

NAG Library Function Document

nag_zgemm (f16zac)

1 Purpose

nag_zgemm (f16zac) performs matrix-matrix multiplication for a complex general matrix.

2 Specification

```
#include <nag.h>
#include <nagf16.h>

void nag_zgemm (Nag_OrderType order, Nag_TransType transa,
               Nag_TransType transb, Integer m, Integer n, Integer k, Complex alpha,
               const Complex a[], Integer pda, const Complex b[], Integer pdb,
               Complex beta, Complex c[], Integer pdc, NagError *fail)
```

3 Description

nag_zgemm (f16zac) performs one of the matrix-matrix operations

$$\begin{aligned} C &\leftarrow \alpha AB + \beta C, & C &\leftarrow \alpha A^T B + \beta C, & C &\leftarrow \alpha A^H B + \beta C, \\ C &\leftarrow \alpha AB^T + \beta C, & C &\leftarrow \alpha A^T B^T + \beta C, & C &\leftarrow \alpha A^H B^T + \beta C, \\ C &\leftarrow \alpha AB^H + \beta C, & C &\leftarrow \alpha A^T B^H + \beta C & \text{or } C &\leftarrow \alpha A^H B^H + \beta C, \end{aligned}$$

where A , B and C are complex matrices, and α and β are complex scalars; C is always m by n .

4 References

Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001) *Basic Linear Algebra Subprograms Technical (BLAST) Forum Standard* University of Tennessee, Knoxville, Tennessee <http://www.netlib.org/blas/blast-forum/blas-report.pdf>

5 Arguments

1: **order** – Nag_OrderType *Input*

On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.

Constraint: **order** = Nag_RowMajor or Nag_ColMajor.

2: **transa** – Nag_TransType *Input*

On entry: specifies whether the operation involves A , A^T or A^H .

transa = Nag_NoTrans

It involves A .

transa = Nag_Trans

It involves A^T .

transa = Nag_ConjTrans

It involves A^H .

Constraint: **transa** = Nag_NoTrans, Nag_Trans or Nag_ConjTrans.

- 3: **transb** – Nag_TransType *Input*
On entry: specifies whether the operation involves B , B^T or B^H .
transb = Nag_NoTrans
 It involves B .
transb = Nag_Trans
 It involves B^T .
transb = Nag_ConjTrans
 It involves B^H .
Constraint: **transb** = Nag_NoTrans, Nag_Trans or Nag_ConjTrans.
- 4: **m** – Integer *Input*
On entry: m , the number of rows of the matrix C ; the number of rows of A if **transa** = Nag_NoTrans, or the number of columns of A if **transa** = Nag_Trans or Nag_ConjTrans.
Constraint: $m \geq 0$.
- 5: **n** – Integer *Input*
On entry: n , the number of columns of the matrix C ; the number of columns of B if **transb** = Nag_NoTrans, or the number of rows of B if **transb** = Nag_Trans or Nag_ConjTrans.
Constraint: $n \geq 0$.
- 6: **k** – Integer *Input*
On entry: k , the number of columns of A if **transa** = Nag_NoTrans, or the number of rows of A if **transa** = Nag_Trans or Nag_ConjTrans; the number of rows of B if **transb** = Nag_NoTrans, or the number of columns of B if **transb** = Nag_Trans or Nag_ConjTrans.
Constraint: $k \geq 0$.
- 7: **alpha** – Complex *Input*
On entry: the scalar α .
- 8: **a**[*dim*] – const Complex *Input*
Note: the dimension, *dim*, of the array **a** must be at least
 $\max(1, \mathbf{pda} \times \mathbf{k})$ when **transa** = Nag_NoTrans and **order** = Nag_ColMajor;
 $\max(1, \mathbf{m} \times \mathbf{pda})$ when **transa** = Nag_NoTrans and **order** = Nag_RowMajor;
 $\max(1, \mathbf{pda} \times \mathbf{m})$ when **transa** = Nag_Trans or Nag_ConjTrans and
order = Nag_ColMajor;
 $\max(1, \mathbf{k} \times \mathbf{pda})$ when **transa** = Nag_Trans or Nag_ConjTrans and
order = Nag_RowMajor.
 If **order** = Nag_ColMajor, A_{ij} is stored in **a**[($j - 1$) \times **pda** + $i - 1$].
 If **order** = Nag_RowMajor, A_{ij} is stored in **a**[($i - 1$) \times **pda** + $j - 1$].
On entry: the matrix A ; A is m by k if **transa** = Nag_NoTrans, or k by m if **transa** = Nag_Trans or Nag_ConjTrans.
- 9: **pda** – Integer *Input*
On entry: the stride separating row or column elements (depending on the value of **order**) in the array **a**.

Constraints:

if **order** = Nag_ColMajor,
 if **transa** = Nag_NoTrans, **pda** \geq max(1, **m**);
 if **transa** = Nag_Trans or Nag_ConjTrans, **pda** \geq max(1, **k**);
 if **order** = Nag_RowMajor,
 if **transa** = Nag_NoTrans, **pda** \geq max(1, **k**);
 if **transa** = Nag_Trans or Nag_ConjTrans, **pda** \geq max(1, **m**).

10: **b**[*dim*] – const Complex

Input

Note: the dimension, *dim*, of the array **b** must be at least

max(1, **pdb** \times **n**) when **transb** = Nag_NoTrans and **order** = Nag_ColMajor;
 max(1, **k** \times **pdb**) when **transb** = Nag_NoTrans and **order** = Nag_RowMajor;
 max(1, **pdb** \times **k**) when **transb** = Nag_Trans or Nag_ConjTrans and
order = Nag_ColMajor;
 max(1, **n** \times **pdb**) when **transb** = Nag_Trans or Nag_ConjTrans and
order = Nag_RowMajor.

If **order** = Nag_ColMajor, B_{ij} is stored in **b**[(*j* – 1) \times **pdb** + *i* – 1].

If **order** = Nag_RowMajor, B_{ij} is stored in **b**[(*i* – 1) \times **pdb** + *j* – 1].

On entry: the matrix *B*; *B* is *k* by *n* if **transb** = Nag_NoTrans, or *n* by *k* if **transb** = Nag_Trans or Nag_ConjTrans.

11: **pdb** – Integer

Input

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **b**.

Constraints:

if **order** = Nag_ColMajor,
 if **transb** = Nag_NoTrans, **pdb** \geq max(1, **k**);
 if **transb** = Nag_Trans or Nag_ConjTrans, **pdb** \geq max(1, **n**);
 if **order** = Nag_RowMajor,
 if **transb** = Nag_NoTrans, **pdb** \geq max(1, **n**);
 if **transb** = Nag_Trans or Nag_ConjTrans, **pdb** \geq max(1, **k**).

12: **beta** – Complex

Input

On entry: the scalar β .

13: **c**[*dim*] – Complex

Input/Output

Note: the dimension, *dim*, of the array **c** must be at least

max(1, **pdc** \times **n**) when **order** = Nag_ColMajor;
 max(1, **m** \times **pdc**) when **order** = Nag_RowMajor.

If **order** = Nag_ColMajor, C_{ij} is stored in **c**[(*j* – 1) \times **pdc** + *i* – 1].

If **order** = Nag_RowMajor, C_{ij} is stored in **c**[(*i* – 1) \times **pdc** + *j* – 1].

On entry: the *m* by *n* matrix *C*.

If **beta** = 0, **c** need not be set.

On exit: the updated matrix *C*.

- 14: **pd**c – Integer *Input*
On entry: the stride separating row or column elements (depending on the value of **order**) in the array **c**.
Constraints:
 if **order** = Nag_ColMajor, **pd**c $\geq \max(1, \mathbf{m})$;
 if **order** = Nag_RowMajor, **pd**c $\geq \max(1, \mathbf{n})$.
- 15: **fail** – NagError * *Input/Output*
 The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_ENUM_INT_2

On entry, **transa** = $\langle value \rangle$, **k** = $\langle value \rangle$, **pda** = $\langle value \rangle$.

Constraint: if **transa** = Nag_NoTrans, **pda** $\geq \max(1, \mathbf{k})$.

On entry, **transa** = $\langle value \rangle$, **m** = $\langle value \rangle$, **pda** = $\langle value \rangle$.

Constraint: if **transa** = Nag_Trans or Nag_ConjTrans, **pda** $\geq \max(1, \mathbf{m})$.

On entry, **transa** = $\langle value \rangle$, **pda** = $\langle value \rangle$, **k** = $\langle value \rangle$.

Constraint: if **transa** = Nag_Trans or Nag_ConjTrans, **pda** $\geq \max(1, \mathbf{k})$.

On entry, **transa** = $\langle value \rangle$, **pda** = $\langle value \rangle$, **m** = $\langle value \rangle$.

Constraint: if **transa** = Nag_NoTrans, **pda** $\geq \max(1, \mathbf{m})$.

On entry, **transb** = $\langle value \rangle$, **k** = $\langle value \rangle$, **pdb** = $\langle value \rangle$.

Constraint: if **transb** = Nag_NoTrans, **pdb** $\geq \max(1, \mathbf{k})$.

On entry, **transb** = $\langle value \rangle$, **k** = $\langle value \rangle$, **pdb** = $\langle value \rangle$.

Constraint: if **transb** = Nag_Trans or Nag_ConjTrans, **pdb** $\geq \max(1, \mathbf{k})$.

On entry, **transb** = $\langle value \rangle$, **n** = $\langle value \rangle$, **pdb** = $\langle value \rangle$.

Constraint: if **transb** = Nag_NoTrans, **pdb** $\geq \max(1, \mathbf{n})$.

On entry, **transb** = $\langle value \rangle$, **n** = $\langle value \rangle$, **pdb** = $\langle value \rangle$.

Constraint: if **transb** = Nag_Trans or Nag_ConjTrans, **pdb** $\geq \max(1, \mathbf{n})$.

NE_INT

On entry, **k** = $\langle value \rangle$.

Constraint: **k** ≥ 0 .

On entry, **m** = $\langle value \rangle$.

Constraint: **m** ≥ 0 .

On entry, **n** = $\langle value \rangle$.

Constraint: **n** ≥ 0 .

NE_INT_2

On entry, **pdc** = $\langle value \rangle$, **m** = $\langle value \rangle$.

Constraint: **pdc** $\geq \max(1, \mathbf{m})$.

On entry, **pdc** = $\langle value \rangle$ and **n** = $\langle value \rangle$.

Constraint: **pdc** $\geq \max(1, \mathbf{n})$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 3.6.5 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

The BLAS standard requires accurate implementations which avoid unnecessary over/underflow (see Section 2.7 of Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001)).

8 Parallelism and Performance

nag_zgemm (f16zac) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

None.

10 Example

This example computes the matrix-matrix product

$$C = \alpha AB + \beta C$$

where

$$A = \begin{pmatrix} 1.0 + 1.0i & 1.0 + 2.0i & -2.0 + 3.0i \\ 2.0 + 1.0i & 2.0 + 2.0i & 1.0 + 2.0i \\ 3.0 + 1.0i & 3.0 + 2.0i & -3.0 + 2.0i \end{pmatrix},$$

$$B = \begin{pmatrix} 1.0 - 1.0i & 1.0 + 2.0i \\ -2.0 + 1.0i & 2.0 - 2.0i \\ 3.0 - 1.0i & -3.0 + 1.0i \end{pmatrix},$$

$$C = \begin{pmatrix} -3.5 - 0.5i & 1.5 + 2.0i \\ -4.5 + 1.5i & -2.0 + 3.5i \\ -5.5 + 3.5i & 3.0 - 1.5i \end{pmatrix},$$

$$\alpha = 1.0 + 0.0i \quad \text{and} \quad \beta = 2.0 + 0.0i.$$

10.1 Program Text

```

/* nag_zgemm (f16zac) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf16.h>
#include <nagx04.h>

int main(void)
{
    /* Scalars */
    Complex alpha, beta;
    Integer exit_status, i, j, k, m, n, pda, pdb, pdc;

    /* Arrays */
    Complex *a = 0, *b = 0, *c = 0;
    char nag_enum_arg[40];

    /* Nag Types */
    NagError fail;
    Nag_OrderType order;
    Nag_TransType transa;
    Nag_TransType transb;

#ifdef NAG_COLUMN_MAJOR
#define A(I, J) a[(J-1)*pda + I - 1]
#define B(I, J) b[(J-1)*pdb + I - 1]
#define C(I, J) c[(J-1)*pdc + I - 1]
    order = Nag_ColMajor;
#else
#define A(I, J) a[(I-1)*pda + J - 1]
#define B(I, J) b[(I-1)*pdb + J - 1]
#define C(I, J) c[(I-1)*pdc + J - 1]
    order = Nag_RowMajor;
#endif

    exit_status = 0;
    INIT_FAIL(fail);

    printf("nag_zgemm (f16zac) Example Program Results\n\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

    /* Read the problem dimensions */
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &m, &n, &k);
#else
    scanf("%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &m, &n, &k);
#endif

    /* Read the transpose parameters */
#ifdef _WIN32
    scanf_s("%39s%*[\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s%*[\n] ", nag_enum_arg);
#endif
}

```

```

/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
transa = (Nag_TransType) nag_enum_name_to_value(nag_enum_arg);
#ifdef _WIN32
scanf_s("%39s%*[\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
scanf("%39s%*[\n] ", nag_enum_arg);
#endif
/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
transb = (Nag_TransType) nag_enum_name_to_value(nag_enum_arg);
/* Read scalar parameters */
#ifdef _WIN32
scanf_s(" ( %lf , %lf ) ( %lf , %lf )%*[\n] ",
        &alpha.re, &alpha.im, &beta.re, &beta.im);
#else
scanf(" ( %lf , %lf ) ( %lf , %lf )%*[\n] ",
        &alpha.re, &alpha.im, &beta.re, &beta.im);
#endif

#ifdef NAG_COLUMN_MAJOR
pdc = m;
if (transa == Nag_NoTrans && transb == Nag_NoTrans) {
    pda = m;
    pdb = k;
}
else if ((transa == Nag_Trans || transa == Nag_ConjTrans)
        && transb == Nag_NoTrans) {
    pda = k;
    pdb = k;
}
else if (transa == Nag_NoTrans &&
        (transb == Nag_Trans || transb == Nag_ConjTrans)) {
    pda = m;
    pdb = n;
}
else {
    pda = k;
    pdb = n;
}
#else
pdc = n;
if (transa == Nag_NoTrans && transb == Nag_NoTrans) {
    pda = k;
    pdb = n;
}
else if ((transa == Nag_Trans || transa == Nag_ConjTrans)
        && transb == Nag_NoTrans) {
    pda = m;
    pdb = n;
}
else if (transa == Nag_NoTrans &&
        (transb == Nag_Trans || transb == Nag_ConjTrans)) {
    pda = k;
    pdb = k;
}
else {
    pda = m;
    pdb = k;
}
#endif

if (m > 0 && n > 0) {
    /* Allocate memory */
    if (!(a = NAG_ALLOC(m * k, Complex)) ||
        !(b = NAG_ALLOC(n * k, Complex)) || !(c = NAG_ALLOC(m * n, Complex)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
    }
}

```

```

        goto END;
    }
}
else {
    printf("Invalid m, n or k\n");
    exit_status = 1;
    return exit_status;
}

/* Input matrix A */
if (transa == Nag_NoTrans) {
    for (i = 1; i <= m; ++i) {
        for (j = 1; j <= k; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#endif
        }
#ifdef _WIN32
        scanf_s("%*[\n] ");
#else
        scanf("%*[\n] ");
#endif
    }
    else {
        for (i = 1; i <= k; ++i) {
            for (j = 1; j <= m; ++j)
#ifdef _WIN32
                scanf_s(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#else
                scanf(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#endif
            }
#ifdef _WIN32
            scanf_s("%*[\n] ");
#else
            scanf("%*[\n] ");
#endif
        }

/* Input matrix B */
if (transb == Nag_NoTrans) {
    for (i = 1; i <= k; ++i) {
        for (j = 1; j <= n; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#else
            scanf(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#endif
        }
#ifdef _WIN32
        scanf_s("%*[\n] ");
#else
        scanf("%*[\n] ");
#endif
    }
    else {
        for (i = 1; i <= n; ++i) {
            for (j = 1; j <= k; ++j)
#ifdef _WIN32
                scanf_s(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#else
                scanf(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#endif
            }
#ifdef _WIN32
            scanf_s("%*[\n] ");
#else
            scanf("%*[\n] ");
#endif
        }
}

```



```

}

/* Input matrix C */
for (i = 1; i <= m; ++i) {
  for (j = 1; j <= n; ++j)
#ifdef _WIN32
    scanf_s(" ( %lf , %lf )", &C(i, j).re, &C(i, j).im);
#else
    scanf(" ( %lf , %lf )", &C(i, j).re, &C(i, j).im);
#endif
}
#ifdef _WIN32
  scanf_s("%*[\n] ");
#else
  scanf("%*[\n] ");
#endif

/* nag_zgemm (f16zac).
 * Complex matrix-matrix multiply.
 */
nag_zgemm(order, transa, transb, m, n, k, alpha, a, pda,
          b, pdb, beta, c, pdc, &fail);
if (fail.code != NE_NOERROR) {
  printf("Error from nag_zgemm.\n%s\n", fail.message);
  exit_status = 1;
  goto END;
}

/* Print result */
/* nag_gen_complx_mat_print (x04dac).
 * Print Complex general matrix (easy-to-use)
 */
fflush(stdout);
nag_gen_complx_mat_print(order, Nag_GeneralMatrix, Nag_NonUnitDiag,
                        m, n, c, pdc, "Matrix Matrix Product", 0, &fail);
if (fail.code != NE_NOERROR) {
  printf("Error from nag_gen_complx_mat_print (x04dac).\n%s\n",
        fail.message);
  exit_status = 1;
  goto END;
}

END:
  NAG_FREE(a);
  NAG_FREE(b);
  NAG_FREE(c);

  return exit_status;
}

```

10.2 Program Data

```

nag_zgemm (f16zac) Example Program Data
3 2 3 :Values of m, n, k
Nag_NoTrans : transa
Nag_NoTrans : transb
( 1.0, 0.0) ( 2.0, 0.0) : alpha, beta
( 1.0, 1.0) ( 1.0, 2.0) (-2.0, 3.0)
( 2.0, 1.0) ( 2.0, 2.0) ( 1.0, 2.0)
( 3.0, 1.0) ( 3.0, 2.0) (-3.0, 2.0) : the end of matrix A
( 1.0,-1.0) ( 1.0, 2.0)
(-2.0, 1.0) ( 2.0,-2.0)
( 3.0,-1.0) (-3.0, 1.0) : the end of matrix B
(-3.5,-0.5) ( 1.5, 2.0)
(-4.5, 1.5) (-2.0, 3.5)
(-5.5, 3.5) ( 3.0,-1.5) : the end of matrix C

```

10.3 Program Results

nag_zgemm (f16zac) Example Program Results

	Matrix	Matrix	Product
		1	2
1	-12.0000	11.0000	
	7.0000	-2.0000	
2	-7.0000	-1.0000	
	5.0000	7.0000	
3	-22.0000	24.0000	
	13.0000	-7.0000	
