NAG Library Routine Document

F08CUF (ZUNMQL)

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

F08CUF (ZUNMQL) multiplies a general complex m by n matrix C by the complex unitary matrix Q from a QL factorization computed by F08CSF (ZGEQLF).

2 Specification

```
SUBROUTINE FO8CUF (SIDE, TRANS, M, N, K, A, LDA, TAU, C, LDC, WORK, LWORK, INFO)

INTEGER M, N, K, LDA, LDC, LWORK, INFO
COMPLEX (KIND=nag_wp) A(LDA,*), TAU(*), C(LDC,*), WORK(max(1,LWORK))
CHARACTER(1) SIDE, TRANS
```

The routine may be called by its LAPACK name *zunmql*.

3 Description

F08CUF (ZUNMQL) is intended to be used following a call to F08CSF (ZGEQLF), which performs a QL factorization of a complex matrix A and represents the unitary matrix Q as a product of elementary reflectors.

This routine may be used to form one of the matrix products

$$QC$$
, $Q^{H}C$, CQ , CQ^{H} ,

overwriting the result on C, which may be any complex rectangular m by n matrix.

A common application of this routine is in solving linear least squares problems, as described in the F08 Chapter Introduction, and illustrated in Section 10 in F08CSF (ZGEQLF).

4 References

Anderson E, Bai Z, Bischof C, Blackford S, Demmel J, Dongarra J J, Du Croz J J, Greenbaum A, Hammarling S, McKenney A and Sorensen D (1999) *LAPACK Users' Guide* (3rd Edition) SIAM, Philadelphia http://www.netlib.org/lapack/lug

5 Parameters

SIDE = 'R'

1: SIDE – CHARACTER(1) Input $On \ entry: \ \text{indicates how} \ Q \ \text{or} \ Q^{\text{H}} \ \text{is to be applied to} \ C.$ SIDE = 'L' $Q \ \text{or} \ Q^{\text{H}} \ \text{is applied to} \ C \ \text{from the left.}$

Q or Q^{H} is applied to C from the right.

Constraint: SIDE = 'L' or 'R'.

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2: TRANS - CHARACTER(1)

Input

On entry: indicates whether Q or Q^{H} is to be applied to C.

TRANS = 'N'

Q is applied to C.

TRANS = 'C'

 $Q^{\rm H}$ is applied to C.

Constraint: TRANS = 'N' or 'C'.

3: M – INTEGER

Input

On entry: m, the number of rows of the matrix C.

Constraint: M > 0.

4: N – INTEGER

Input

On entry: n, the number of columns of the matrix C.

Constraint: N > 0.

5: K – INTEGER

Input

On entry: k, the number of elementary reflectors whose product defines the matrix Q.

Constraints:

if SIDE = 'L',
$$M \ge K \ge 0$$
; if SIDE = 'R', $N \ge K \ge 0$.

6: A(LDA,*) - COMPLEX (KIND=nag wp) array

Input

Note: the second dimension of the array A must be at least max(1, K).

On entry: details of the vectors which define the elementary reflectors, as returned by F08CSF (ZGEQLF).

On exit: is modified by F08CUF (ZUNMQL) but restored on exit.

7: LDA – INTEGER

Input

On entry: the first dimension of the array A as declared in the (sub)program from which F08CUF (ZUNMQL) is called.

Constraints:

if SIDE = 'L', LDA
$$\geq \max(1, M)$$
; if SIDE = 'R', LDA $\geq \max(1, N)$.

8: TAU(*) – COMPLEX (KIND=nag_wp) array

Input

Note: the dimension of the array TAU must be at least max(1, K).

On entry: further details of the elementary reflectors, as returned by F08CSF (ZGEQLF).

9: C(LDC,*) - COMPLEX (KIND=nag wp) array

Input/Output

Note: the second dimension of the array C must be at least max(1, N).

On entry: the m by n matrix C.

On exit: C is overwritten by QC or $Q^{H}C$ or CQ or CQ^{H} as specified by SIDE and TRANS.

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10: LDC - INTEGER

Input

On entry: the first dimension of the array C as declared in the (sub)program from which F08CUF (ZUNMQL) is called.

Constraint: LDC $\geq \max(1, M)$.

11: WORK(max(1,LWORK)) - COMPLEX (KIND=nag wp) array

Workspace

On exit: if INFO = 0, the real part of WORK(1) contains the minimum value of LWORK required for optimal performance.

12: LWORK – INTEGER

Input

On entry: the dimension of the array WORK as declared in the (sub)program from which F08CUF (ZUNMQL) is called.

If LWORK = -1, a workspace query is assumed; the routine only calculates the optimal size of the WORK array, returns this value as the first entry of the WORK array, and no error message related to LWORK is issued.

Suggested value: for optimal performance, LWORK \geq N \times nb if SIDE = 'L' and at least M \times nb if SIDE = 'R', where nb is the optimal **block size**.

Constraints:

```
if SIDE = 'L', LWORK \geq max(1, N) or LWORK = -1; if SIDE = 'R', LWORK \geq max(1, M) or LWORK = -1.
```

13: INFO - INTEGER

Output

On exit: INFO = 0 unless the routine detects an error (see Section 6).

6 Error Indicators and Warnings

INFO < 0

If INFO = -i, argument i had an illegal value. An explanatory message is output, and execution of the program is terminated.

7 Accuracy

The computed result differs from the exact result by a matrix E such that

$$||E||_2 = O\epsilon ||C||_2$$

where ϵ is the *machine precision*.

8 Parallelism and Performance

F08CUF (ZUNMQL) is not threaded by NAG in any implementation.

F08CUF (ZUNMQL) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this routine. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

The total number of floating-point operations is approximately 8nk(2m-k) if SIDE = 'L' and 8mk(2n-k) if SIDE = 'R'.

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The real analogue of this routine is F08CGF (DORMQL).

10 Example

See Section 10 in F08CSF (ZGEQLF).

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