## F01YWFP

## NAG Parallel Library Routine Document

Note: before using this routine, please read the Users' Note for your implementation to check for implementation-dependent details. You are advised to enclose any calls to NAG Parallel Library routines between calls to Z01AAFP and Z01ABFP.

## 1 Description

F01YWFP generates and distributes an $n$ by $n$ complex Hermitian banded matrix $A$, stored in compact storage format, on a one-dimensional logical grid of processors in column block distribution.

This routine distributes banded matrices in the form required by a number of the routines in Chapter F04 (especially F07HRFP (PZPBTRF) and F07HSFP (PZPBTRS) which are used for factorization and solution of complex banded linear systems). A user-supplied subroutine is required to generate a block of the matrix $A$ on each processor.

## 2 Specification

```
SUBROUTINE F01YWFP(GMAT, UPLO, N, BW, A, IDESCA, IFAIL)
COMPLEX*16 A (*)
INTEGER N, BW, IDESCA(*), IFAIL
CHARACTER*1 UPLO
EXTERNAL GMAT
```


## 3 Usage

### 3.1 Definitions

The following definitions are used in describing the data distribution within this document:

| $b_{w}$ | - | the half band width of the complex Hermitian banded matrix; |
| :--- | :--- | :--- |
| $p$ | - | $m_{p} \times n_{p}$, the total number of processors in the Library Grid. |
| $m_{p}$ | - | the number of rows in the Library Grid, for this routine $m_{p}=1$ or $m_{p}=p ;$ |
| $n_{p}$ | - | the number of columns in the Library Grid, for this routine $n_{p}=1$ or $n_{p}=p$. |
| $M_{b}^{X}$ | - | the blocking factor for the distribution of the rows of a matrix $X$. |
| $N_{b}^{X}$ | - | the blocking factor for the distribution of the columns of a matrix $X$. |

### 3.2 Global and Local Arguments

The following global input arguments must have the same value on entry to the routine on each processor and the global output arguments will have the same value on exit from the routine on each processor:

Global input arguments: UPLO, N, BW, some elements of IDESCA (see Section 4 for a description of IDESCA), IFAIL
Global output arguments: IFAIL
The remaining arguments are local.

### 3.3 Distribution Strategy

The matrix $A$ will be distributed over a one-dimensional array of processors, assuming a column block distribution and stored in an array A. For Hermitian banded matrix, $A$, is stored in compact storage format (see the F07 Chapter Introduction). It is important that $p \times N_{b}^{A} \geq n$ and $N_{b}^{A} \geq 2 \times b_{w}$. This means that no processor may access more than one block of the matrix. The column block distribution is described in more detail in the F07 Chapter Introduction.

## 4 Arguments

1: GMAT - SUBROUTINE, supplied by the user.
External Procedure
GMAT must return the block (represented below in bold) of the matrix $A$ in the array AL:

$$
A=\left(\begin{array}{cccccccccc}
a_{1,1} & \cdots & a_{1, b_{w}+1} & & & & & & & \\
\vdots & \ddots & \ddots & \ddots & & & & & & \\
a_{b_{w}+1,1} & \ddots & \ddots & \ddots & \mathbf{a}_{\mathbf{k}_{\mathbf{1}}, \mathbf{j}_{\mathbf{1}}} & & & & & \\
& \ddots & \ddots & \ddots & \vdots & \ddots & \mathbf{a}_{\mathbf{k}_{\mathbf{2}}, \mathbf{j}_{\mathbf{2}}} & & & \\
& & \ddots & \ddots & \mathbf{a}_{\mathbf{j}_{\mathbf{1}}, \mathbf{j}_{\mathbf{1}}} & \ddots & \vdots & \ddots & & \\
& & & \ddots & \vdots & \ddots & \mathbf{a}_{\mathbf{j}_{\mathbf{2}}, \mathbf{j}_{\mathbf{2}}} & \ddots & \ddots & \\
& & & & a_{l_{1}, j_{1}} & \ddots & \vdots & \ddots & \ddots & \ddots \\
& & & & & a_{l_{2}, j_{2}} & \ddots & \ddots & \ddots & a_{n-b_{w}, n} \\
& & & & & & & \ddots & \ddots & \ddots \\
& & & & & & & & a_{n, n-b_{w}} & \cdots \\
& a_{n, n}
\end{array}\right)
$$

if UPLO $=$ ' $\mathrm{U}^{\prime}$; and
if UPLO $=$ 'L'; where $k_{1}, k_{2}, l_{1}$ and $l_{2}$ are such that;

$$
\begin{aligned}
& k_{i}=\max \left(1, j_{i}-b_{w}\right) \text { for } i=1,2 \text { and } \\
& l_{i}=\min \left(n: j_{i}+b_{w}\right) \text { for } i=1,2 .
\end{aligned}
$$

More precisely,

$$
\mathrm{AL}(k, j)=a_{i j}
$$

where $i, j, k$ are such that:
$j_{1} \leq j \leq j_{2} ;$
$1 \leq k \leq b_{w}+1 ;$
$\max \left(1, j-b_{w}\right) \leq i \leq j$ if UPLO $={ }^{\prime} \mathrm{L}$ ';
$j \leq i \leq \min \left(n, j+b_{w}\right)$ if UPLO $={ }^{\prime} \mathrm{U}^{\prime}$;
and $i$ is the $k^{t h}$ index where the corresponding term $a_{i j}$ lies (see the F07 Chapter Introduction).

Its specification is:

```
SUBROUTINE GMAT(J1, J2, BW,UPLO, AL, LDAL)
COMPLEX*16 AL (LDAL,*)
INTEGER J1, J2, BW, LDAL
```

1: J1 - INTEGER
Local Input
On entry: $\quad j_{1}$, the first column of the block of $A$ to be generated.
2: J2 - INTEGER
Local Input
On entry: $j_{2}$, the last column of the block of $A$ to be generated.
3: BW - INTEGER
Global Input
On entry: $b_{w}$, the half band width of the matrix $A$ to be generated.
4: UPLO - CHARACTER*1
Global Input
On entry: indicates whether the upper or the lower triangular part of the matrix $A$ is required.
If UPLO $=$ ' U ', then a block of the upper traingular part of $A$ is required;
if UPLO $=$ 'L', then a block of the lower traingular part of $A$ is required.
5: $\operatorname{AL}\left(\mathrm{LDAL},{ }^{*}\right)$ - COMPLEX* 16 array
Local Output
On exit: AL must contain the upper or lower triangular (depending on the value of UPLO) part of columns $j_{1}$ to $j_{2}$ of the band matrix $A$.

6: LDAL - INTEGER
Local Input
On entry: the size of the first dimension of the array AL as declared in the (sub)program from which F01YWFP is called.

GMAT must be declared as EXTERNAL in the (sub)program from which F01YWFP is called. Arguments denoted as Input must not be changed by this procedure.

2: UPLO - CHARACTER*1
Global Input
On entry: indicates whether the upper or lower triangular part of $A$ is stored :
if UPLO $=$ ' U ', then the upper triangular part of $A$ is stored.
if UPLO $=$ 'L', then the lower triangular part of $A$ is stored.
Constraint: $\quad \mathrm{UPLO}=$ ' U ' or ' L '.
3: N - INTEGER
Global Input
On entry: $n$, the order of the matrix $A$.
Constraint: $\mathrm{N} \geq 0$.
4: BW - INTEGER
Global Input
On entry: $b_{w}$, the half band width of matrix $A$.
Constraints: $0 \leq \mathrm{BW} \leq \mathrm{N}-1$.
5: $\mathrm{A}(*)-$ COMPLEX*16 array
Note: the array A is formally defined as a vector. However, you may find it more convenient to consider A as a two-dimensional array of dimension $\left(\ell_{A}, \gamma\right)$ where $\ell_{A}=\operatorname{IDESCA}(9)$ if $\operatorname{IDESCA}(1)=1$, or $\ell_{A}=\operatorname{IDESCA}(6)$ if $\operatorname{IDESCA}(1)=501$, and $\gamma \geq N_{b}^{A}$.
On exit: the local part of the matrix $A$ (stored in compact storage format) which will contain the upper part if UPLO $=$ ' U ' or the lower part if UPLO $=$ 'L'. See the F07 Chapter Introduction for further details.

6: $\operatorname{IDESCA}(*)$ - INTEGER array
Note: the dimension of the array IDESCA must be at least 9 when $\operatorname{IDESCA}(1)=1$, and at least 6 when $\operatorname{IDESCA}(1)=501$.
Distribution: if $\operatorname{IDESCA}(1)=1$, the array elements $\operatorname{IDESCA}(3: 8)$, must be global to each processor on the Library Grid. If $\operatorname{IDESCA}(1)=501$, then only the array elements $\operatorname{IDESCA}(3: 5)$ must be global. In either case IDESCA(2) is local to each processor.

On entry: the array descriptor for the matrix $A$. This array must contain details of the distribution of the matrix $A$ and the logical processor grid.

IDESCA(1), the descriptor type.
If $\operatorname{IDESCA}(1)=501$, then $p=1 \times n_{p}$ or $p=m_{p} \times 1$, and the remaining elements of IDESCA must be set as follows:

IDESCA(2), the Library context, usually returned by a call to the Library Grid initialisation routine Z01AAFP;
$\operatorname{IDESCA}(3)$, the size $n$, of the matrix $A$;
IDESCA(4), the blocking factor, $N_{b}^{A}$, used to distribute the columns of the matrix $A$;
IDESCA(5), the processor index over which the first column of the matrix $A$ is distributed;
IDESCA(6), the leading dimension of the conceptual two-dimensional array A.
$\operatorname{IDESCA}(7: 9)$ are not referenced.
If $\operatorname{IDESCA}(1)=1$, then $p=1 \times n_{p}$ and the remaining elements of IDESCA must be set as follows:

IDESCA(2), the Library context, usually returned by a call to the Library Grid initialisation routine Z01AAFP;
$\operatorname{IDESCA}(3)$, the number of rows, $n$, of the matrix $A$;
$\operatorname{IDESCA}(4)$, the number of columns, $n$, of the matrix $A$;
$\operatorname{IDESCA}(5)$, is not referenced;
IDESCA(6), the blocking factor, $N_{b}^{A}$, used to distribute the columns of the matrix $A$;
$\operatorname{IDESCA}(7)$, the processor index over which the first column of the matrix $A$ is distributed;
$\operatorname{IDESCA}(8)$, is not referenced;
IDESCA(9), the leading dimension of the conceptual two-dimensional array A.
Suggested value: $\operatorname{IDESCA}(1)=501$ and $p=1 \times n_{p}$, if $\operatorname{IDESCB}(1)=1, \operatorname{IDESCB}(5)=\operatorname{IDESCB}(8)$ $=1$.

Constraints:

```
\(\operatorname{IDESCA}(1)=1\) or 501 ;
if \(\operatorname{IDESCA}(1)=1\), then \(p=1 \times n_{p}\);
if \(\operatorname{IDESCA}(1)=501\); then \(p=m_{p} \times 1\) or \(p=1 \times n_{p}\);
if \(\operatorname{IDESCA}(1)=501\), then
    \(\operatorname{IDESCA}(3)=\mathrm{N}\);
    \(\operatorname{IDESCA}(4) \geq 2 \times \mathrm{BW}\) and \(p \times \operatorname{IDESCA}(4) \geq \mathrm{N}\);
    \(\operatorname{IDESCA}(5) \geq 0\);
    \(\operatorname{IDESCA}(6) \geq \mathrm{BW}+1\);
if \(\operatorname{IDESCA}(1)=1\), then
    \(\operatorname{IDESCA}(3)=\operatorname{IDESCA}(4)=\mathrm{N}\);
    \(\operatorname{IDESCA}(6) \geq 2 \times \mathrm{BW}\) and \(p \times \operatorname{IDESCA}(6) \geq \mathrm{N}\);
    \(\operatorname{IDESCA}(7) \geq 0\);
    \(\operatorname{IDESCA}(9) \geq \mathrm{BW}+1\).
```

7: IFAIL - INTEGER
Global Input/Global Output
The NAG Parallel Library provides a mechanism, via the routine Z02EAFP, to reduce the amount of parameter validation performed by this routine. For a full description refer to the Z02 Chapter Introduction.
On entry: IFAIL must be set to $0,-1$ or 1 . For users not familiar with this argument (described in the Essential Introduction) the recommended values are:

IFAIL $=0$, if multigridding is not employed;
$\operatorname{IFAIL}=-1$, if multigridding is employed.
On exit: IFAIL $=0$ (or -9999 if reduced error checking is enabled) unless the routine detects an error (see Section 5).

## 5 Errors and Warnings

If on entry IFAIL $=0$ or -1 , explanatory error messages are output from the root processor (or processor $\{0,0\}$ when the root processor is not available) on the current error message unit (as defined by X04AAF).
Errors detected by F01YWFP in the default error checking mode only
IFAIL $=-2000$
The routine has been called with a value of ICNTXT (stored in IDESCA(2)) which was not returned by a call to Z01AAFP on one or more processors.

IFAIL $=-1000$
The utility routine Z01AAFP has not been called to define the logical processor grid and initialise the internal variables used by the Library.
IFAIL $=-i$
On entry, one of the arguments was invalid:
if the $k$ th argument is a scalar IFAIL $=-k$;
if the $k$ th argument is an array and its $j$ th element is invalid, IFAIL $=-(100 \times k+j)$.
This error occured either because a global argument did not have the same value on all logical processors, or because its value on one or more processors was incorrect. An explanatory message distinguishes between these two cases.

## 6 Further Comments

### 6.1 Algorithmic Detail

The routine generates a complex Hermitian banded matrix and stores it in a one-dimensional array distributed by block-columns on a one-dimensional logical grid of processors.

### 6.2 Parallelism Detail

The routine generates the matrix on each logical processor independently.

## 7 References

[1] Blackford L S, Choi J, Cleary A, D'Azevedo E, Demmel J, Dhillon I, Dongarra J, Hammarling S, Henry G, Petitet A, Stanley K, Walker D and Whaley R C (1997) ScaLAPACK Users' Guide SIAM 3600 University City Science Center, Philadelpia, PA 19104-2688, USA. URL: http://www.netlib.org/scalapack/slug/scalapack_slug.html

## 8 Example

See Section 8 of the document for F07HRFP (PZPBTRF).

