

NAG Library Routine Document

G05SCF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

1 Purpose

G05SCF generates a vector of pseudorandom numbers from a Cauchy distribution with median a and semi-interquartile range b .

2 Specification

```
SUBROUTINE G05SCF (N, XMED, SEMIQR, STATE, X, IFAIL)
```

```
INTEGER          N, STATE(*), IFAIL
REAL (KIND=nag_wp) XMED, SEMIQR, X(N)
```

3 Description

The distribution has PDF (probability density function)

$$f(x) = \frac{1}{\pi b \left(1 + \left(\frac{x-a}{b} \right)^2 \right)}$$

G05SCF returns the value

$$a + b \frac{2y_1 - 1}{y_2},$$

where y_1 and y_2 are a pair of consecutive pseudorandom numbers from a uniform distribution over $(0, 1)$, such that

$$(2y_1 - 1)^2 + y_2^2 \leq 1.$$

One of the initialization routines G05KFF (for a repeatable sequence if computed sequentially) or G05KGF (for a non-repeatable sequence) must be called prior to the first call to G05SCF.

4 References

Kendall M G and Stuart A (1969) *The Advanced Theory of Statistics (Volume 1)* (3rd Edition) Griffin

Knuth D E (1981) *The Art of Computer Programming (Volume 2)* (2nd Edition) Addison-Wesley

5 Parameters

1: N – INTEGER *Input*

On entry: n , the number of pseudorandom numbers to be generated.

Constraint: $N \geq 0$.

2: XMED – REAL (KIND=nag_wp) *Input*

On entry: a , the median of the distribution.

- 3: SEMIQR – REAL (KIND=nag_wp) *Input*
On entry: b , the semi-interquartile range of the distribution.
Constraint: SEMIQR \geq 0.0.
- 4: STATE(*) – INTEGER array *Communication Array*
Note: the actual argument supplied must be the array STATE supplied to the initialization routines G05KFF or G05KGF.
On entry: contains information on the selected base generator and its current state.
On exit: contains updated information on the state of the generator.
- 5: X(N) – REAL (KIND=nag_wp) array *Output*
On exit: the n pseudorandom numbers from the specified Cauchy distribution.
- 6: IFAIL – INTEGER *Input/Output*
On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Section 3.3 in the Essential Introduction for details.
 For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this parameter, the recommended value is 0. **When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.**
On exit: IFAIL = 0 unless the routine detects an error or a warning has been flagged (see Section 6).

6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1 , explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

On entry, $N < 0$.

IFAIL = 3

On entry, SEMIQR < 0.0 .

IFAIL = 4

On entry, STATE vector was not initialized or has been corrupted.

7 Accuracy

Not applicable.

8 Further Comments

None.

9 Example

This example prints the first five pseudorandom real numbers from a Cauchy distribution with median 1.0 and semi-interquartile range 2.0, generated by a single call to G05SCF, after initialization by G05KFF.

9.1 Program Text

```

Program g05scfe

!      G05SCF Example Program Text

!      Mark 24 Release. NAG Copyright 2012.

!      .. Use Statements ..
Use nag_library, Only: g05kff, g05scf, nag_wp
!      .. Implicit None Statement ..
Implicit None
!      .. Parameters ..
Integer, Parameter          :: lseed = 1, nin = 5, nout = 6
!      .. Local Scalars ..
Real (Kind=nag_wp)         :: semigr, xmed
Integer                     :: genid, ifail, lstate, n, subid
!      .. Local Arrays ..
Real (Kind=nag_wp), Allocatable :: x(:)
Integer                     :: seed(lseed)
Integer, Allocatable        :: state(:)
!      .. Executable Statements ..
Write (nout,*) 'G05SCF Example Program Results'
Write (nout,*)

!      Skip heading in data file
Read (nin,*)

!      Read in the base generator information and seed
Read (nin,*) genid, subid, seed(1)

!      Initial call to initialiser to get size of STATE array
lstate = 0
Allocate (state(lstate))
ifail = 0
Call g05kff(genid,subid,seed,lseed,state,lstate,ifail)

!      Reallocate STATE
Deallocate (state)
Allocate (state(lstate))

!      Initialize the generator to a repeatable sequence
ifail = 0
Call g05kff(genid,subid,seed,lseed,state,lstate,ifail)

!      Read in sample size
Read (nin,*) n

Allocate (x(n))

!      Read in the distribution parameters
Read (nin,*) xmed, semigr

!      Generate the variates
ifail = 0
Call g05scf(n,xmed,semigr,state,x,ifail)

!      Display the variates
Write (nout,99999) x(1:n)

99999 Format (1X,F10.4)
End Program g05scfe

```

9.2 Program Data

```

G05SCF Example Program Data
1 1 1762543      :: GENID,SUBID,SEED(1)
5              :: N
1.0 2.0        :: XMED,SEMIQR

```

9.3 Program Results

G05SCF Example Program Results

```
6.1229
2.2328
-2.2118
0.4118
0.9892
```
