

## NAG Library Routine Document

### F08BKF (DORMRZ)

**Note:** before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

#### 1 Purpose

F08BKF (DORMRZ) multiplies a general real  $m$  by  $n$  matrix  $C$  by the real orthogonal matrix  $Z$  from an  $RZ$  factorization computed by F08BHF (DTZRZF).

#### 2 Specification

```
SUBROUTINE F08BKF (SIDE, TRANS, M, N, K, L, A, LDA, TAU, C, LDC, WORK, &
                  LWORK, INFO)
INTEGER          M, N, K, L, LDA, LDC, LWORK, INFO
REAL (KIND=nag_wp) A(LDA,*), TAU(*), C(LDC,*), WORK(max(1,LWORK))
CHARACTER(1)    SIDE, TRANS
```

The routine may be called by its LAPACK name *dormrz*.

#### 3 Description

F08BKF (DORMRZ) is intended to be used following a call to F08BHF (DTZRZF), which performs an  $RZ$  factorization of a real upper trapezoidal matrix  $A$  and represents the orthogonal matrix  $Z$  as a product of elementary reflectors.

This routine may be used to form one of the matrix products

$$ZC, \quad Z^T C, \quad CZ, \quad CZ^T,$$

overwriting the result on  $C$ , which may be any real rectangular  $m$  by  $n$  matrix.

#### 4 References

Anderson E, Bai Z, Bischof C, Blackford S, Demmel J, Dongarra J J, Du Croz J J, Greenbaum A, Hammarling S, McKenney A and Sorensen D (1999) *LAPACK Users' Guide* (3rd Edition) SIAM, Philadelphia <http://www.netlib.org/lapack/lug>

#### 5 Parameters

1: SIDE – CHARACTER(1) *Input*

*On entry:* indicates how  $Z$  or  $Z^T$  is to be applied to  $C$ .

SIDE = 'L'

$Z$  or  $Z^T$  is applied to  $C$  from the left.

SIDE = 'R'

$Z$  or  $Z^T$  is applied to  $C$  from the right.

*Constraint:* SIDE = 'L' or 'R'.

2: TRANS – CHARACTER(1) *Input*

*On entry:* indicates whether  $Z$  or  $Z^T$  is to be applied to  $C$ .

TRANS = 'N'

$Z$  is applied to  $C$ .

- TRANS = 'T'  
 $Z^T$  is applied to  $C$ .  
 Constraint: TRANS = 'N' or 'T'.
- 3: M – INTEGER *Input*  
*On entry:*  $m$ , the number of rows of the matrix  $C$ .  
 Constraint:  $M \geq 0$ .
- 4: N – INTEGER *Input*  
*On entry:*  $n$ , the number of columns of the matrix  $C$ .  
 Constraint:  $N \geq 0$ .
- 5: K – INTEGER *Input*  
*On entry:*  $k$ , the number of elementary reflectors whose product defines the matrix  $Z$ .  
 Constraints:  
     if SIDE = 'L',  $M \geq K \geq 0$ ;  
     if SIDE = 'R',  $N \geq K \geq 0$ .
- 6: L – INTEGER *Input*  
*On entry:*  $l$ , the number of columns of the matrix  $A$  containing the meaningful part of the Householder reflectors.  
 Constraints:  
     if SIDE = 'L',  $M \geq L \geq 0$ ;  
     if SIDE = 'R',  $N \geq L \geq 0$ .
- 7: A(LDA,\*) – REAL (KIND=nag\_wp) array *Input*  
**Note:** the second dimension of the array  $A$  must be at least  $\max(1, M)$  if SIDE = 'L' and at least  $\max(1, N)$  if SIDE = 'R'.  
*On entry:* the  $i$ th row of  $A$  must contain the vector which defines the elementary reflector  $H_i$ , for  $i = 1, 2, \dots, k$ , as returned by F08BHF (DTZRZF).
- 8: LDA – INTEGER *Input*  
*On entry:* the first dimension of the array  $A$  as declared in the (sub)program from which F08BKF (DORMRZ) is called.  
 Constraint:  $LDA \geq \max(1, K)$ .
- 9: TAU(\*) – REAL (KIND=nag\_wp) array *Input*  
**Note:** the dimension of the array TAU must be at least  $\max(1, K)$ .  
*On entry:* TAU( $i$ ) must contain the scalar factor of the elementary reflector  $H_i$ , as returned by F08BHF (DTZRZF).
- 10: C(LDC,\*) – REAL (KIND=nag\_wp) array *Input/Output*  
**Note:** the second dimension of the array  $C$  must be at least  $\max(1, N)$ .  
*On entry:* the  $m$  by  $n$  matrix  $C$ .  
*On exit:*  $C$  is overwritten by  $ZC$  or  $Z^T C$  or  $CZ$  or  $Z^T C$  as specified by SIDE and TRANS.

- 11: LDC – INTEGER *Input*  
*On entry:* the first dimension of the array C as declared in the (sub)program from which F08BKF (DORMRZ) is called.  
*Constraint:*  $LDC \geq \max(1, M)$ .
- 12: WORK(max(1, LWORK)) – REAL (KIND=nag\_wp) array *Workspace*  
*On exit:* if INFO = 0, WORK(1) contains the minimum value of LWORK required for optimal performance.
- 13: LWORK – INTEGER *Input*  
*On entry:* the dimension of the array WORK as declared in the (sub)program from which F08BKF (DORMRZ) is called.  
 If LWORK = -1, a workspace query is assumed; the routine only calculates the optimal size of the WORK array, returns this value as the first entry of the WORK array, and no error message related to LWORK is issued.  
*Suggested value:* for optimal performance,  $LWORK \geq N \times nb$  if SIDE = 'L' and at least  $M \times nb$  if SIDE = 'R', where *nb* is the optimal **block size**.  
*Constraints:*  
     if SIDE = 'L',  $LWORK \geq \max(1, N)$  or LWORK = -1;  
     if SIDE = 'R',  $LWORK \geq \max(1, M)$  or LWORK = -1.
- 14: INFO – INTEGER *Output*  
*On exit:* INFO = 0 unless the routine detects an error (see Section 6).

## 6 Error Indicators and Warnings

INFO < 0

If INFO = -*i*, argument *i* had an illegal value. An explanatory message is output, and execution of the program is terminated.

## 7 Accuracy

The computed result differs from the exact result by a matrix *E* such that

$$\|E\|_2 = O\epsilon \|C\|_2$$

where  $\epsilon$  is the *machine precision*.

## 8 Parallelism and Performance

F08BKF (DORMRZ) is not threaded by NAG in any implementation.

F08BKF (DORMRZ) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this routine. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

## 9 Further Comments

The total number of floating-point operations is approximately *4nlk* if SIDE = 'L' and *4mlk* if SIDE = 'R'.

The complex analogue of this routine is F08BXF (ZUNMRZ).

## **10 Example**

See Section 10 in F08BHF (DTZRZF).

---