEF, RMSXY, MRX, PARX, LDPARX, FVA, FSD, STTF,          &
                   ISTTF, NSTTF, WA, IWA, MWA, IMWA, IFAIL)
INTEGER            MR(7), NSER, MT(4,NSER), NPARA, KFC, NEV, NFV,           &
                   LDXXY, KZEF, MRX(7,NSER), LDPARX, ISTTF, NSTTF, IWA,     &
                   MWA(IMWA), IMWA, IFAIL
REAL (KIND=nag_wp) PARA(NPARA), XXY(LDXXY,NSER), RMSXY(NSER),               &
                   PARX(LDPARX,NSER), FVA(NFV), FSD(NFV), STTF(ISTTF),      &
                   WA(IWA)
```

3 Description

G13BJF has two stages. The first stage is essentially the same as a call to the model estimation routine G13BEF, with zero iterations. In particular, all the parameters remain unchanged in the supplied input series transfer function models and output noise series ARIMA model. The internal nuisance parameters associated with the pre-observation period effects of the input series are estimated where requested, and so are any backforecasts of the output noise series. The output components z_t and n_t, and residuals a_t are calculated exactly as in Section 3 in G13BEF, and the state set for forecasting is constituted.

The second stage is essentially the same as a call to the forecasting routine G13BHF. The same information is required, and the same information is returned.

Use of G13BJF should be confined to situations in which the state set for forecasting is unknown. Forecasting from the original data is relatively expensive because it requires recalculation of the state set. G13BJF returns the state set for use in producing further forecasts using G13BHF, or for updating the state set using G13BGF.

4 References

Box G E P and Jenkins G M (1976) *Time Series Analysis: Forecasting and Control* (Revised Edition) Holden–Day

5 Parameters

1: MR(7) – INTEGER array *Input*

On entry: the orders vector (p, d, q, P, D, Q, s) of the ARIMA model for the output noise component.

p, q, P and Q refer respectively to the number of autoregressive (ϕ), moving average (θ), seasonal autoregressive (Φ) and seasonal moving average (Θ) parameters.

d, D and s refer respectively to the order of non-seasonal differencing, the order of seasonal differencing and the seasonal period.

Constraints:

$p,\ d,\ q,\ P,\ D,\ Q,\ s \geq 0$;
$p + q + P + Q > 0$;
$s \neq 1$;
if $s = 0$, $P + D + Q = 0$;
if $s > 1$, $P + D + Q > 0$;
$d + s \times (P + D) \leq n$;
$p + d - q + s \times (P + D - Q) \leq n$.

2: NSER – INTEGER *Input*

On entry: the number of input and output series. There may be any number of input series (including none), but only one output series.

3: MT(4, NSER) – INTEGER array *Input*

On entry: the transfer function model orders b, p and q of each of the input series. The data for input series i is held in column i. Row 1 holds the value b_i, row 2 holds the value q_i and row 3 holds the value p_i.

For a simple input, $b_i = q_i = p_i = 0$.

Row 4 holds the value r_i, where $r_i = 1$ for a simple input, and $r_i = 2$ or 3 for a transfer function input.

The choice $r_i = 3$ leads to estimation of the pre-period input effects as nuisance parameters, and $r_i = 2$ suppresses this estimation. This choice may affect the returned forecasts and the state set.

When $r_i = 1$, any nonzero contents of rows 1, 2 and 3 of column i are ignored.

Constraint: $\mathrm{MT}(4, i) = 1$, 2 or 3, for $i = 1, 2, \ldots, \mathrm{NSER} - 1$.

4: PARA(NPARA) – REAL (KIND=nag_wp) array *Input/Output*

On entry: estimates of the multi-input model parameters. These are in order, firstly the ARIMA model parameters: p values of ϕ parameters, q values of θ parameters, P values of Φ parameters, Q values of Θ parameters.

These are followed by the transfer function model parameter values $\omega_0, \omega_1, \ldots, \omega_{q_1}$, $\delta_1, \ldots, \delta_{p_1}$ for the first of any input series and similarly for each subsequent input series. The final component of PARA is the value of the constant c.

On exit: the parameter values may be updated using an additional iteration in the estimation process.

5: NPARA – INTEGER *Input*

On entry: the exact number of ϕ, θ, Φ, Θ, ω, δ, c parameters, so that $\mathrm{NPARA} = p + q + P + Q + \mathrm{NSER} + \sum(p + q)$, the summation being over all the input series. (c must be included whether its value was previously estimated or was set fixed.)

6: KFC – INTEGER *Input*

On entry: must be set to 1 if the constant was estimated when the model was fitted, and 0 if it was held at a fixed value. This only affects the degrees of freedom used in calculating the estimated residual variance.

Constraint: $\mathrm{KFC} = 0$ or 1.

7: NEV – INTEGER *Input*

On entry: the number of original (undifferenced) values in each of the input and output time series.

8: NFV – INTEGER *Input*

On entry: the number of forecast values of the output series required.

Constraint: $\text{NFV} > 0$.

9: XXY(LDXXY, NSER) – REAL (KIND=nag_wp) array *Input/Output*

On entry: the columns of XXY must contain in the first NEV places, the past values of each of the input and output series, in that order. In the next NFV places, the columns relating to the input series (i.e., columns 1 to $\text{NSER} - 1$) contain the future values of the input series which are necessary for construction of the forecasts of the output series y.

On exit: if $\text{KZEF} = 0$ then XXY is unchanged except that the relevant NFV values in the column relating to the output series (column NSER) contain the forecast values (FVA), but if $\text{KZEF} \neq 0$ then the columns of XXY contain the corresponding values of the input component series z_t and the values of the output noise component n_t, in that order.

10: LDXXY – INTEGER *Input*

On entry: the first dimension of the array XXY as declared in the (sub)program from which G13BJF is called.

Constraint: $\text{LDXXY} \geq (\text{NEV} + \text{NFV})$.

11: KZEF – INTEGER *Input*

On entry: must be set to 0 if the relevant NFV values of the forecasts (FVA) are to be held in the output series column (NSER) of XXY (which is otherwise unchanged) on exit, and must not be set to 0 if the values of the input component series z_t and the values of the output noise component n_t are to overwrite the contents of XXY on exit.

12: RMSXY(NSER) – REAL (KIND=nag_wp) array *Input/Output*

On entry: the first $(\text{NSER} - 1)$ elements of RMSXY must contain the estimated residual variance of the input series ARIMA models. In the case of those inputs for which no ARIMA model is available or its effects are to be excluded in the calculation of forecast standard errors, the corresponding entry of RMSXY should be set to 0.

On exit: RMSXY(NSER) contains the estimated residual variance of the output noise ARIMA model which is calculated from the supplied series. Otherwise RMSXY is unchanged.

13: MRX(7, NSER) – INTEGER array *Input/Output*

On entry: the orders array for each of the input series ARIMA models. Thus, column i contains values of p, d, q, P, D, Q, s for input series i. In the case of those inputs for which no ARIMA model is available, the corresponding orders should be set to 0.

On exit: unchanged, except for column NSER which is used as workspace.

14: PARX(LDPARX, NSER) – REAL (KIND=nag_wp) array *Input*

On entry: values of the parameters (ϕ, θ, Φ, and Θ) for each of the input series ARIMA models.

Thus column i contains $\text{MRX}(1, i)$ values of ϕ, $\text{MRX}(3, i)$ values of θ, $\text{MRX}(4, i)$ values of Φ and $\text{MRX}(6, i)$ values of Θ, in that order.

Values in the columns relating to those input series for which no ARIMA model is available are ignored.

15: LDPARX – INTEGER *Input*

On entry: the first dimension of the array PARX as declared in the (sub)program from which G13BJF is called.

Constraint: LDPARX $\geq nce$, where nce is the maximum number of parameters in any of the input series ARIMA models. If there are no input series, then LDPARX ≥ 1.

16: FVA(NFV) – REAL (KIND=nag_wp) array *Output*

On exit: the required forecast values for the output series. (Note that these are also output in column NSER of XXY if KZEF $= 0$.)

17: FSD(NFV) – REAL (KIND=nag_wp) array *Output*

On exit: the standard errors for each of the forecast values.

18: STTF(ISTTF) – REAL (KIND=nag_wp) array *Output*

On exit: the NSTTF values of the state set based on the first NEV sets of (past) values of the input and output series.

19: ISTTF – INTEGER *Input*

On entry: the dimension of the array STTF as declared in the (sub)program from which G13BJF is called.

Constraint: ISTTF $\geq (P \times s) + d + (D \times s) + q + \max(p, Q \times s) + ncf$, where $ncf = \sum(b_i + q_i + p_i)$ and the summation is over all input series for which $r_i > 1$.

20: NSTTF – INTEGER *Output*

On exit: the number of values in the state set array STTF.

21: WA(IWA) – REAL (KIND=nag_wp) array *Workspace*
22: IWA – INTEGER *Input*

On entry: the dimension of the array WA as declared in the (sub)program from which G13BJF is called.

It is not practical to outline a method for deriving the exact minimum permissible value of IWA, but the following gives a reasonably good approximation which tends to be on the conservative side.

Note: there are three error indicators associated with IWA. These are IFAIL $= 4$, 5 or 6. The first of these probably indicates an abnormal entry value of NFV, while the second indicates that IWA is much too small and needs to be increased by a substantial amount. The last of these indicates that IWA is too small but returns the necessary minimum value in MWA(1).

Let $q' = q + (Q \times s)$ and $d' = d + (D \times s)$, where the output noise ARIMA model orders are p, d, q, P, D, Q, s.

Let there be l input series, where $l = \text{NSER} - 1$.

Let $mx_i = \max(b_i + q_i, p_i)$,
if $r_i = 3$, for $i = 1, 2, \ldots, l$, if $l > 0$
$mx_i = 0$, if $r_i \neq 3$, for $i = 1, 2, \ldots, l$, if $l > 0$

where the transfer function model orders of input series i are given by b_i, q_i, p_i, r_i.

Let $qx = \max(q', mx_1, mx_2, \ldots, mx_l)$

Let $ncg = \text{NPARA} + qx + \sum_{i=1}^{l} mx_i$ and $nch = N + d + 6 \times qx$.

Finally, let $nci = \text{NSER}$, and then increment nci by 1 every time any of the following conditions are satisfied. (The last two conditions should be applied separately to each input series, so that for example if we have two input series and $p_1 > 0$ and $p_2 > 0$, then nci is incremented by 2 in respect of these.)

The conditions are:

$p > 0$

$q > 0$

$P > 0$

$Q > 0$

$qx > 0$

$mx_i > 0$, separately, for $i = 1, 2, \ldots, l$, if $l > 0$

$p_i > 0$, separately, for $i = 1, 2, \ldots, l$, if $l > 0$,

then $\text{IWA} > 2 \times (ncg)^2 + nch \times (nci + 4)$.

23: MWA(IMWA) – INTEGER array *Workspace*

24: IMWA – INTEGER *Input*

On entry: the dimension of the array MWA as declared in the (sub)program from which G13BJF is called.

Constraint: $\text{IMWA} \geq (16 \times \text{NSER}) + (7 \times ncg) + (3 \times \text{NPARA}) + 27$.

The derivation of ncg is described under IWA.

When IMWA is too small, as indicated by $\text{IFAIL} = 7$, the requisite minimum value of IMWA is returned in MWA(1).

25: IFAIL – INTEGER *Input/Output*

On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Section 3.3 in the Essential Introduction for details.

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this parameter, the recommended value is 0. **When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.**

On exit: $\text{IFAIL} = 0$ unless the routine detects an error or a warning has been flagged (see Section 6).

6 Error Indicators and Warnings

If on entry $\text{IFAIL} = 0$ or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

$\text{IFAIL} = 1$

On entry, $\text{KFC} < 0$,
or $\text{KFC} > 1$,
or $\text{LDXXY} < (\text{NEV} + \text{NFV})$,
or $\text{NFV} \leq 0$.

IFAIL $= 2$

On entry, LDPARX is too small or NPARA is inconsistent with the orders specified in arrays MR and MT; or one of the r_i, stored in MT$(4, i)$, does not equal 1, 2 or 3.

IFAIL $= 3$

On entry or during execution, one or more sets of δ parameters do not satisfy the stationarity or invertibility test conditions.

IFAIL $= 4$

On entry, IWA is too small for the final forecasting calculations. This is a highly unlikely error, and would probably indicate that NFV was abnormally large.

IFAIL $= 5$

On entry, IWA is too small by a very considerable margin. No information is supplied about the requisite minimum size.

IFAIL $= 6$

On entry, IWA is too small, but the requisite minimum size is returned in MWA(1).

IFAIL $= 7$

On entry, IMWA is too small, but the requisite minimum size is returned in MWA(1).

IFAIL $= 8$

This indicates a failure in F04ASF which is used to solve the equations giving the latest estimates of the parameters.

IFAIL $= 9$

This indicates a failure in the inversion of the second derivative matrix associated with parameter estimation.

IFAIL $= 10$

On entry or during execution, one or more sets of the ARIMA (ϕ, θ, Φ or Θ) parameters do not satisfy the stationarity or invertibility test conditions.

IFAIL $= 11$

On entry, ISTTF is too small.

IFAIL $= -99$

An unexpected error has been triggered by this routine. Please contact NAG.

See Section 3.8 in the Essential Introduction for further information.

IFAIL $= -399$

Your licence key may have expired or may not have been installed correctly.

See Section 3.7 in the Essential Introduction for further information.

IFAIL $= -999$

Dynamic memory allocation failed.

See Section 3.6 in the Essential Introduction for further information.

7 Accuracy

The computations are believed to be stable.

8 Parallelism and Performance

G13BJF is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

G13BJF makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this routine. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

The time taken by G13BJF is approximately proportional to the product of the length of each series and the square of the number of parameters in the multi-input model.

10 Example

The data in this example relates to 40 observations of an output time series and 5 input time series. The output series has one autoregressive (ϕ) parameter and one seasonal moving average (Θ) parameter, with initial values $\phi = 0.495$, $\Theta = 0.238$ and $c = -82.858$. The seasonal period is 4. This example differs from the example in G13BEF in that four of the input series are simple series and the fifth is defined by a transfer function with orders $b_5 = 1$, $q_5 = 0$, $p_5 = 1$, $r_5 = 3$, which allows for pre-observation period effects. The initial values for the transfer model are:

$$\omega_1 = -0.367, \quad \omega_2 = -3.876, \quad \omega_3 = 4.516, \quad \omega_4 = 2.474 \quad \omega_5 = 8.629, \quad \delta_1 = 0.688.$$

A further 8 values of the input series are supplied, and it is assumed that the values for the fifth series have themselves been forecast from an ARIMA model with orders $2 \;\; 0 \;\; 2 \;\; 0 \;\; 1 \;\; 1 \;\; 4$, in which $\phi_1 = 1.6743$, $\phi_2 = -0.9505$, $\theta_1 = 1.4605$, $\theta_2 = -0.4862$ and $\Theta_1 = 0.8993$, and for which the residual mean square is 0.1720.

The following are computed and printed out: the state set after initial processing of the original 40 sets of values, the estimated residual variance for the output noise series, the 8 forecast values and their standard errors, and the values of the components z_t and the output noise component n_t.

10.1 Program Text

```
    Program g13bjfe

!     G13BJF Example Program Text

!     Mark 25 Release. NAG Copyright 2014.

!     .. Use Statements ..
      Use nag_library, Only: g13bjf, nag_wp, x04caf
!     .. Implicit None Statement ..
      Implicit None
!     .. Parameters ..
      Integer, Parameter               :: nin = 5, nout = 6
!     .. Local Scalars ..
      Integer                          :: dp, i, ifail, imwa, isttf, iwa, kfc, &
                                          kzef, ldparx, ldxxy, mx, n, ncf,     &
                                          ncg, nch, nci, nev, nfv, nis, npara, &
                                          nparx, nser, nsttf, qp, qx, smx
!     .. Local Arrays ..
      Real (Kind=nag_wp), Allocatable  :: fsd(:), fva(:), para(:), parx(:,:),  &
                                          rmsxy(:), sttf(:), wa(:), xxy(:,:)
```

```
      Integer                          :: mr(7)
      Integer, Allocatable             :: mrx(:,:), mt(:,:), mwa(:)
!     .. Intrinsic Procedures ..
      Intrinsic                        :: max, sum
!     .. Executable Statements ..
      Write (nout,*) 'G13BJF Example Program Results'
      Write (nout,*)

!     Skip heading in data file
      Read (nin,*)

!     Read in problem size
      Read (nin,*) kfc, nev, nfv, nser, kzef

!     Number of input series
      nis = nser - 1

      Allocate (mt(4,nser))

!     Read in the orders for the output noise
      Read (nin,*) mr(1:7)

!     Read in transfer function
      Do i = 1, nis
        Read (nin,*) mt(1:4,i)
      End Do

!     Calculate NPARA
      npara = 0
      Do i = 1, nis
        npara = npara + mt(2,i) + mt(3,i)
      End Do
      npara = npara + mr(1) + mr(3) + mr(4) + mr(6) + nser

!     Calculate array sizes
      n = nev + nfv
      ldxxy = n
      ncf = 0
      Do i = 1, nis
        If (mt(4,i)>1) Then
          ncf = sum(mt(1:3,i))
        End If
      End Do
      isttf = mr(4)*mr(7) + mr(2) + mr(5)*mr(7) + mr(3) + &
        max(mr(1),mr(6)*mr(7)) + ncf
      qp = mr(3) + mr(6)*mr(7)
      dp = mr(2) + mr(5)*mr(7)
      smx = 0
      qx = qp
      nci = nser
      Do i = 1, nis
        If (mt(4,i)==3) Then
          mx = max(mt(1,i)+mt(2,i),mt(3,i))
          nci = nci + 1
        Else
          mx = 0
        End If
        If (mt(3,i)>0) Then
          nci = nci + 1
        End If
        smx = smx + mx
        qx = max(qx,mx)
      End Do
      ncg = npara + qx + smx
      nch = dp + 6*qx + nev
      If (qx>0) Then
        nci = nci + 1
      End If
      If (mr(1)>0) Then
        nci = nci + 1
      End If
```

```
      If (mr(3)>0) Then
        nci = nci + 1
      End If
      If (mr(4)>0) Then
        nci = nci + 1
      End If
      If (mr(6)>0) Then
        nci = nci + 1
      End If
      iwa = 2*(ncg**2) + nch*(nci+4)
      imwa = 16*nser + 7*ncg + 3*npara + 27
      Allocate (para(npara),xxy(ldxxy,nser),rmsxy(nser),mrx(7,nser),fva(nfv), &
        fsd(nfv),sttf(isttf),wa(iwa),mwa(imwa))

!     Read in multi-input model parameters
      Read (nin,*) para(1:npara)

!     Read in the observed values for the input and output series
      Read (nin,*)(xxy(i,1:nser),i=1,nev)

!     Read in the future values for the input series
      Read (nin,*)(xxy(nev+i,1:nis),i=1,nfv)

      If (nis>=1) Then
!       Read in residual variance of input series
        Read (nin,*) rmsxy(1:nis)

!       Read in orders for input series ARIMA where available
!       (i.e. where residual variance is not zero)
        ldparx = 0
        Do i = 1, nis
          If (rmsxy(i)/=0.0E0_nag_wp) Then
            Read (nin,*) mrx(1:7,i)
            nparx = mrx(1,i) + mrx(3,i) + mrx(4,i) + mrx(6,i)
            ldparx = max(ldparx,nparx)
          Else
            mrx(1:7,i) = 0
          End If
        End Do
      Else
!       No input series
        ldparx = 1
      End If

      Allocate (parx(ldparx,nser))

!     Read in parameters for each input series ARIMA
      If (nis>0) Then
        Do i = 1, nis
          If (rmsxy(i)/=0.0E0_nag_wp) Then
            nparx = mrx(1,i) + mrx(3,i) + mrx(4,i) + mrx(6,i)
            If (nparx>0) Then
              Read (nin,*) parx(1:nparx,i)
            End If
          End If
        End Do
      End If

      ifail = 0
      Call g13bjf(mr,nser,mt,para,npara,kfc,nev,nfv,xxy,ldxxy,kzef,rmsxy,mrx, &
        parx,ldparx,fva,fsd,sttf,isttf,nsttf,wa,iwa,mwa,imwa,ifail)

!     Display results
      Write (nout,99999) 'After processing', nev, ' sets of observations'
      Write (nout,99998) nsttf, ' values of the state set are derived'
      Write (nout,*)
      Write (nout,99997) sttf(1:nsttf)
      Write (nout,*)
      Write (nout,*) 'The residual mean square for the output'
      Write (nout,99996) 'series is also derived and its value is', &
        rmsxy(nser)
```

```
      Write (nout,*)
      Write (nout,*) 'The forecast values and their standard errors are'
      Write (nout,*)
      Write (nout,*) '   I       FVA       FSD'
      Write (nout,*)
      Write (nout,99995)(i,fva(i),fsd(i),i=1,nfv)
      Write (nout,*)
      Flush (nout)
      ifail = 0
      Call x04caf('General',' ',n,nser,xxy,ldxxy, &
        'The values of z(t) and n(t) are',ifail)
      Write (nout,99994) 'The first ', nis, &
        ' columns hold the z(t) and the last column the n(t)'

99999 Format (1X,A,I3,A)
99998 Format (1X,I3,A)
99997 Format (1X,6F10.4)
99996 Format (1X,A,F10.4)
99995 Format (1X,I4,F10.3,F10.4)
99994 Format (1X,A,I0,A)
    End Program g13bjfe
```

10.2 Program Data

```
G13BJF Example Program Data
 1   40    8    6    1                            :: KFC,NEV,NFV,NSER,KZEF
 1    0    0    0    0    1    4                  :: MR
0  0  0  1                                        :: Transfer fun. series 1 MT(:,1)
0  0  0  1                                        :: Transfer fun. series 2 MT(:,2)
0  0  0  1                                        :: Transfer fun. series 3 MT(:,3)
0  0  0  1                                        :: Transfer fun. series 4 MT(:,4)
1  0  1  3                                        :: Transfer fun. series 5 MT(:,5)
0.4950  0.2380 -0.3670  -3.8760  4.5160
2.4740  8.6290  0.6880 -82.8580                   :: End of PARA
  1.0     1.0     0.0     0.0     8.075 105.0
  1.0     0.0     1.0     0.0     7.819 119.0
  1.0     0.0     0.0     1.0     7.366 119.0
  1.0    -1.0    -1.0    -1.0     8.113 109.0
  2.0     1.0     0.0     0.0     7.380 117.0
  2.0     0.0     1.0     0.0     7.134 135.0
  2.0     0.0     0.0     1.0     7.222 126.0
  2.0    -1.0    -1.0    -1.0     7.768 112.0
  3.0     1.0     0.0     0.0     7.386 116.0
  3.0     0.0     1.0     0.0     6.965 122.0
  3.0     0.0     0.0     1.0     6.478 115.0
  3.0    -1.0    -1.0    -1.0     8.105 115.0
  4.0     1.0     0.0     0.0     8.060 122.0
  4.0     0.0     1.0     0.0     7.684 138.0
  4.0     0.0     0.0     1.0     7.580 135.0
  4.0    -1.0    -1.0    -1.0     7.093 125.0
  5.0     1.0     0.0     0.0     6.129 115.0
  5.0     0.0     1.0     0.0     6.026 108.0
  5.0     0.0     0.0     1.0     6.679 100.0
  5.0    -1.0    -1.0    -1.0     7.414  96.0
  6.0     1.0     0.0     0.0     7.112 107.0
  6.0     0.0     1.0     0.0     7.762 115.0
  6.0     0.0     0.0     1.0     7.645 123.0
  6.0    -1.0    -1.0    -1.0     8.639 122.0
  7.0     1.0     0.0     0.0     7.667 128.0
  7.0     0.0     1.0     0.0     8.080 136.0
  7.0     0.0     0.0     1.0     6.678 140.0
  7.0    -1.0    -1.0    -1.0     6.739 122.0
  8.0     1.0     0.0     0.0     5.569 102.0
  8.0     0.0     1.0     0.0     5.049 103.0
  8.0     0.0     0.0     1.0     5.642  89.0
  8.0    -1.0    -1.0    -1.0     6.808  77.0
  9.0     1.0     0.0     0.0     6.636  89.0
  9.0     0.0     1.0     0.0     8.241  94.0
  9.0     0.0     0.0     1.0     7.968 104.0
  9.0    -1.0    -1.0    -1.0     8.044 108.0
```

```
 10.0     1.0     0.0     0.0     7.791 119.0
 10.0     0.0     1.0     0.0     7.024 126.0
 10.0     0.0     0.0     1.0     6.102 119.0
 10.0    -1.0    -1.0    -1.0     6.053 103.0 :: XXY (observed values)
 11.0     1.0     0.0     0.0     5.941
 11.0     0.0     1.0     0.0     5.386
 11.0     0.0     0.0     1.0     5.811
 11.0    -1.0    -1.0    -1.0     6.716
 12.0     1.0     0.0     0.0     6.923
 12.0     0.0     1.0     0.0     6.939
 12.0     0.0     0.0     1.0     6.705
 12.0    -1.0    -1.0    -1.0     6.914        :: End of XXY (future values)
  0.0     0.0     0.0     0.0     0.1720       :: End of RMSXY
  2  0  2  0  1  1  4                          :: Orders for series 5, MRX(:,5)
1.6743  -0.9505  1.4605  -0.4862  0.8993       :: Params for series 5, PARX(:,5)
```

10.3 Program Results

```
 G13BJF Example Program Results

 After processing 40 sets of observations
   6 values of the state set are derived

     6.0530  193.8741    2.0790   -2.8580   -3.5906   -2.5203

 The residual mean square for the output
 series is also derived and its value is   20.7599

 The forecast values and their standard errors are

    I       FVA       FSD

    1    93.398    4.5563
    2    96.958    6.2172
    3    86.046    7.0933
    4    77.589    7.3489
    5    82.139    7.3941
    6    96.276    7.5823
    7    98.345    8.1445
    8    93.577    8.8536

 The values of z(t) and n(t) are
              1          2          3          4          5          6
  1     -0.3391    -3.8886     0.0000     0.0000   188.6028   -79.3751
  2     -0.3391    -0.0000     4.5139     0.0000   199.4379   -84.6127
  3     -0.3391    -0.0000     0.0000     2.4789   204.6834   -87.8232
  4     -0.3391     3.8886    -4.5139    -2.4789   204.3834   -91.9402
  5     -0.6782    -3.8886     0.0000     0.0000   210.6229   -89.0560
  6     -0.6782    -0.0000     4.5139     0.0000   208.5905   -77.4262
  7     -0.6782    -0.0000     0.0000     2.4789   205.0696   -80.8703
  8     -0.6782     3.8886    -4.5139    -2.4789   203.4065   -87.6242
  9     -1.0173    -3.8886     0.0000     0.0000   206.9738   -86.0678
 10     -1.0173    -0.0000     4.5139     0.0000   206.1317   -87.6283
 11     -1.0173    -0.0000     0.0000     2.4789   201.9196   -88.3812
 12     -1.0173     3.8886    -4.5139    -2.4789   194.8194   -75.6979
 13     -1.3564    -3.8886     0.0000     0.0000   203.9738   -76.7287
 14     -1.3564    -0.0000     4.5139     0.0000   209.8837   -75.0412
 15     -1.3564    -0.0000     0.0000     2.4789   210.7052   -76.8277
 16     -1.3564     3.8886    -4.5139    -2.4789   210.3730   -80.9125
 17     -1.6955    -3.8886     0.0000     0.0000   205.9421   -85.3580
 18     -1.6955    -0.0000     4.5139     0.0000   194.5753   -89.3937
 19     -1.6955    -0.0000     0.0000     2.4789   185.8662   -86.6496
 20     -1.6955     3.8886    -4.5139    -2.4789   185.5090   -84.7094
 21     -2.0346    -3.8886     0.0000     0.0000   191.6056   -78.6824
 22     -2.0346    -0.0000     4.5139     0.0000   193.1941   -80.6734
 23     -2.0346    -0.0000     0.0000     2.4789   199.8958   -77.3402
 24     -2.0346     3.8886    -4.5139    -2.4789   203.4970   -76.3583
 25     -2.3737    -3.8886     0.0000     0.0000   214.5519   -80.2896
 26     -2.3737    -0.0000     4.5139     0.0000   213.7702   -79.9104
 27     -2.3737    -0.0000     0.0000     2.4789   216.7963   -76.9015
```

```
 28     -2.3737     3.8886    -4.5139    -2.4789   206.7803   -79.3024
 29     -2.7128    -3.8886     0.0000     0.0000   200.4157   -91.8142
 30     -2.7128    -0.0000     4.5139     0.0000   185.9409   -84.7420
 31     -2.7128    -0.0000     0.0000     2.4789   171.4951   -82.2613
 32     -2.7128     3.8886    -4.5139    -2.4789   166.6735   -83.8565
 33     -3.0519    -3.8886     0.0000     0.0000   173.4176   -77.4771
 34     -3.0519    -0.0000     4.5139     0.0000   176.5733   -84.0353
 35     -3.0519    -0.0000     0.0000     2.4789   192.5940   -88.0211
 36     -3.0519     3.8886    -4.5139    -2.4789   201.2606   -87.1045
 37     -3.3910    -3.8886     0.0000     0.0000   207.8790   -81.5993
 38     -3.3910    -0.0000     4.5139     0.0000   210.2493   -85.3721
 39     -3.3910    -0.0000     0.0000     2.4789   205.2616   -85.3495
 40     -3.3910     3.8886    -4.5139    -2.4789   193.8741   -84.3790
 41     -3.7301    -3.8886     0.0000     0.0000   185.6167   -84.6003
 42     -3.7301     0.0000     4.5139     0.0000   178.9692   -82.7953
 43     -3.7301     0.0000     0.0000     2.4789   169.6066   -82.3091
 44     -3.7301     3.8886    -4.5139    -2.4789   166.8325   -82.4095
 45     -4.0692    -3.8886     0.0000     0.0000   172.7331   -82.6360
 46     -4.0692     0.0000     4.5139     0.0000   178.5789   -82.7481
 47     -4.0692     0.0000     0.0000     2.4789   182.7389   -82.8036
 48     -4.0692     3.8886    -4.5139    -2.4789   183.5818   -82.8311
 The first 5 columns hold the z(t) and the last column the n(t)
```