

NAG Library Function Document

nag_zhpgst (f08tsc)

1 Purpose

nag_zhpgst (f08tsc) reduces a complex Hermitian-definite generalized eigenproblem $Az = \lambda Bz$, $ABz = \lambda z$ or $BAz = \lambda z$ to the standard form $Cy = \lambda y$, where A is a complex Hermitian matrix and B has been factorized by nag_zpptrf (f07grc), using packed storage.

2 Specification

```
#include <nag.h>
#include <nagf08.h>

void nag_zhpgst (Nag_OrderType order, Nag_ComputeType comp_type,
                 Nag_UptoType uplo, Integer n, Complex ap[], const Complex bp[],
                 NagError *fail)
```

3 Description

To reduce the complex Hermitian-definite generalized eigenproblem $Az = \lambda Bz$, $ABz = \lambda z$ or $BAz = \lambda z$ to the standard form $Cy = \lambda y$ using packed storage, nag_zhpgst (f08tsc) must be preceded by a call to nag_zpptrf (f07grc) which computes the Cholesky factorization of B ; B must be positive definite.

The different problem types are specified by the argument **comp_type**, as indicated in the table below. The table shows how C is computed by the function, and also how the eigenvectors z of the original problem can be recovered from the eigenvectors of the standard form.

comp_type	Problem	uplo	B	C	z
Nag_Compute_1	$Az = \lambda Bz$	Nag_Upper Nag_Lower	$U^H U$ LL^H	$U^{-H} AU^{-1}$ $L^{-1} AL^{-H}$	$U^{-1} y$ $L^{-H} y$
Nag_Compute_2	$ABz = \lambda z$	Nag_Upper Nag_Lower	$U^H U$ LL^H	UAU^H $L^H AL$	$U^{-1} y$ $L^{-H} y$
Nag_Compute_3	$BAz = \lambda z$	Nag_Upper Nag_Lower	$U^H U$ LL^H	UAU^H $L^H AL$	$U^H y$ Ly

4 References

Golub G H and Van Loan C F (1996) *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

5 Arguments

1: **order** – Nag_OrderType *Input*

On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.

Constraint: **order** = Nag_RowMajor or Nag_ColMajor.

2: **comp_type** – Nag_ComputeType *Input*

On entry: indicates how the standard form is computed.

comp_type = Nag_Compute_1

if **uplo** = Nag_Upper, $C = U^{-H}AU^{-1}$;

if **uplo** = Nag_Lower, $C = L^{-1}AL^{-H}$.

comp_type = Nag_Compute_2 or Nag_Compute_3

if **uplo** = Nag_Upper, $C = UAU^H$;

if **uplo** = Nag_Lower, $C = L^HAL$.

Constraint: **comp_type** = Nag_Compute_1, Nag_Compute_2 or Nag_Compute_3.

3: **uplo** – Nag_UplType *Input*

On entry: indicates whether the upper or lower triangular part of A is stored and how B has been factorized.

uplo = Nag_Upper

The upper triangular part of A is stored and $B = U^H U$.

uplo = Nag_Lower

The lower triangular part of A is stored and $B = LL^H$.

Constraint: **uplo** = Nag_Upper or Nag_Lower.

4: **n** – Integer *Input*

On entry: n , the order of the matrices A and B .

Constraint: **n** ≥ 0 .

5: **ap[dim]** – Complex *Input/Output*

Note: the dimension, *dim*, of the array **ap** must be at least $\max(1, \mathbf{n} \times (\mathbf{n} + 1)/2)$.

On entry: the upper or lower triangle of the n by n Hermitian matrix A , packed by rows or columns.

The storage of elements A_{ij} depends on the **order** and **uplo** arguments as follows:

if **order** = Nag_ColMajor and **uplo** = Nag_Upper,

A_{ij} is stored in **ap** $[(j - 1) \times j/2 + i - 1]$, for $i \leq j$;

if **order** = Nag_ColMajor and **uplo** = Nag_Lower,

A_{ij} is stored in **ap** $[(2n - j) \times (j - 1)/2 + i - 1]$, for $i \geq j$;

if **order** = Nag_RowMajor and **uplo** = Nag_Upper,

A_{ij} is stored in **ap** $[(2n - i) \times (i - 1)/2 + j - 1]$, for $i \leq j$;

if **order** = Nag_RowMajor and **uplo** = Nag_Lower,

A_{ij} is stored in **ap** $[(i - 1) \times i/2 + j - 1]$, for $i \geq j$.

On exit: the upper or lower triangle of **ap** is overwritten by the corresponding upper or lower triangle of C as specified by **comp_type** and **uplo**, using the same packed storage format as described above.

6: **bp[dim]** – const Complex *Input*

Note: the dimension, *dim*, of the array **bp** must be at least $\max(1, \mathbf{n} \times (\mathbf{n} + 1)/2)$.

On entry: the Cholesky factor of B as specified by **uplo** and returned by nag_zpptrf (f07grc).

7: **fail** – NagError * *Input/Output*

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_INT

On entry, $\mathbf{n} = \langle value \rangle$.

Constraint: $\mathbf{n} \geq 0$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 3.6.5 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

Forming the reduced matrix C is a stable procedure. However it involves implicit multiplication by B^{-1} if $(\mathbf{comp_type} = \text{Nag_Compute_1})$ or B (if $\mathbf{comp_type} = \text{Nag_Compute_2}$ or Nag_Compute_3). When `nag_zhpgst` (f08tsc) is used as a step in the computation of eigenvalues and eigenvectors of the original problem, there may be a significant loss of accuracy if B is ill-conditioned with respect to inversion.

8 Parallelism and Performance

`nag_zhpgst` (f08tsc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

The total number of real floating-point operations is approximately $4n^3$.

The real analogue of this function is `nag_dspgst` (f08tec).

10 Example

This example computes all the eigenvalues of $Az = \lambda Bz$, where

$$A = \begin{pmatrix} -7.36 + 0.00i & 0.77 - 0.43i & -0.64 - 0.92i & 3.01 - 6.97i \\ 0.77 + 0.43i & 3.49 + 0.00i & 2.19 + 4.45i & 1.90 + 3.73i \\ -0.64 + 0.92i & 2.19 - 4.45i & 0.12 + 0.00i & 2.88 - 3.17i \\ 3.01 + 6.97i & 1.90 - 3.73i & 2.88 + 3.17i & -2.54 + 0.00i \end{pmatrix}$$

and

$$B = \begin{pmatrix} 3.23 + 0.00i & 1.51 - 1.92i & 1.90 + 0.84i & 0.42 + 2.50i \\ 1.51 + 1.92i & 3.58 + 0.00i & -0.23 + 1.11i & -1.18 + 1.37i \\ 1.90 - 0.84i & -0.23 - 1.11i & 4.09 + 0.00i & 2.33 - 0.14i \\ 0.42 - 2.50i & -1.18 - 1.37i & 2.33 + 0.14i & 4.29 + 0.00i \end{pmatrix},$$

using packed storage. Here B is Hermitian positive definite and must first be factorized by nag_zpptrf (f07grc). The program calls nag_zhpgst (f08tsc) to reduce the problem to the standard form $Cy = \lambda y$; then nag_zhptrd (f08gsc) to reduce C to tridiagonal form, and nag_dsterf (f08jfc) to compute the eigenvalues.

10.1 Program Text

```
/* nag_zhpgst (f08tsc) Example Program.
*
* NAGPRODCODE Version.
*
* Copyright 2016 Numerical Algorithms Group.
*
* Mark 26, 2016.
*/
#include <stdio.h>
#include <nag.h>
#include <nag_stlib.h>
#include <nagf07.h>
#include <nagf08.h>

int main(void)
{
    /* Scalars */
    Integer i, j, n, ap_len, bp_len, d_len, e_len, tau_len;
    Integer exit_status = 0;
    NagError fail;
    Nag_UptoType uplo;
    Nag_OrderType order;

    /* Arrays */
    char nag_enum_arg[40];
    Complex *ap = 0, *bp = 0, *tau = 0;
    double *d = 0, *e = 0;

#ifdef NAG_COLUMN_MAJOR
#define A_UPPER(I, J) ap[J*(J-1)/2 + I - 1]
#define A_LOWER(I, J) ap[(2*n-J)*(J-1)/2 + I - 1]
#define B_UPPER(I, J) bp[J*(J-1)/2 + I - 1]
#define B_LOWER(I, J) bp[(2*n-J)*(J-1)/2 + I - 1]
    order = Nag_ColMajor;
#else
#define A_LOWER(I, J) ap[I*(I-1)/2 + J - 1]
#define A_UPPER(I, J) ap[(2*n-I)*(I-1)/2 + J - 1]
#define B_LOWER(I, J) bp[I*(I-1)/2 + J - 1]
#define B_UPPER(I, J) bp[(2*n-I)*(I-1)/2 + J - 1]
    order = Nag_RowMajor;
#endif
    INIT_FAIL(fail);

    /* Initialize arrays */
    if (nag_enum_arg[0] == 'C') {
        ap[0] = 3.23;
        ap[1] = 1.51;
        ap[2] = 1.90;
        ap[3] = 0.42;
        ap[4] = 1.51;
        ap[5] = 3.58;
        ap[6] = -0.23;
        ap[7] = -1.18;
        ap[8] = 1.90;
        ap[9] = -0.84;
        ap[10] = -0.23;
        ap[11] = 4.09;
        ap[12] = 2.33;
        ap[13] = 0.42;
        ap[14] = -2.50;
        ap[15] = -1.18;
        ap[16] = 2.33;
        ap[17] = 4.29;
        ap[18] = 0.0;
        ap[19] = 0.0;
        ap[20] = 0.0;
        ap[21] = 0.0;
        ap[22] = 0.0;
        ap[23] = 0.0;
        ap[24] = 0.0;
        ap[25] = 0.0;
        ap[26] = 0.0;
        ap[27] = 0.0;
        ap[28] = 0.0;
        ap[29] = 0.0;
        ap[30] = 0.0;
        ap[31] = 0.0;
        ap[32] = 0.0;
        ap[33] = 0.0;
        ap[34] = 0.0;
        ap[35] = 0.0;
        ap[36] = 0.0;
        ap[37] = 0.0;
        ap[38] = 0.0;
        ap[39] = 0.0;
        bp[0] = 1.51;
        bp[1] = 3.58;
        bp[2] = -0.23;
        bp[3] = -1.18;
        bp[4] = 1.90;
        bp[5] = -0.84;
        bp[6] = -0.23;
        bp[7] = 4.09;
        bp[8] = 2.33;
        bp[9] = 0.42;
        bp[10] = -2.50;
        bp[11] = -1.18;
        bp[12] = 2.33;
        bp[13] = 4.29;
        bp[14] = 0.0;
        bp[15] = 0.0;
        bp[16] = 0.0;
        bp[17] = 0.0;
        bp[18] = 0.0;
        bp[19] = 0.0;
        bp[20] = 0.0;
        bp[21] = 0.0;
        bp[22] = 0.0;
        bp[23] = 0.0;
        bp[24] = 0.0;
        bp[25] = 0.0;
        bp[26] = 0.0;
        bp[27] = 0.0;
        bp[28] = 0.0;
        bp[29] = 0.0;
        bp[30] = 0.0;
        bp[31] = 0.0;
        bp[32] = 0.0;
        bp[33] = 0.0;
        bp[34] = 0.0;
        bp[35] = 0.0;
        bp[36] = 0.0;
        bp[37] = 0.0;
        bp[38] = 0.0;
        bp[39] = 0.0;
        d[0] = 3.23;
        d[1] = 1.51;
        d[2] = 1.90;
        d[3] = 0.42;
        d[4] = 1.51;
        d[5] = 3.58;
        d[6] = -0.23;
        d[7] = -1.18;
        d[8] = 1.90;
        d[9] = -0.84;
        d[10] = -0.23;
        d[11] = 4.09;
        d[12] = 2.33;
        d[13] = 0.42;
        d[14] = -2.50;
        d[15] = -1.18;
        d[16] = 2.33;
        d[17] = 4.29;
        d[18] = 0.0;
        d[19] = 0.0;
        d[20] = 0.0;
        d[21] = 0.0;
        d[22] = 0.0;
        d[23] = 0.0;
        d[24] = 0.0;
        d[25] = 0.0;
        d[26] = 0.0;
        d[27] = 0.0;
        d[28] = 0.0;
        d[29] = 0.0;
        d[30] = 0.0;
        d[31] = 0.0;
        d[32] = 0.0;
        d[33] = 0.0;
        d[34] = 0.0;
        d[35] = 0.0;
        d[36] = 0.0;
        d[37] = 0.0;
        d[38] = 0.0;
        d[39] = 0.0;
        e[0] = 1.51;
        e[1] = 3.58;
        e[2] = -0.23;
        e[3] = -1.18;
        e[4] = 1.90;
        e[5] = -0.84;
        e[6] = -0.23;
        e[7] = 4.09;
        e[8] = 2.33;
        e[9] = 0.42;
        e[10] = -2.50;
        e[11] = -1.18;
        e[12] = 2.33;
        e[13] = 4.29;
        e[14] = 0.0;
        e[15] = 0.0;
        e[16] = 0.0;
        e[17] = 0.0;
        e[18] = 0.0;
        e[19] = 0.0;
        e[20] = 0.0;
        e[21] = 0.0;
        e[22] = 0.0;
        e[23] = 0.0;
        e[24] = 0.0;
        e[25] = 0.0;
        e[26] = 0.0;
        e[27] = 0.0;
        e[28] = 0.0;
        e[29] = 0.0;
        e[30] = 0.0;
        e[31] = 0.0;
        e[32] = 0.0;
        e[33] = 0.0;
        e[34] = 0.0;
        e[35] = 0.0;
        e[36] = 0.0;
        e[37] = 0.0;
        e[38] = 0.0;
        e[39] = 0.0;
    }
    else {
        ap[0] = 3.23;
        ap[1] = 1.51;
        ap[2] = 1.90;
        ap[3] = 0.42;
        ap[4] = 1.51;
        ap[5] = 3.58;
        ap[6] = -0.23;
        ap[7] = -1.18;
        ap[8] = 1.90;
        ap[9] = -0.84;
        ap[10] = -0.23;
        ap[11] = 4.09;
        ap[12] = 2.33;
        ap[13] = 0.42;
        ap[14] = -2.50;
        ap[15] = -1.18;
        ap[16] = 2.33;
        ap[17] = 4.29;
        ap[18] = 0.0;
        ap[19] = 0.0;
        ap[20] = 0.0;
        ap[21] = 0.0;
        ap[22] = 0.0;
        ap[23] = 0.0;
        ap[24] = 0.0;
        ap[25] = 0.0;
        ap[26] = 0.0;
        ap[27] = 0.0;
        ap[28] = 0.0;
        ap[29] = 0.0;
        ap[30] = 0.0;
        ap[31] = 0.0;
        ap[32] = 0.0;
        ap[33] = 0.0;
        ap[34] = 0.0;
        ap[35] = 0.0;
        ap[36] = 0.0;
        ap[37] = 0.0;
        ap[38] = 0.0;
        ap[39] = 0.0;
        bp[0] = 1.51;
        bp[1] = 3.58;
        bp[2] = -0.23;
        bp[3] = -1.18;
        bp[4] = 1.90;
        bp[5] = -0.84;
        bp[6] = -0.23;
        bp[7] = 4.09;
        bp[8] = 2.33;
        bp[9] = 0.42;
        bp[10] = -2.50;
        bp[11] = -1.18;
        bp[12] = 2.33;
        bp[13] = 4.29;
        bp[14] = 0.0;
        bp[15] = 0.0;
        bp[16] = 0.0;
        bp[17] = 0.0;
        bp[18] = 0.0;
        bp[19] = 0.0;
        bp[20] = 0.0;
        bp[21] = 0.0;
        bp[22] = 0.0;
        bp[23] = 0.0;
        bp[24] = 0.0;
        bp[25] = 0.0;
        bp[26] = 0.0;
        bp[27] = 0.0;
        bp[28] = 0.0;
        bp[29] = 0.0;
        bp[30] = 0.0;
        bp[31] = 0.0;
        bp[32] = 0.0;
        bp[33] = 0.0;
        bp[34] = 0.0;
        bp[35] = 0.0;
        bp[36] = 0.0;
        bp[37] = 0.0;
        bp[38] = 0.0;
        bp[39] = 0.0;
        d[0] = 3.23;
        d[1] = 1.51;
        d[2] = 1.90;
        d[3] = 0.42;
        d[4] = 1.51;
        d[5] = 3.58;
        d[6] = -0.23;
        d[7] = -1.18;
        d[8] = 1.90;
        d[9] = -0.84;
        d[10] = -0.23;
        d[11] = 4.09;
        d[12] = 2.33;
        d[13] = 0.42;
        d[14] = -2.50;
        d[15] = -1.18;
        d[16] = 2.33;
        d[17] = 4.29;
        d[18] = 0.0;
        d[19] = 0.0;
        d[20] = 0.0;
        d[21] = 0.0;
        d[22] = 0.0;
        d[23] = 0.0;
        d[24] = 0.0;
        d[25] = 0.0;
        d[26] = 0.0;
        d[27] = 0.0;
        d[28] = 0.0;
        d[29] = 0.0;
        d[30] = 0.0;
        d[31] = 0.0;
        d[32] = 0.0;
        d[33] = 0.0;
        d[34] = 0.0;
        d[35] = 0.0;
        d[36] = 0.0;
        d[37] = 0.0;
        d[38] = 0.0;
        d[39] = 0.0;
        e[0] = 1.51;
        e[1] = 3.58;
        e[2] = -0.23;
        e[3] = -1.18;
        e[4] = 1.90;
        e[5] = -0.84;
        e[6] = -0.23;
        e[7] = 4.09;
        e[8] = 2.33;
        e[9] = 0.42;
        e[10] = -2.50;
        e[11] = -1.18;
        e[12] = 2.33;
        e[13] = 4.29;
        e[14] = 0.0;
        e[15] = 0.0;
        e[16] = 0.0;
        e[17] = 0.0;
        e[18] = 0.0;
        e[19] = 0.0;
        e[20] = 0.0;
        e[21] = 0.0;
        e[22] = 0.0;
        e[23] = 0.0;
        e[24] = 0.0;
        e[25] = 0.0;
        e[26] = 0.0;
        e[27] = 0.0;
        e[28] = 0.0;
        e[29] = 0.0;
        e[30] = 0.0;
        e[31] = 0.0;
        e[32] = 0.0;
        e[33] = 0.0;
        e[34] = 0.0;
        e[35] = 0.0;
        e[36] = 0.0;
        e[37] = 0.0;
        e[38] = 0.0;
        e[39] = 0.0;
    }

    /* Compute eigenvalues */
    if (nag_enum_arg[0] == 'V') {
        if (nagf08tsc(&nag_enum_arg[1], &n, &uplo, &order, &ap, &bp, &d, &e, &tau, &i, &j, &exit_status, &fail) != Nag_SuccExit) {
            printf("Error from nagf08tsc\n");
            exit(-1);
        }
    }
    else {
        if (nagf08tsc(&nag_enum_arg[1], &n, &uplo, &order, &ap, &bp, &d, &e, &tau, &i, &j, &exit_status, &fail) != Nag_SuccExit) {
            printf("Error from nagf08tsc\n");
            exit(-1);
        }
    }

    /* Print eigenvalues */
    if (nag_enum_arg[0] == 'V') {
        printf("Eigenvalues\n");
        for (i = 0; i < n; i++) {
            printf("%12.4f %12.4fi\n", d[i], e[i]);
        }
    }
    else {
        printf("Eigenvalues\n");
        for (i = 0; i < n; i++) {
            printf("%12.4f %12.4fi\n", d[i], e[i]);
        }
    }

    /* Free memory */
    if (nag_enum_arg[0] == 'V') {
        if (nagf08gsc(&n, &uplo, &ap, &bp, &tau, &i, &j, &exit_status, &fail) != Nag_SuccExit) {
            printf("Error from nagf08gsc\n");
            exit(-1);
        }
    }
    else {
        if (nagf08gsc(&n, &uplo, &ap, &bp, &tau, &i, &j, &exit_status, &fail) != Nag_SuccExit) {
            printf("Error from nagf08gsc\n");
            exit(-1);
        }
    }

    /* Print eigenvalues */
    if (nag_enum_arg[0] == 'V') {
        printf("Eigenvalues\n");
        for (i = 0; i < n; i++) {
            printf("%12.4f %12.4fi\n", d[i], e[i]);
        }
    }
    else {
        printf("Eigenvalues\n");
        for (i = 0; i < n; i++) {
            printf("%12.4f %12.4fi\n", d[i], e[i]);
        }
    }

    /* Free memory */
    if (nag_enum_arg[0] == 'V') {
        if (nagf08jfc(&n, &order, &d, &e, &tau, &exit_status, &fail) != Nag_SuccExit) {
            printf("Error from nagf08jfc\n");
            exit(-1);
        }
    }
    else {
        if (nagf08jfc(&n, &order, &d, &e, &tau, &exit_status, &fail) != Nag_SuccExit) {
            printf("Error from nagf08jfc\n");
            exit(-1);
        }
    }

    /* Print eigenvalues */
    if (nag_enum_arg[0] == 'V') {
        printf("Eigenvalues\n");
        for (i = 0; i < n; i++) {
            printf("%12.4f %12.4fi\n", d[i], e[i]);
        }
    }
    else {
        printf("Eigenvalues\n");
        for (i = 0; i < n; i++) {
            printf("%12.4f %12.4fi\n", d[i], e[i]);
        }
    }

    /* Exit successfully */
    exit(0);
}
```

```

printf("nag_zhpgst (f08tsc) Example Program Results\n\n");

/* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[^\n] ");
#else
    scanf("%*[^\n] ");
#endif
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%*[^\n] ", &n);
#else
    scanf("%" NAG_IFMT "%*[^\n] ", &n);
#endif
ap_len = n * (n + 1) / 2;
bp_len = n * (n + 1) / 2;
d_len = n;
e_len = n - 1;
tau_len = n;

/* Allocate memory */
if (!(ap = NAG_ALLOC(ap_len, Complex)) ||
    !(bp = NAG_ALLOC(bp_len, Complex)) ||
    !(d = NAG_ALLOC(d_len, double)) ||
    !(e = NAG_ALLOC(e_len, double)) || !(tau = NAG_ALLOC(tau_len, Complex)))
{
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
}

/* Read A and B from data file */
#ifdef _WIN32
    scanf_s("%39s%*[^\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s%*[^\n] ", nag_enum_arg);
#endif
/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
uplo = (Nag_UptoType) nag_enum_name_to_value(nag_enum_arg);
if (uplo == Nag_Upper) {
    for (i = 1; i <= n; ++i) {
        for (j = i; j <= n; ++j) {
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A_UPPER(i, j).re, &A_UPPER(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A_UPPER(i, j).re, &A_UPPER(i, j).im);
#endif
        }
    }
}
#ifdef _WIN32
    scanf_s("%*[^\n] ");
#else
    scanf("%*[^\n] ");
#endif
    for (i = 1; i <= n; ++i) {
        for (j = i; j <= n; ++j) {
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &B_UPPER(i, j).re, &B_UPPER(i, j).im);
#else
            scanf(" ( %lf , %lf )", &B_UPPER(i, j).re, &B_UPPER(i, j).im);
#endif
        }
    }
}
#ifdef _WIN32
    scanf_s("%*[^\n] ");
#else
    scanf("%*[^\n] ");
#endif
}
else {

```

```

    for (i = 1; i <= n; ++i) {
        for (j = 1; j <= i; ++j) {
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A_LOWER(i, j).re, &A_LOWER(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A_LOWER(i, j).re, &A_LOWER(i, j).im);
#endif
        }
    }
#endif _WIN32
    scanf_s("%*[^\n] ");
#else
    scanf("%*[^\n] ");
#endif
    for (i = 1; i <= n; ++i) {
        for (j = 1; j <= i; ++j) {
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &B_LOWER(i, j).re, &B_LOWER(i, j).im);
#else
            scanf(" ( %lf , %lf )", &B_LOWER(i, j).re, &B_LOWER(i, j).im);
#endif
        }
    }
#endif _WIN32
    scanf_s("%*[^\n] ");
#else
    scanf("%*[^\n] ");
#endif
}
/* Compute the Cholesky factorization of B */
/* nag_zpptrf (f07grc).
 * Cholesky factorization of complex Hermitian
 * positive-definite matrix, packed storage
 */
nag_zpptrf(order, uplo, n, bp, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_dpptrf (f07gdc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Reduce the problem to standard form C*y = lambda*y, storing */
/* the result in A */
/* nag_zhpgst (f08tsc).
 * Reduction to standard form of complex Hermitian-definite
 * generalized eigenproblem Ax = lambda Bx, ABx = lambda x
 * or BAx = lambda x, packed storage, B factorized by
 * nag_zpptrf (f07grc)
 */
nag_zhpgst(order, Nag_Compute_1, uplo, n, ap, bp, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_zhpgst (f08tsc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Reduce C to tridiagonal form T = (Q^T)*C*Q */
/* nag_zhptrd (f08gsc).
 * Unitary reduction of complex Hermitian matrix to real
 * symmetric tridiagonal form, packed storage
 */
nag_zhptrd(order, uplo, n, ap, d, e, tau, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_zhptrd (f08gsc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Calculate the eigenvalues of T (same as C) */
/* nag_dsterf (f08jfc).
 * All eigenvalues of real symmetric tridiagonal matrix,
 * root-free variant of QL or QR
 */
nag_dsterf(n, d, e, &fail);

```

```

if (fail.code != NE_NOERROR) {
    printf("Error from nag_dsterf (f08jfc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Print eigenvalues */
printf("Eigenvalues\n");
for (i = 1; i <= n; ++i)
    printf("%8.4f%s", d[i - 1], i % 9 == 0 || i == n ? "\n" : " ");
printf("\n");
END:
NAG_FREE(ap);
NAG_FREE(bp);
NAG_FREE(d);
NAG_FREE(e);
NAG_FREE(tau);

return exit_status;
}

```

10.2 Program Data

```

nag_zhpgst (f08tsc) Example Program Data
 4                                     :Value of n
 Nag_Lower                            :Value of uplo
 (-7.36, 0.00)
 ( 0.77, 0.43) ( 3.49, 0.00)
 (-0.64, 0.92) ( 2.19,-4.45) ( 0.12, 0.00)
 ( 3.01, 6.97) ( 1.90,-3.73) ( 2.88, 3.17) (-2.54, 0.00) :End of matrix A
 ( 3.23, 0.00)
 ( 1.51, 1.92) ( 3.58, 0.00)
 ( 1.90,-0.84) (-0.23,-1.11) ( 4.09, 0.00)
 ( 0.42,-2.50) (-1.18,-1.37) ( 2.33, 0.14) ( 4.29, 0.00) :End of matrix B

```

10.3 Program Results

```

nag_zhpgst (f08tsc) Example Program Results
Eigenvalues
-5.9990   -2.9936    0.5047    3.9990

```
