

NAG Library Function Document

nag_zunmbr (f08kuc)

1 Purpose

nag_zunmbr (f08kuc) multiplies an arbitrary complex m by n matrix C by one of the complex unitary matrices Q or P which were determined by nag_zgebrd (f08ksc) when reducing a complex matrix to bidiagonal form.

2 Specification

```
#include <nag.h>
#include <nagf08.h>

void nag_zunmbr (Nag_OrderType order, Nag_VectType vect, Nag_SideType side,
                Nag_TransType trans, Integer m, Integer n, Integer k, const Complex a[],
                Integer pda, const Complex tau[], Complex c[], Integer pdc,
                NagError *fail)
```

3 Description

nag_zunmbr (f08kuc) is intended to be used after a call to nag_zgebrd (f08ksc), which reduces a complex rectangular matrix A to real bidiagonal form B by a unitary transformation: $A = QBP^H$. nag_zgebrd (f08ksc) represents the matrices Q and P^H as products of elementary reflectors.

This function may be used to form one of the matrix products

$$QC, Q^H C, CQ, CQ^H, PC, P^H C, CP \text{ or } CP^H,$$

overwriting the result on C (which may be any complex rectangular matrix).

4 References

Golub G H and Van Loan C F (1996) *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

5 Arguments

Note: in the descriptions below, r denotes the order of Q or P^H : if **side** = Nag_LeftSide, $r = \mathbf{m}$ and if **side** = Nag_RightSide, $r = \mathbf{n}$.

1: **order** – Nag_OrderType *Input*

On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.

Constraint: **order** = Nag_RowMajor or Nag_ColMajor.

2: **vect** – Nag_VectType *Input*

On entry: indicates whether Q or Q^H or P or P^H is to be applied to C .

vect = Nag_ApplyQ
 Q or Q^H is applied to C .

- vect** = Nag_ApplyP
 P or P^H is applied to C .
Constraint: **vect** = Nag_ApplyQ or Nag_ApplyP.
- 3: **side** – Nag_SideType *Input*
On entry: indicates how Q or Q^H or P or P^H is to be applied to C .
side = Nag_LeftSide
 Q or Q^H or P or P^H is applied to C from the left.
side = Nag_RightSide
 Q or Q^H or P or P^H is applied to C from the right.
Constraint: **side** = Nag_LeftSide or Nag_RightSide.
- 4: **trans** – Nag_TransType *Input*
On entry: indicates whether Q or P or Q^H or P^H is to be applied to C .
trans = Nag_NoTrans
 Q or P is applied to C .
trans = Nag_ConjTrans
 Q^H or P^H is applied to C .
Constraint: **trans** = Nag_NoTrans or Nag_ConjTrans.
- 5: **m** – Integer *Input*
On entry: m , the number of rows of the matrix C .
Constraint: **m** ≥ 0 .
- 6: **n** – Integer *Input*
On entry: n , the number of columns of the matrix C .
Constraint: **n** ≥ 0 .
- 7: **k** – Integer *Input*
On entry: if **vect** = Nag_ApplyQ, the number of columns in the original matrix A .
If **vect** = Nag_ApplyP, the number of rows in the original matrix A .
Constraint: **k** ≥ 0 .
- 8: **a**[*dim*] – const Complex *Input*
Note: the dimension, *dim*, of the array **a** must be at least
 $\max(1, \mathbf{pda} \times \min(r, \mathbf{k}))$ when **vect** = Nag_ApplyQ and **order** = Nag_ColMajor;
 $\max(1, r \times \mathbf{pda})$ when **vect** = Nag_ApplyQ and **order** = Nag_RowMajor;
 $\max(1, \mathbf{pda} \times r)$ when **vect** = Nag_ApplyP and **order** = Nag_ColMajor;
 $\max(1, \min(r, \mathbf{k}) \times \mathbf{pda})$ when **vect** = Nag_ApplyP and **order** = Nag_RowMajor.
On entry: details of the vectors which define the elementary reflectors, as returned by nag_zgbrd (f08ksc).
- 9: **pda** – Integer *Input*
On entry: the stride separating row or column elements (depending on the value of **order**) in the array **a**.

Constraints:

if **order** = Nag_ColMajor,
 if **vect** = Nag_ApplyQ, **pda** \geq max(1, *r*);
 if **vect** = Nag_ApplyP, **pda** \geq max(1, min(*r*, **k**));
 if **order** = Nag_RowMajor,
 if **vect** = Nag_ApplyQ, **pda** \geq max(1, min(*r*, **k**));
 if **vect** = Nag_ApplyP, **pda** \geq max(1, *r*).

10: **tau**[*dim*] – const Complex *Input*

Note: the dimension, *dim*, of the array **tau** must be at least max(1, min(*r*, **k**)).

On entry: further details of the elementary reflectors, as returned by nag_zgebrd (f08ksc) in its argument **taup** if **vect** = Nag_ApplyQ, or in its argument **taup** if **vect** = Nag_ApplyP.

11: **c**[*dim*] – Complex *Input/Output*

Note: the dimension, *dim*, of the array **c** must be at least

max(1, **pd**c \times **n**) when **order** = Nag_ColMajor;
 max(1, **m** \times **pd**c) when **order** = Nag_RowMajor.

The (*i*, *j*)th element of the matrix *C* is stored in

c[(*j* – 1) \times **pd**c + *i* – 1] when **order** = Nag_ColMajor;
c[(*i* – 1) \times **pd**c + *j* – 1] when **order** = Nag_RowMajor.

On entry: the matrix *C*.

On exit: **c** is overwritten by *QC* or *Q^HC* or *CQ* or *C^HQ* or *PC* or *P^HC* or *CP* or *C^HP* as specified by **vect**, **side** and **trans**.

12: **pd**c – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **c**.

Constraints:

if **order** = Nag_ColMajor, **pd**c \geq max(1, **m**);
 if **order** = Nag_RowMajor, **pd**c \geq max(1, **n**).

13: **fail** – NagError * *Input/Output*

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_BAD_PARAM

On entry, argument (*value*) had an illegal value.

NE_ENUM_INT_2

On entry, **vect** = $\langle value \rangle$, **pda** = $\langle value \rangle$, **k** = $\langle value \rangle$.
 Constraint: if **vect** = Nag_ApplyQ, **pda** $\geq \max(1, \min(r, \mathbf{k}))$;
 if **vect** = Nag_ApplyP, **pda** $\geq \max(1, r)$.

On entry, **vect** = $\langle value \rangle$, **pda** = $\langle value \rangle$ and **k** = $\langle value \rangle$.
 Constraint: if **vect** = Nag_ApplyQ, **pda** $\geq \max(1, r)$;
 if **vect** = Nag_ApplyP, **pda** $\geq \max(1, \min(r, \mathbf{k}))$.

NE_INT

On entry, **k** = $\langle value \rangle$.
 Constraint: **k** ≥ 0 .

On entry, **m** = $\langle value \rangle$.
 Constraint: **m** ≥ 0 .

On entry, **n** = $\langle value \rangle$.
 Constraint: **n** ≥ 0 .

On entry, **pda** = $\langle value \rangle$.
 Constraint: **pda** > 0 .

On entry, **pdcc** = $\langle value \rangle$.
 Constraint: **pdcc** > 0 .

NE_INT_2

On entry, **pdcc** = $\langle value \rangle$ and **m** = $\langle value \rangle$.
 Constraint: **pdcc** $\geq \max(1, \mathbf{m})$.

On entry, **pdcc** = $\langle value \rangle$ and **n** = $\langle value \rangle$.
 Constraint: **pdcc** $\geq \max(1, \mathbf{n})$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.
 See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.
 See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

The computed result differs from the exact result by a matrix E such that

$$\|E\|_2 = O(\epsilon)\|C\|_2,$$

where ϵ is the *machine precision*.

8 Parallelism and Performance

nag_zunmbr (f08kuc) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

nag_zunmbr (f08kuc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

The total number of real floating-point operations is approximately

if **side** = Nag_LeftSide and $m \geq k$, $8nk(2m - k)$;

if **side** = Nag_RightSide and $n \geq k$, $8mk(2n - k)$;

if **side** = Nag_LeftSide and $m < k$, $8m^2n$;

if **side** = Nag_RightSide and $n < k$, $8mn^2$,

where k is the value of the argument **k**.

The real analogue of this function is nag_dormbr (f08kgc).

10 Example

For this function two examples are presented. Both illustrate how the reduction to bidiagonal form of a matrix A may be preceded by a QR or LQ factorization of A .

In the first example, $m > n$, and

$$A = \begin{pmatrix} 0.96 - 0.81i & -0.03 + 0.96i & -0.91 + 2.06i & -0.05 + 0.41i \\ -0.98 + 1.98i & -1.20 + 0.19i & -0.66 + 0.42i & -0.81 + 0.56i \\ 0.62 - 0.46i & 1.01 + 0.02i & 0.63 - 0.17i & -1.11 + 0.60i \\ -0.37 + 0.38i & 0.19 - 0.54i & -0.98 - 0.36i & 0.22 - 0.20i \\ 0.83 + 0.51i & 0.20 + 0.01i & -0.17 - 0.46i & 1.47 + 1.59i \\ 1.08 - 0.28i & 0.20 - 0.12i & -0.07 + 1.23i & 0.26 + 0.26i \end{pmatrix}.$$

The function first performs a QR factorization of A as $A = Q_a R$ and then reduces the factor R to bidiagonal form B : $R = Q_b B P^H$. Finally it forms Q_a and calls nag_zunmbr (f08kuc) to form $Q = Q_a Q_b$.

In the second example, $m < n$, and

$$A = \begin{pmatrix} 0.28 - 0.36i & 0.50 - 0.86i & -0.77 - 0.48i & 1.58 + 0.66i \\ -0.50 - 1.10i & -1.21 + 0.76i & -0.32 - 0.24i & -0.27 - 1.15i \\ 0.36 - 0.51i & -0.07 + 1.33i & -0.75 + 0.47i & -0.08 + 1.01i \end{pmatrix}.$$

The function first performs an LQ factorization of A as $A = L P_a^H$ and then reduces the factor L to bidiagonal form B : $L = Q B P_b^H$. Finally it forms P_b^H and calls nag_zunmbr (f08kuc) to form $P^H = P_b^H P_a^H$.

10.1 Program Text

```

/* nag_zunmbr (f08kuc) Example Program.
*
* NAGPRODCODE Version.
*
* Copyright 2016 Numerical Algorithms Group.
*
* Mark 26, 2016.
*/

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <naga02.h>
#include <nagf08.h>
#include <nagx04.h>

```

```

int main(void)
{
    /* Scalars */
    Integer i, ic, j, m, n, pda, pdph, pdu;
    Integer d_len, e_len, tau_len, tauq_len, taup_len;
    Integer exit_status = 0;
    NagError fail;
    Nag_OrderType order;
    /* Arrays */
    Complex *a = 0, *ph = 0, *tau = 0, *taup = 0, *tauq = 0, *u = 0;
    double *d = 0, *e = 0;

#ifdef NAG_COLUMN_MAJOR
#define A(I, J)  a[(J-1)*pda + I - 1]
#define U(I, J)  u[(J-1)*pdu + I - 1]
#define PH(I, J) ph[(J-1)*pdph + I - 1]
    order = Nag_ColMajor;
#else
#define A(I, J)  a[(I-1)*pda + J - 1]
#define U(I, J)  u[(I-1)*pdu + J - 1]
#define PH(I, J) ph[(I-1)*pdph + J - 1]
    order = Nag_RowMajor;
#endif

    INIT_FAIL(fail);

    printf("nag_zunmbr (f08kuc) Example Program Results\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif
    for (ic = 1; ic <= 2; ++ic) {
#ifdef _WIN32
        scanf_s("%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &m, &n);
#else
        scanf("%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &m, &n);
#endif
    }

#ifdef NAG_COLUMN_MAJOR
    pda = m;
    pdph = n;
    pdu = m;
#else
    pda = n;
    pdph = n;
    pdu = m;
#endif
    tau_len = n;
    taup_len = n;
    tauq_len = n;
    d_len = n;
    e_len = n - 1;

    /* Allocate memory */
    if (!(a = NAG_ALLOC(m * n, Complex)) ||
        !(ph = NAG_ALLOC(n * n, Complex)) ||
        !(tau = NAG_ALLOC(tau_len, Complex)) ||
        !(taup = NAG_ALLOC(taup_len, Complex)) ||
        !(tauq = NAG_ALLOC(tauq_len, Complex)) ||
        !(u = NAG_ALLOC(m * m, Complex)) ||
        !(d = NAG_ALLOC(d_len, double)) || !(e = NAG_ALLOC(e_len, double)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto ENDL;
    }

    /* Read A from data file */

```

```

    for (i = 1; i <= m; ++i) {
        for (j = 1; j <= n; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#endif
    }
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif
    if (m >= n) {
        /* Compute the QR factorization of A */
        /* nag_zgeqrf (f08asc).
         * QR factorization of complex general rectangular matrix
         */
        nag_zgeqrf(order, m, n, a, pda, tau, &fail);
        if (fail.code != NE_NOERROR) {
            printf("Error from nag_zgeqrf (f08asc).\n%s\n", fail.message);
            exit_status = 1;
            goto ENDL;
        }
        /* Copy A to U */
        for (i = 1; i <= m; ++i) {
            for (j = 1; j <= n; ++j) {
                U(i, j).re = A(i, j).re;
                U(i, j).im = A(i, j).im;
            }
        }
        /* Form Q explicitly, storing the result in U */
        /* nag_zungqr (f08atc).
         * Form all or part of unitary Q from QR factorization
         * determined by nag_zgeqrf (f08asc) or nag_zgeqpf (f08bsc)
         */
        nag_zungqr(order, m, n, n, u, pdu, tau, &fail);
        if (fail.code != NE_NOERROR) {
            printf("Error from nag_zungqr (f08atc).\n%s\n", fail.message);
            exit_status = 1;
            goto ENDL;
        }
        /* Copy R to PH (used as workspace) */
        for (i = 1; i <= n; ++i) {
            for (j = i; j <= n; ++j) {
                PH(i, j).re = A(i, j).re;
                PH(i, j).im = A(i, j).im;
            }
        }
        /* Set the strictly lower triangular part of R to zero */
        for (i = 2; i <= n; ++i) {
            for (j = 1; j <= MIN(i - 1, n - 1); ++j) {
                PH(i, j).re = 0.0;
                PH(i, j).im = 0.0;
            }
        }
        /* Bidiagonalize R */
        /* nag_zgebrd (f08ksc).
         * Unitary reduction of complex general rectangular matrix
         * to bidiagonal form
         */
        nag_zgebrd(order, n, n, ph, pdph, d, e, tauq, taup, &fail);
        if (fail.code != NE_NOERROR) {
            printf("Error from nag_zgebrd (f08ksc).\n%s\n", fail.message);
            exit_status = 1;
            goto ENDL;
        }
        /* Update Q, storing the result in U */
        /* nag_zunmbr (f08kuc).
         * Apply unitary transformations from reduction to
         * bidiagonal form determined by nag_zgebrd (f08ksc)

```

```

*/
nag_zunmbr(order, Nag_ApplyQ, Nag_RightSide, Nag_NoTrans,
           m, n, n, ph, pdph, tauq, u, pdu, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_zunmbr (f08kuc).\n%s\n", fail.message);
    exit_status = 1;
    goto ENDL;
}
/* Print bidiagonal form and matrix Q */
printf("\nExample 1: bidiagonal matrix B\nDiagonal\n");
for (i = 1; i <= n; ++i)
    printf("%8.4f%s", d[i - 1], i % 8 == 0 ? "\n" : " ");
printf("\nSuperdiagonal\n");
for (i = 1; i <= n - 1; ++i)
    printf("%8.4f%s", e[i - 1], i % 8 == 0 ? "\n" : " ");
printf("\n\n");
/* nag_gen_complx_mat_print_comp (x04dbc).
 * Print complex general matrix (comprehensive)
 */
fflush(stdout);
nag_gen_complx_mat_print_comp(order,
                              Nag_GeneralMatrix,
                              Nag_NonUnitDiag,
                              m,
                              n,
                              u,
                              pdu,
                              Nag_BracketForm,
                              "%7.4f",
                              "Example 1: matrix Q",
                              Nag_IntegerLabels, 0,
                              Nag_IntegerLabels, 0, 80, 0, 0, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_complx_mat_print_comp (x04dbc).
           "\n%s\n", fail.message);
    exit_status = 1;
    goto ENDL;
}
}
else {
    /* Compute the LQ factorization of A */
    /* nag_zgelqf (f08avc).
     * LQ factorization of complex general rectangular matrix
     */
    nag_zgelqf(order, m, n, a, pda, tau, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_zgelqf (f08avc).\n%s\n", fail.message);
        exit_status = 1;
        goto ENDL;
    }
    /* Copy A to PH */
    for (i = 1; i <= m; ++i) {
        for (j = 1; j <= n; ++j) {
            PH(i, j).re = A(i, j).re;
            PH(i, j).im = A(i, j).im;
        }
    }
    /* Form Q explicitly, storing the result in PH */
    /* nag_zunglq (f08awc).
     * Form all or part of unitary Q from LQ factorization
     * determined by nag_zgelqf (f08avc)
     */
    nag_zunglq(order, m, n, m, ph, pdph, tau, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_zunglq (f08awc).\n%s\n", fail.message);
        exit_status = 1;
        goto ENDL;
    }
    /* Copy L to U (used as workspace) */
    for (i = 1; i <= m; ++i) {
        for (j = 1; j <= i; ++j) {

```



```

        U(i, j).re = A(i, j).re;
        U(i, j).im = A(i, j).im;
    }
}
/* Set the strictly upper triangular part of L to zero */
for (i = 1; i <= m - 1; ++i) {
    for (j = i + 1; j <= m; ++j) {
        U(i, j).re = 0.0;
        U(i, j).im = 0.0;
    }
}
/* Bidiagonalize L */
/* nag_zgebrd (f08ksc), see above. */
nag_zgebrd(order, m, m, u, pdu, d, e, tauq, taup, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_zgebrd (f08ksc).\n%s\n", fail.message);
    exit_status = 1;
    goto ENDL;
}
/* Update P^H, storing the result in PH */
/* nag_zunmbr (f08kuc), see above. */
nag_zunmbr(order, Nag_ApplyP, Nag_LeftSide, Nag_ConjTrans,
           m, n, m, u, pdu, taup, ph, pdph, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_zunmbr (f08kuc).\n%s\n", fail.message);
    exit_status = 1;
    goto ENDL;
}

/* Print bidiagonal form and matrix P^H */
printf("\nExample 2: bidiagonal matrix B\n%s\n", "Diagonal");
for (i = 1; i <= m; ++i)
    printf("%8.4f%s", d[i - 1], i % 8 == 0 ? "\n" : " ");
printf("\nSuperdiagonal\n");
for (i = 1; i <= m - 1; ++i)
    printf("%8.4f%s", e[i - 1], i % 8 == 0 ? "\n" : " ");
printf("\n\n");
/* nag_gen_complx_mat_print_comp (x04dbc), see above. */
fflush(stdout);
nag_gen_complx_mat_print_comp(order,
                              Nag_GeneralMatrix,
                              Nag_NonUnitDiag,
                              m,
                              n,
                              ph,
                              pdph,
                              Nag_BracketForm,
                              "%7.4f",
                              "Example 2: matrix P^H",
                              Nag_IntegerLabels, 0,
                              Nag_IntegerLabels, 0, 80, 0, 0, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_complx_mat_print_comp (x04dbc)."\n%s\n", fail.message);
    exit_status = 1;
    goto ENDL;
}
}
}
ENDL:
NAG_FREE(a);
NAG_FREE(ph);
NAG_FREE(tau);
NAG_FREE(taup);
NAG_FREE(tauq);
NAG_FREE(u);
NAG_FREE(d);
NAG_FREE(e);
}
NAG_FREE(a);
NAG_FREE(ph);
NAG_FREE(tau);

```

```

NAG_FREE(taup);
NAG_FREE(tauq);
NAG_FREE(u);
NAG_FREE(d);
NAG_FREE(e);
return exit_status;
}

```

10.2 Program Data

```

nag_zunmbr (f08kuc) Example Program Data
  6 4 :Values of M and N, Example 1
( 0.96,-0.81) (-0.03, 0.96) (-0.91, 2.06) (-0.05, 0.41)
(-0.98, 1.98) (-1.20, 0.19) (-0.66, 0.42) (-0.81, 0.56)
( 0.62,-0.46) ( 1.01, 0.02) ( 0.63,-0.17) (-1.11, 0.60)
(-0.37, 0.38) ( 0.19,-0.54) (-0.98,-0.36) ( 0.22,-0.20)
( 0.83, 0.51) ( 0.20, 0.01) (-0.17,-0.46) ( 1.47, 1.59)
( 1.08,-0.28) ( 0.20,-0.12) (-0.07, 1.23) ( 0.26, 0.26) :End of matrix A
  3 4 :Values of M and N, Example 2
( 0.28,-0.36) ( 0.50,-0.86) (-0.77,-0.48) ( 1.58, 0.66)
(-0.50,-1.10) (-1.21, 0.76) (-0.32,-0.24) (-0.27,-1.15)
( 0.36,-0.51) (-0.07, 1.33) (-0.75, 0.47) (-0.08, 1.01) :End of matrix A

```

10.3 Program Results

```
nag_zunmbr (f08kuc) Example Program Results
```

Example 1: bidiagonal matrix B

Diagonal

```
-3.0870 -2.0660 -1.8731 -2.0022
```

Superdiagonal

```
 2.1126 -1.2628  1.6126
```

Example 1: matrix Q

```

      1          2          3          4
1 (-0.3110, 0.2624) ( 0.6521, 0.5532) ( 0.0427, 0.0361) (-0.2634,-0.0741)
2 ( 0.3175,-0.6414) ( 0.3488, 0.0721) ( 0.2287, 0.0069) ( 0.1101,-0.0326)
3 (-0.2008, 0.1490) (-0.3103, 0.0230) ( 0.1855,-0.1817) (-0.2956, 0.5648)
4 ( 0.1199,-0.1231) (-0.0046,-0.0005) (-0.3305, 0.4821) (-0.0675, 0.3464)
5 (-0.2689,-0.1652) ( 0.1794,-0.0586) (-0.5235,-0.2580) ( 0.3927, 0.1450)
6 (-0.3499, 0.0907) ( 0.0829,-0.0506) ( 0.3202, 0.3038) ( 0.3174, 0.3241)

```

Example 2: bidiagonal matrix B

Diagonal

```
 2.7615  1.6298 -1.3275
```

Superdiagonal

```
-0.9500 -1.0183
```

Example 2: matrix P^H

```

      1          2          3          4
1 (-0.1258, 0.1618) (-0.2247, 0.3864) ( 0.3460, 0.2157) (-0.7099,-0.2966)
2 ( 0.4148, 0.1795) ( 0.1368,-0.3976) ( 0.6885, 0.3386) ( 0.1667,-0.0494)
3 ( 0.4575,-0.4807) (-0.2733, 0.4981) (-0.0230, 0.3861) ( 0.1730, 0.2395)

```
