## F11YQFP

## NAG Parallel Library Routine Document

Note: before using this routine, please read the Users' Note for your implementation to check for implementation-dependent details. You are advised to enclose any calls to NAG Parallel Library routines between calls to Z01AAFP and Z01ABFP.

## 1 Description

F11YQFP permutes the local part of a complex dense vector $x$ of length $n$, distributed conformally to a sparse matrix $A$ (see Section 2.5 of the F11 Chapter Introduction), from matrix-based order into distribution-based order (see Section 2.6.2 of the F11 Chapter Introduction).

One of the routines F11ZBFP or F11ZPFP must be called prior to F11YQFP to set up auxiliary information about the sparse matrix $A$ in the array IAINFO.

## 2 Specification

```
SUBROUTINE F11YQFP(ICNTXT, N, XL, XD, IAINFO, IFAIL)
COMPLEX*16 XL(*), XD(*)
INTEGER ICNTXT, N, IAINFO(*), IFAIL
```


## 3 Usage

### 3.1 Definitions

The following definitions are used in describing the data distribution within this document:
$m_{l} \quad-\quad$ the number of vector elements stored on the calling processor ( $m_{l}=\operatorname{IAINFO}(3)$, see IAINFO).

### 3.2 Global and Local Arguments

Global input arguments: N, IFAIL
Global output arguments: IFAIL
The remaining arguments are local.

### 3.3 Distribution Strategy

The vector $x$ must be distributed conformally to the sparse matrix $A$, i.e., $x$ must be distributed across the Library Grid in the same way as each of the columns of the matrix $A$ is. This data distribution is described in more detail in Section 2.5 of the F11 Chapter Introduction.

### 3.4 Related Routines

Some Library routines can be used to generate or distribute real dense vectors conformally to a given real or complex sparse matrix.

Real vector generation: F01YTFP
Real vector scatter:
F01XTFP

### 3.5 Requisites

The sparse matrix $A$ must have been preprocessed to set up the auxiliary information vector IAINFO by F11ZBFP (or F11ZPFP if $A$ is complex).

## 4 Arguments

1: ICNTXT - INTEGER
Local Input
On entry: the Library context, usually returned by a call to the Library Grid initialisation routine Z01AAFP.

Note: the value of ICNTXT must not be changed.
2: N - INTEGER
Global Input
On entry: $n$, the order of the matrix $A$. It must contain the same value as the parameter N used in a prior call to F11ZBFP or F11ZPFP in which the array IAINFO was initialised.
Constraint: $\mathrm{N} \geq 1$.
3: $\mathrm{XL}(*)$ - COMPLEX*16 array Local Input
Note: the dimension of the array XL must be at least $\max \left(1, m_{l}\right)$.
On entry: the local part of the vector $x$ in matrix-based order.
4: $\quad \mathrm{XD}(*)$ - COMPLEX*16 array
Local Output
Note: the dimension of the array XD must be at least $\max \left(1, m_{l}\right)$.
On exit: the local part of the vector $x$ in distribution-based order.
5: $\operatorname{IAINFO}(*)$ - INTEGER array
Note: the dimension of the array IAINFO must be at least max(200,IAINFO(2)).
On entry: the first IAINFO(2) elements of IAINFO contain auxiliary information about the matrix A. The array IAINFO must be initialised by a prior call to F11ZBFP or F11ZPFP. The first IAINFO(2) elements of IAINFO must not be changed between successive calls to library routines involving the matrix $A$.

Note: on exit from F11ZBFP or F11ZPFP, the element $\operatorname{IAINFO}(3)$ contains $m_{l}$, the number of rows of the matrix assigned to the calling processor.

6: IFAIL - INTEGER
Global Input/Global Output
The NAG Parallel Library provides a mechanism, via the routine Z02EAFP, to reduce the amount of parameter validation performed by this routine. For a full description refer to the Z02 Chapter Introduction.
On entry: IFAIL must be set to $0,-1$ or 1 . For users not familiar with this argument (described in the Essential Introduction) the recommended values are:

IFAIL $=0$, if multigridding is not employed;
IFAIL $=-1$, if multigridding is employed.
On exit: IFAIL $=0$ (or -9999 if reduced error checking is enabled) unless the routine detects an error (see Section 5).

## 5 Errors and Warnings

If on entry IFAIL $=0$ or -1 , explanatory error messages are output from the root processor (or processor $\{0,0\}$ when the root processor is not available) on the current error message unit (as defined by X04AAF).

### 5.1 Full Error Checking Mode Only

IFAIL $=-2000$
The routine has been called with an invalid value of ICNTXT on one or more processors.
IFAIL $=-1000$
The logical processor grid and library mechanism (Library Grid) have not been correctly defined, see Z01AAFP.

IFAIL $=-i$
On entry, the $i$ th argument was invalid. This error occured either because a global argument did not have the same value on all logical processors, or because its value on one or more processors was incorrect. An explanatory message distinguishes between these two cases.

IFAIL $=1$
IAINFO was not initialised by a prior call to F11ZBFP or F11ZPFP.

## IFAIL $=2$

On entry, the data stored in the arguments N and IAINFO is inconsistent. This indicates that, after the array IAINFO was set up by a call to F11ZBFP or F11ZPFP, at least one of these arguments was changed between successive calls to library routines.

## 6 Further Comments

The routine performs all operations on each logical processor independently.

## 7 References

None.

## 8 Example

This example generates a vector $x, x(i)=i$, for $i=1, \ldots n$, of length $n=n_{x}^{2}$ in matrix-based order. It then converts it to distribution-based order and prints the vector on the root processor. The matrix-based order is determined by a sparse matrix $A$ representing a five-point finite-difference approximation to the partial differential equation:

$$
c_{1} \frac{\partial^{2} w}{\partial x^{2}}+c_{2} \frac{\partial^{2} w}{\partial y^{2}}+c_{3} \frac{\partial w}{\partial x}+c_{4} \frac{\partial w}{\partial y}+c_{5} w=f
$$

defined on the unit square.

### 8.1 Example Text

```
* F11YQFP Example Program Text
* NAG Parallel Library Release 3. NAG Copyright 1999.
* .. Parameters ..
    INTEGER NIN, NOUT
    PARAMETER (NIN=5,NOUT=6)
    INTEGER MLMAX
    PARAMETER (MLMAX=1000)
    INTEGER LA
    PARAMETER (LA=5*MLMAX)
    INTEGER LIA, LWORK
    PARAMETER (LIA=-1,LWORK=1)
    * .. Scalars in Common ..
    COMPLEX*16 C1, C2, C3, C4, C5
```

```
    INTEGER NX
* .. Local Scalars ..
    INTEGER ICNTXT, IFAIL, LEVEL, MB, ML, MP, N, NNZ, NP
    LOGICAL ROOT, ZGRID
    CHARACTER DUP, KIND, SYMM, ZERO
    CHARACTER*80 FORMAT
* .. Local Arrays ..
    COMPLEX*16 A(LA), WORK(LWORK), XD(MLMAX), XL(MLMAX)
    INTEGER CA(1), IAINFO(200), ICOL(LA), IERR(1), IROW(LA),
    + RA(1)
* .. External Functions ..
    LOGICAL Z01ACFP
    EXTERNAL Z01ACFP
* .. External Subroutines ..
    EXTERNAL F01CPFP, F01YPFP, F01YTFP, F11YQFP, F11ZPFP,
    + F11ZZFP, GMAT, GVEC, X04BWFP, Z01AAFP, Z01ABFP,
    + Z01BBFP, Z02EAFP
* .. Common blocks ..
    COMMON /PROB/C1, C2, C3, C4, C5, NX
* .. Executable Statements ..
    ROOT = Z01ACFP()
    IF (ROOT) WRITE (NOUT,*) 'F11YQFP Example Program Results'
*
* Open input file on all processors
*
    OPEN (NIN,FILE='f11yqfpe.d')
* Skip heading in data file
* Read size of processor grid
*
    READ (NIN,*)
    READ (NIN,*) MP
    NP = 1
* Read problem parameters
*
    READ (NIN,*) NX
    N = NX**2
*
* Read algorithmic parameters
*
    READ (NIN,*) MB
    READ (NIN,*) FORMAT
    READ (NIN,*) LEVEL
* Read complex coefficients in PDE
*
    READ (NIN,*) C1, C2, C3, C4, C5
*
* Close input file
*
    CLOSE (NIN)
* Initialize Library Grid
*
    IFAIL = 0
    CALL Z01AAFP(ICNTXT,MP,NP,IFAIL)
```

```
* Check whether processor is part of the Library Grid
*
    CALL Z01BBFP(ICNTXT,ZGRID,IFAIL)
    IF ( .NOT. ZGRID) GO TO 40
*
* Set error checking level
*
    CALL Z02EAFP(ICNTXT,LEVEL,IFAIL)
*
* Generate sparse matrix
*
    CALL F01YPFP(ICNTXT,GMAT,N,MB,NNZ,A,LA,IROW,ICOL,IFAIL)
*
* Set up auxiliary data for subsequent operations
    DUP = 'F'
    ZERO = 'R'
    SYMM = 'S'
    KIND = 'N'
    CALL F11ZPFP(ICNTXT,N,MB,NNZ,A,IROW,ICOL,DUP,ZERO,SYMM,KIND,
    +
        AINFO,LIA,IFAIL)
*
* Check whether number of rows is less than the corresponding
* maximum possible value determined by MLMAX
    ML = IAINFO(3)
    IERR(1) = 0
    IF (ML.GT.MLMAX) IERR(1) = 1
    CALL F01CPFP(ICNTXT,'X','All', 1,1,IERR,1,RA,CA,1,0,-1, -1,IFAIL)
    IF (IERR(1).NE.O) THEN
        IF (ROOT) WRITE (NOUT,99999)
        GO TO 20
    END IF
* Generate the vector in array XL in matrix-based order
*
    CALL F01YTFP(ICNTXT,GVEC,N,XL,IAINFO,IFAIL)
* Permute to ScaLAPACK/distribution-based order
*
    CALL F11YQFP(ICNTXT,N,XL,XD,IAINFO,IFAIL)
*
* Produce report
*
    IF (ROOT) THEN
        WRITE (NOUT,'(/1X,''Result vector''/1X,13(''_'')/)')
    END IF
    CALL X04BWFP(ICNTXT,NOUT,N,1,MB,XD,MLMAX,FORMAT,WORK,IFAIL)
*
* Release internally allocated memory if necessary
*
    20 IF (LIA.EQ.-1) CALL F11ZZFP(ICNTXT,IAINFO,IFAIL)
*
* Finalize Library Grid
*
    40 CALL Z01ABFP(ICNTXT,'N',IFAIL)
* End of example program
```

```
*
    STOP
*
99999 FORMAT (1X,'** ERROR: Number of rows per processor too large')
    END
    SUBROUTINE GMAT(I1,I2,N,NNZL,AL,LAL,IROWL,ICOLL)
* This routine generates a block tridiagonal matrix
* representing the five-point finite difference
* approximation to the equation:
*
* c1*W_xx + c2*w_yy + c3*\mp@subsup{w}{-}{}x + c4*w_y + c5*w = f
*
* where the ci are complex coefficients.
* The right-hand side vector is set up in the
* routine GVEC.
*
* .. Scalar Arguments ..
    INTEGER I1, I2, LAL, N, NNZL
* .. Array Arguments ..
    COMPLEX*16 AL(LAL)
    INTEGER ICOLL(LAL), IROWL(LAL)
* .. Scalars in Common ..
    COMPLEX*16 C1, C2, C3, C4, C5
    INTEGER NX
* .. Local Scalars ..
    COMPLEX*16 D1, D2, D3, D4, D5
    DOUBLE PRECISION H, RH, RH2
    INTEGER I, IX, IY
* .. Intrinsic Functions ..
    INTRINSIC DBLE, MOD
* .. Common blocks ..
    COMMON /PROB/C1, C2, C3, C4, C5, NX
* .. Executable Statements ..
*
* Calculate details of mesh
*
    H = 1/DBLE (NX+1)
    RH = 1.DO/H
    RH2 = RH*RH
*
* Define stencil coefficient
*
    D1 = -2*RH2*(C1+C2) + C5
    D2 = RH2*C1 + 0.5*RH*C3
    D3 = RH2*C1 - 0.5*RH*C3
    D4 = RH2*C2 + 0.5*RH*C4
    D5 = RH2*C2 - 0.5*RH*C4
*
* Check whether there is sufficient storage space
*
    IF (LAL.LT.5*(I2-I1+1)) THEN
        NNZL = -1
        RETURN
    END IF
```

```
    NNZL = 0
    DO 20 I = I1, I2
* Calculate indices of mesh node
    IX = 1 + MOD(I-1,NX)
    IY = 1 + (I-1)/NX
*
* Set up diagonal elements of matrix first
*
    NNZL = NNZL + 1
    IROWL(NNZL) = I
    ICOLL(NNZL) = I
    AL(NNZL) = D1
* Now add off-diagonal elements where necessary
*
    IF (IX.GT.1) THEN
        NNZL = NNZL + 1
        IROWL(NNZL) = I
        ICOLL(NNZL) = I - 1
        AL(NNZL) = D3
    END IF
    IF (IX.LT.NX) THEN
        NNZL = NNZL + 1
        IROWL(NNZL) = I
        ICOLL(NNZL) = I + 1
        AL(NNZL) = D2
            END IF
        IF (IY.GT.1) THEN
        NNZL = NNZL + 1
        IROWL(NNZL) = I
        ICOLL(NNZL) = I - NX
        AL(NNZL) = D5
    END IF
    IF (IY.LT.NX) THEN
            NNZL = NNZL + 1
            IROWL(NNZL) = I
            ICOLL(NNZL) = I + NX
            AL(NNZL) = D4
    END IF
*
    2 0 ~ C O N T I N U E ~
    RETURN
    END
    SUBROUTINE GVEC(I1,I2,X)
*
*
* .. Scalar Arguments ..
    INTEGER I1, I2
* .. Array Arguments ..
    COMPLEX*16 X(*)
* .. Local Scalars ..
```


## INTEGER <br> I

* .. Intrinsic Functions ..

INTRINSIC CMPLX, DBLE

* .. Executable Statements ..

DO 20 I = I1, I2
$X(I-I 1+1)=\operatorname{CMPLX}(\operatorname{DBLE}(I),-\operatorname{DBLE}(I))$
20 CONTINUE

RETURN
END

### 8.2 Example Data

```
F11YQFP Example Program Data
    4 : MP
    4 : NX
    4 : MB
'(4(:,', (',,F7.3,'','',F7.3,'')''))' : FORMAT
    0 : LEVEL
    (1.0, 2.0) (1.0,-1.0)
    (0.0, 3.0) (1.0, 0.0)
    (1.3,-2.2) : C1, C2, C3, C4, C5
```


### 8.3 Example Results

F11YQFP Example Program Results
Result vector
( $1.000,-1.000$ )
( $2.000,-2.000$ )
( 3.000, -3.000)
( $4.000,-4.000$ )
( $5.000,-5.000)$
( $6.000,-6.000$ )
( 7.000, -7.000)
( 8.000, -8.000)
( 9.000, -9.000)
( 10.000,-10.000)
( $11.000,-11.000$ )
( $12.000,-12.000$ )
( $13.000,-13.000$ )
( 14.000,-14.000)
( $15.000,-15.000$ )
( $16.000,-16.000$ )

