NAG Library Routine Document D02OZF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

D02QZF interpolates components of the solution of a non-stiff system of first-order differential equations from information provided by the integrator routines D02QFF or D02QGF.

2 Specification

```
SUBROUTINE DO2QZF (NEQF, TWANT, NWANT, YWANT, YPWANT, RWORK, LRWORK, IWORK, LIWORK, IFAIL)

INTEGER NEQF, NWANT, LRWORK, IWORK(LIWORK), LIWORK, IFAIL
REAL (KIND=nag_wp) TWANT, YWANT(NWANT), YPWANT(NWANT), RWORK(LRWORK)
```

3 Description

D02QZF evaluates the first NWANT components of the solution of a non-stiff system of first-order ordinary differential equations at any point using the method of Watts and Shampine (1986) and information generated by D02QFF or D02QGF. D02QZF should not normally be used to extrapolate outside the current range of the values produced by the integration routine.

4 References

Watts H A and Shampine L F (1986) Smoother interpolants for Adams codes SIAM J. Sci. Statist. Comput. 7 334–345

5 Parameters

1: NEQF - INTEGER

Input

On entry: the number of first-order ordinary differential equations being solved by the integration routine. It must contain the same value as the parameter NEQF in a prior call to the setup routine D02QWF.

2: TWANT – REAL (KIND=nag wp)

Input

On entry: the point at which components of the solution and derivative are to be evaluated. TWANT should not normally be an extrapolation point, that is TWANT should satisfy

```
told \leq TWANT \leq T,
```

or if integration is proceeding in the negative direction

```
told > TWANT > T,
```

where told is the previous integration point and is, to within rounding, TCURR – HLAST (see D02QXF). Extrapolation is permitted but not recommended and IFAIL = 2 is returned whenever extrapolation is attempted.

3: NWANT – INTEGER

Input

On entry: the number of components of the solution and derivative whose values at TWANT are required. The first NWANT components are evaluated.

Constraint: $1 \leq NWANT \leq NEQF$.

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4: YWANT(NWANT) - REAL (KIND=nag_wp) array

Output

On exit: the calculated value of the ith component of the solution at TWANT, for i = 1, 2, ..., NWANT.

5: YPWANT(NWANT) - REAL (KIND=nag wp) array

Output

On exit: the calculated value of the ith component of the derivative at TWANT, for i = 1, 2, ..., NWANT.

6: RWORK(LRWORK) – REAL (KIND=nag wp) array

Communication Array

On entry: this **must** be the same parameter RWORK as supplied to D02QWF and to D02QFF or D02QGF. It is used to pass information from these routines to D02QZF. Therefore its contents **must not** be changed before a call to D02QZF.

7: LRWORK – INTEGER

Input

On entry: the dimension of the array RWORK as declared in the (sub)program from which D02QZF is called.

This must be the same parameter LRWORK as supplied to D02QWF.

8: IWORK(LIWORK) – INTEGER array

Communication Array

On entry: this **must** be the same parameter IWORK as supplied to D02QWF and to D02QFF or D02QGF. It is used to pass information from these routines to D02QZF. Therefore its contents **must not** be changed before a call to D02QZF.

9: LIWORK – INTEGER

Input

On entry: the dimension of the array IWORK as declared in the (sub)program from which D02QZF is called.

This must be the same parameter LIWORK as supplied to D02QWF.

10: IFAIL - INTEGER

Input/Output

On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Section 3.3 in the Essential Introduction for details.

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this parameter, the recommended value is 0. When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.

On exit: IFAIL = 0 unless the routine detects an error or a warning has been flagged (see Section 6).

6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

An integration routine (D02QFF or D02QGF) has not been called, no integration steps have been taken since the last call to D02QWF with STATEF = 'S', one or more of the parameters LRWORK, LIWORK and NEQF does not match the same parameter supplied to D02QWF, or NWANT does not satisfy $1 \le NWANT \le NEQF$.

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IFAIL = 2

D02QZF has been called for extrapolation. The values of the solution and its derivative at TWANT have been calculated and placed in YWANT and YPWANT before returning with this warning (see Section 7).

These error exits may be caused by overwriting elements of RWORK and IWORK.

7 Accuracy

The error in interpolation is of a similar order to the error arising from the integration. The same order of accuracy can be expected when extrapolating using D02QZF. However, the actual error in extrapolation will, in general, be much larger than for interpolation.

8 Further Comments

When interpolation for only a few components is required then it is more efficient to order the components of interest so that they are numbered first.

9 Example

This example solves the equation

$$y'' = -y$$
, $y(0) = 0$, $y'(0) = 1$

reposed as

$$y_1' = y_2$$

$$y_2' = -y_1$$

over the range $[0, \pi/2]$ with initial conditions $y_1 = 0$ and $y_2 = 1$ using vector error control (VECTOL = .TRUE.) and D02QFF in one-step mode (ONESTP = .TRUE.). D02QZF is used to provide solution values at intervals of $\pi/16$.

9.1 Program Text

```
D02QZF Example Program Text
    Mark 24 Release. NAG Copyright 2012.
    Module d02qzfe_mod
!
      DO2QZF Example Program Module:
             Parameters and User-defined Routines
1
1
      .. Use Statements ..
      Use nag_library, Only: nag_wp
!
      .. Implicit None Statement ..
      Implicit None
      .. Parameters ..
      Integer, Parameter
                                             :: neqf = 2, neqg = 0, nin = 5,
                                                nout = 6
                                             :: latol = neqf
      Integer, Parameter
                                             :: liwork = 21 + 4*neqg
      Integer, Parameter
      Integer, Parameter
                                             :: lrtol = neqf
                                             :: lrwork = 23 + 23*neqf + 14*neqq
      Integer, Parameter
    Contains
      Subroutine fcn(neqf,x,y,f)
        .. Scalar Arguments ..
!
        Real (Kind=nag_wp), Intent (In)
                                               :: X
        Integer, Intent (In)
                                               :: neqf
        .. Array Arguments ..
        Real (Kind=nag_wp), Intent (Out)
Real (Kind=nag_wp), Intent (In)
                                              :: f(neqf)
                                              :: y(neqf)
        .. Executable Statements ..
        f(1) = y(2)
```

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```
f(2) = -y(1)
        Return
     End Subroutine fcn
    End Module d02qzfe_mod
    Program d02qzfe
     D02QZF Example Main Program
!
      .. Use Statements ..
      Use nag_library, Only: d02qff, d02qfz, d02qwf, d02qzf, nag_wp
     Use d02qzfe_mod, Only: fcn, latol, liwork, lrtol, lrwork, neqf, neqg,
                             nin, nout
      .. Implicit None Statement ..
!
     Implicit None
      .. Local Scalars ..
                                           :: hmax, t, tcrit, tinc, tout,
     Real (Kind=nag_wp)
                                               tstart, twant
                                            :: ifail, maxstp, nwant
      Integer
     Logical
                                            :: alterg, crit, onestp, root,
                                              sophst, vectol
     Character (1)
                                            :: statef
!
      .. Local Arrays ..
     Real (Kind=nag_wp), Allocatable
                                           :: atol(:), rtol(:), rwork(:),
                                              y(:), ypwant(:), ywant(:)
     Integer, Allocatable
                                            :: iwork(:)
      .. Executable Statements ..
     Write (nout,*) 'D02QZF Example Program Results'
1
     Skip heading in data file
      Read (nin,*)
     Allocate (atol(latol),rtol(lrtol),rwork(lrwork),y(neqf),ypwant(neqf), &
       ywant(neqf),iwork(liwork))
     Read (nin,*) hmax, tstart
     Read (nin,*) tcrit, tinc
     Read (nin,*) statef
     Read (nin,*) vectol, onestp, crit
     Read (nin,*) maxstp
     Read (nin,*) rtol(1:neqf)
     Read (nin,*) atol(1:neqf)
     Read (nin,*) y(1:neqf)
     tout = tcrit
     t = tstart
      twant = tstart + tinc
     nwant = neqf
!
     Set up integration.
      ifail = 0
      Call d02qwf(statef,neqf,vectol,atol,latol,rtol,lrtol,onestp,crit,tcrit, &
       hmax,maxstp,neqg,alterg,sophst,rwork,lrwork,iwork,liwork,ifail)
     Write (nout,*)
      Write (nout,*) ' T
                                  Y(1)
                                          Y(2)'
     Write (nout, 99999) t, y(1), y(2)
integ: Do While (t<tout)</pre>
        ifail = -1
        Call d02qff(fcn,neqf,t,y,tout,d02qfz,neqg,root,rwork,lrwork,iwork, &
          liwork, ifail)
        If (ifail/=0) Exit integ
!
        Interpolate at wanted time values up to time = t.
        Do While (twant<=t)</pre>
          ifail = 0
          Call d02gzf(negf,twant,nwant,ywant,ywant,rwork,lrwork,iwork,liwork, &
           ifail)
          Write (nout, 99999) twant, ywant(1), ywant(2)
          twant = twant + tinc
```

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```
End Do
End Do integ
99999 Format (1X,F7.4,2X,2(F7.4,2X))
End Program dO2qzfe
```

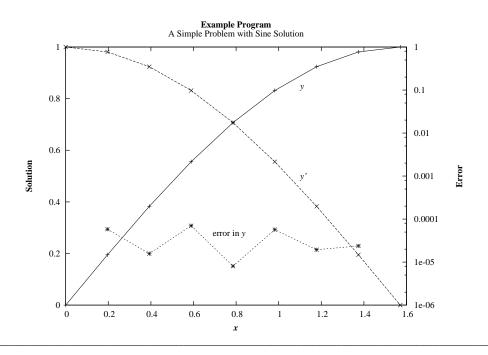
9.2 Program Data

```
D02QZF Example Program Data
2.0 0.0 : hmax, tstart
1.57079632679489661923 1.96349540849362077403E-1 : tcrit, tinc
S : statef
.TRUE. .TRUE. .TRUE.
500 : maxstp
1.0E-4 1.0E-4 : rtol
1.0E-8 1.0E-8 1.0E-8 : atol
0.0 1.0 : y
```

9.3 Program Results

D02QZF Example Program Results

T	Y(1)	Y(2)
0.0000	0.0000	1.0000
0.1963	0.1951	0.9808
0.3927	0.3827	0.9239
0.5890	0.5556	0.8315
0.7854	0.7071	0.7071
0.9817	0.8315	0.5556
1.1781	0.9239	0.3827
1.3744	0.9808	0.1951
1.5708	1.0000	-0.0000



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