

NAG Library Function Document

nag_sparse_herm_precon_ssor_solve (f11jrc)

1 Purpose

nag_sparse_herm_precon_ssor_solve (f11jrc) solves a system of linear equations involving the preconditioning matrix corresponding to SSOR applied to a complex sparse Hermitian matrix, represented in symmetric coordinate storage format.

2 Specification

```
#include <nag.h>
#include <nagf11.h>

void nag_sparse_herm_precon_ssor_solve (Integer n, Integer nnz,
                                         const Complex a[], const Integer irow[], const Integer icol[],
                                         const double rdiag[], double omega, Nag_SparseSym_CheckData check,
                                         const Complex y[], Complex x[], NagError *fail)
```

3 Description

nag_sparse_herm_precon_ssor_solve (f11jrc) solves a system of equations

$$Mx = y$$

involving the preconditioning matrix

$$M = \frac{1}{\omega(2 - \omega)}(D + \omega L)D^{-1}(D + \omega L)^H$$

corresponding to symmetric successive-over-relaxation (SSOR) (see Young (1971)) on a linear system $Ax = b$, where A is a sparse complex Hermitian matrix stored in symmetric coordinate storage (SCS) format (see Section 2.1.2 in the f11 Chapter Introduction).

In the definition of M given above D is the diagonal part of A , L is the strictly lower triangular part of A and ω is a user-defined relaxation parameter. Note that since A is Hermitian the matrix D is necessarily real.

4 References

Young D (1971) *Iterative Solution of Large Linear Systems* Academic Press, New York

5 Arguments

- | | | |
|----|--|--------------|
| 1: | n – Integer | <i>Input</i> |
| | <i>On entry:</i> n , the order of the matrix A . | |
| | <i>Constraint:</i> $n \geq 1$. | |
| 2: | nnz – Integer | <i>Input</i> |
| | <i>On entry:</i> the number of nonzero elements in the lower triangular part of the matrix A . | |
| | <i>Constraint:</i> $1 \leq \text{nnz} \leq n \times (n + 1)/2$. | |

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_INT

On entry, $\mathbf{n} = \langle value \rangle$.

Constraint: $\mathbf{n} \geq 1$.

On entry, $\mathbf{nnz} = \langle value \rangle$.

Constraint: $\mathbf{nnz} \geq 1$.

NE_INT_2

On entry, $\mathbf{nnz} = \langle value \rangle$ and $\mathbf{n} = \langle value \rangle$.

Constraint: $\mathbf{nnz} \leq \mathbf{n} \times (\mathbf{n} + 1)/2$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in How to Use the NAG Library and its Documentation for further information.

NE_INVALID_SCS

On entry, $I = \langle value \rangle$, $\mathbf{icol}[I - 1] = \langle value \rangle$, $\mathbf{irow}[I - 1] = \langle value \rangle$.

Constraint: $1 \leq \mathbf{icol}[i - 1] \leq \mathbf{irow}[i - 1]$.

On entry, $I = \langle value \rangle$, $\mathbf{irow}[I - 1] = \langle value \rangle$ and $\mathbf{n} = \langle value \rangle$.

Constraint: $1 \leq \mathbf{irow}[i - 1] \leq \mathbf{n}$.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 3.6.5 in How to Use the NAG Library and its Documentation for further information.

NE_NOT_STRICTLY_INCREASING

On entry, $\mathbf{a}[i - 1]$ is out of order: $i = \langle value \rangle$.

On entry, the location $(\mathbf{irow}[I - 1], \mathbf{icol}[I - 1])$ is a duplicate: $I = \langle value \rangle$. Consider calling nag_sparse_herm_sort (f11zpc) to reorder and sum or remove duplicates.

NE_REAL

On entry, $\mathbf{omega} = \langle value \rangle$.

Constraint: $0.0 < \mathbf{omega} < 2.0$.

NE_ZERO_DIAG_ELEM

The matrix A has no diagonal entry in row $\langle value \rangle$.

7 Accuracy

The computed solution x is the exact solution of a perturbed system of equations $(M + \delta M)x = y$, where

$$|\delta M| \leq c(n)\epsilon|D + \omega L||D^{-1}||(D + \omega L)^T|,$$

$c(n)$ is a modest linear function of n , and ϵ is the **machine precision**.

8 Parallelism and Performance

`nag_sparse_herm_precon_ssor_solve` (f11jrc) is not threaded in any implementation.

9 Further Comments

9.1 Timing

The time taken for a call to `nag_sparse_herm_precon_ssor_solve` (f11jrc) is proportional to **nnz**.

10 Example

This example program solves the preconditioning equation $Mx = y$ for a 9 by 9 sparse complex Hermitian matrix A , given in symmetric coordinate storage (SCS) format.

10.1 Program Text

```
/* nag_sparse_herm_precon_ssor_solve (f11jrc) Example Program.
*
* NAGPRODCODE Version.
*
* Copyright 2016 Numerical Algorithms Group.
*
* Mark 26, 2016.
*/
#include <nag.h>
#include <nag_stdlib.h>
#include <naga02.h>
#include <nagf11.h>

int main(void)
{
    /* Scalars */
    Integer exit_status = 0;
    double omega;
    Integer i, n, nnz;
    /* Arrays */
    char nag_enum_arg[100];
    Complex *a = 0, *x = 0, *y = 0;
    double *rdiag = 0;
    Integer *icol = 0, *irow = 0;
    /* NAG types */
    Nag_SparseSym_CheckData check;
    NagError fail;

    INIT_FAIL(fail);

    printf("nag_sparse_herm_precon_ssor_solve (f11jrc) Example Program Results");
    printf("\n");
    /* Skip heading in data file */
#ifndef _WIN32
    scanf_s("%*[^\n]");
#else
    scanf("%*[^\n]");
#endif
    /* Read algorithmic parameters */
#ifndef _WIN32
    scanf_s("%" NAG_IFMT "%*[^\n] ", &n);
#else
    scanf("%" NAG_IFMT "%*[^\n] ", &n);
#endif
#ifndef _WIN32
    scanf_s("%" NAG_IFMT "%*[^\n] ", &nnz);
#else
    scanf("%" NAG_IFMT "%*[^\n] ", &nnz);
#endif
```

```

/* Allocate memory */
if (!(a = NAG_ALLOC(nnz, Complex)) ||
    !(x = NAG_ALLOC(n, Complex)) ||
    !(y = NAG_ALLOC(n, Complex)) ||
    !(rdiag = NAG_ALLOC(n, double)) ||
    !(icol = NAG_ALLOC(nnz, Integer)) || !(irow = NAG_ALLOC(nnz, Integer)))
)
{
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
}
#endif _WIN32
scanf_s("%99s*[^\\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
scanf("%99s*[^\\n] ", nag_enum_arg);
#endif
/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
check = (Nag_SparseSym_CheckData) nag_enum_name_to_value(nag_enum_arg);
#endif _WIN32
scanf_s("%lf%*[^\\n]", &omega);
#else
scanf("%lf%*[^\\n]", &omega);
#endif
/* Read the matrix a */
for (i = 0; i < nnz; i++)
#endif _WIN32
    scanf_s(" ( %lf , %lf ) %" NAG_IFMT "%" NAG_IFMT "%*[^\\n]",
            &a[i].re, &a[i].im, &irow[i], &icol[i]);
#else
    scanf(" ( %lf , %lf ) %" NAG_IFMT "%" NAG_IFMT "%*[^\\n]",
            &a[i].re, &a[i].im, &irow[i], &icol[i]);
#endif
/* Read rhs vector y */
for (i = 0; i < n; i++)
#endif _WIN32
    scanf_s(" ( %lf , %lf ) ", &y[i].re, &y[i].im);
#else
    scanf(" ( %lf , %lf ) ", &y[i].re, &y[i].im);
#endif
scanf_s("%*[^\\n]");
#endif
/* Fill in the diagonal part */
for (i = 0; i < nnz; i++)
    if (irow[i] == icol[i])
        rdiag[irow[i] - 1] = 1.0 / (double) (a[i].re);

/* nag_sparse_herm_precon_ssor_solve (f11jrc).
 * Solution of linear system involving preconditioning matrix
 * generated by applying SSOR to complex sparse Hermitian matrix
 */
nag_sparse_herm_precon_ssor_solve(n, nnz, a, irow, icol, rdiag,
                                  omega, check, y, x, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_sparse_herm_precon_ssor_solve (f11jrc)\n%s\n",
           fail.message);
    exit_status = 1;
    goto END;
}

/* Output x */
printf("      Converged Solution\n");
for (i = 0; i < n; i++)
    printf(" (%13.4e, %13.4e) \n", x[i].re, x[i].im);

```

```

END:
    NAG_FREE(a);
    NAG_FREE(x);
    NAG_FREE(y);
    NAG_FREE(rdiag);
    NAG_FREE(icol);
    NAG_FREE(irow);
    return exit_status;
}

```

10.2 Program Data

```

nag_sparse_herm_precon_ssor_solve (f11jrc) Example Program Data
    9                      : n
    23                     : nnz
Nag_SparseSym_Check   : check
    1.1                   : omega
( 6., 0.)   1   1
(-1., 1.)   2   1
( 6., 0.)   2   2
( 0., 1.)   3   2
( 5., 0.)   3   3
( 5., 0.)   4   4
( 2.,-2.)   5   1
( 4., 0.)   5   5
( 1., 1.)   6   3
( 2., 0.)   6   4
( 6., 0.)   6   6
(-4., 3.)   7   2
( 0., 1.)   7   5
(-1., 0.)   7   6
( 6., 0.)   7   7
(-1.,-1.)   8   4
( 0.,-1.)   8   6
( 9., 0.)   8   8
( 1., 3.)   9   1
( 1., 2.)   9   5
(-1., 0.)   9   6
( 1., 4.)   9   8
( 9., 0.)   9   9   : a[i], irow[i], icol[i], i=0,...,nnz-1
( 8., 54.)
(-10., -92.)
( 25., 27.)
( 26., -28.)
( 54., 12.)
( 26., -22.)
( 47., 65.)
( 71., -57.)
( 60., 70.)          : y[i], i=0,...,n-1

```

10.3 Program Results

```

nag_sparse_herm_precon_ssor_solve (f11jrc) Example Program Results
    Converged Solution
( 1.0977e+00,      5.9139e+00)
( 2.2304e-01,     -1.4085e+01)
( 2.2315e+00,      7.0868e+00)
( 4.8164e+00,     -6.1807e+00)
( 6.7632e+00,      1.5690e+00)
( 3.3531e+00,     -4.7849e+00)
( 6.6991e-01,     -1.4646e+00)
( 8.8315e+00,     -3.6326e+00)
( 4.7685e+00,      1.2130e-01)

```
