

# NAG Library Function Document

## nag\_zhesvx (f07mpc)

### 1 Purpose

nag\_zhesvx (f07mpc) uses the diagonal pivoting factorization to compute the solution to a complex system of linear equations

$$AX = B,$$

where  $A$  is an  $n$  by  $n$  Hermitian matrix and  $X$  and  $B$  are  $n$  by  $r$  matrices. Error bounds on the solution and a condition estimate are also provided.

### 2 Specification

```
#include <nag.h>
#include <nagf07.h>

void nag_zhesvx (Nag_OrderType order, Nag_FactoredFormType fact,
                Nag_UploType uplo, Integer n, Integer nrhs, const Complex a[],
                Integer pda, Complex af[], Integer pdaf, Integer ipiv[],
                const Complex b[], Integer pdb, Complex x[], Integer pdx, double *rcond,
                double ferr[], double berr[], NagError *fail)
```

### 3 Description

nag\_zhesvx (f07mpc) performs the following steps:

1. If **fact** = Nag\_NotFactored, the diagonal pivoting method is used to factor  $A$ . The form of the factorization is  $A = UDU^H$  if **uplo** = Nag\_Upper or  $A = LDL^H$  if **uplo** = Nag\_Lower, where  $U$  (or  $L$ ) is a product of permutation and unit upper (lower) triangular matrices, and  $D$  is Hermitian and block diagonal with 1 by 1 and 2 by 2 diagonal blocks.
2. If some  $d_{ii} = 0$ , so that  $D$  is exactly singular, then the function returns with **fail.errnum** =  $i$  and **fail.code** = NE\_SINGULAR. Otherwise, the factored form of  $A$  is used to estimate the condition number of the matrix  $A$ . If the reciprocal of the condition number is less than *machine precision*, **fail.code** = NE\_SINGULAR\_WP is returned as a warning, but the function still goes on to solve for  $X$  and compute error bounds as described below.
3. The system of equations is solved for  $X$  using the factored form of  $A$ .
4. Iterative refinement is applied to improve the computed solution matrix and to calculate error bounds and backward error estimates for it.

### 4 References

Anderson E, Bai Z, Bischof C, Blackford S, Demmel J, Dongarra J J, Du Croz J J, Greenbaum A, Hammarling S, McKenney A and Sorensen D (1999) *LAPACK Users' Guide* (3rd Edition) SIAM, Philadelphia <http://www.netlib.org/lapack/lug>

Golub G H and Van Loan C F (1996) *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

Higham N J (2002) *Accuracy and Stability of Numerical Algorithms* (2nd Edition) SIAM, Philadelphia

## 5 Arguments

- 1: **order** – Nag\_OrderType *Input*  
*On entry:* the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag\_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.  
*Constraint:* **order** = Nag\_RowMajor or Nag\_ColMajor.
- 2: **fact** – Nag\_FactoredFormType *Input*  
*On entry:* specifies whether or not the factorized form of the matrix  $A$  has been supplied.  
**fact** = Nag\_Factored  
**af** and **ipiv** contain the factorized form of the matrix  $A$ . **af** and **ipiv** will not be modified.  
**fact** = Nag\_NotFactored  
The matrix  $A$  will be copied to **af** and factorized.  
*Constraint:* **fact** = Nag\_Factored or Nag\_NotFactored.
- 3: **uplo** – Nag\_UploType *Input*  
*On entry:* if **uplo** = Nag\_Upper, the upper triangle of  $A$  is stored.  
If **uplo** = Nag\_Lower, the lower triangle of  $A$  is stored.  
*Constraint:* **uplo** = Nag\_Upper or Nag\_Lower.
- 4: **n** – Integer *Input*  
*On entry:*  $n$ , the number of linear equations, i.e., the order of the matrix  $A$ .  
*Constraint:*  $n \geq 0$ .
- 5: **nrhs** – Integer *Input*  
*On entry:*  $r$ , the number of right-hand sides, i.e., the number of columns of the matrix  $B$ .  
*Constraint:* **nrhs**  $\geq 0$ .
- 6: **a**[*dim*] – const Complex *Input*  
**Note:** the dimension, *dim*, of the array **a** must be at least  $\max(1, \mathbf{pda} \times \mathbf{n})$ .  
*On entry:* the  $n$  by  $n$  Hermitian matrix  $A$ .  
If **order** = Nag\_ColMajor,  $A_{ij}$  is stored in **a**[( $j - 1$ )  $\times$  **pda** +  $i - 1$ ].  
If **order** = Nag\_RowMajor,  $A_{ij}$  is stored in **a**[( $i - 1$ )  $\times$  **pda** +  $j - 1$ ].  
If **uplo** = Nag\_Upper, the upper triangular part of  $A$  must be stored and the elements of the array below the diagonal are not referenced.  
If **uplo** = Nag\_Lower, the lower triangular part of  $A$  must be stored and the elements of the array above the diagonal are not referenced.
- 7: **pda** – Integer *Input*  
*On entry:* the stride separating row or column elements (depending on the value of **order**) of the matrix  $A$  in the array **a**.  
*Constraint:* **pda**  $\geq \max(1, \mathbf{n})$ .
- 8: **af**[*dim*] – Complex *Input/Output*  
**Note:** the dimension, *dim*, of the array **af** must be at least  $\max(1, \mathbf{pdaf} \times \mathbf{n})$ .

The  $(i, j)$ th element of the matrix is stored in

$\mathbf{af}[(j-1) \times \mathbf{pdaf} + i - 1]$  when **order** = Nag\_ColMajor;  
 $\mathbf{af}[(i-1) \times \mathbf{pdaf} + j - 1]$  when **order** = Nag\_RowMajor.

*On entry:* if **fact** = Nag\_Factored, **af** contains the block diagonal matrix  $D$  and the multipliers used to obtain the factor  $U$  or  $L$  from the factorization  $\mathbf{a} = UDU^H$  or  $\mathbf{a} = LDL^H$  as computed by nag\_zhetrf (f07mrc).

*On exit:* if **fact** = Nag\_NotFactored, **af** returns the block diagonal matrix  $D$  and the multipliers used to obtain the factor  $U$  or  $L$  from the factorization  $\mathbf{a} = UDU^H$  or  $\mathbf{a} = LDL^H$ .

9: **pdaf** – Integer *Input*

*On entry:* the stride separating row or column elements (depending on the value of **order**) of the matrix  $A$  in the array **af**.

*Constraint:*  $\mathbf{pdaf} \geq \max(1, \mathbf{n})$ .

10: **ipiv**[*dim*] – Integer *Input/Output*

**Note:** the dimension, *dim*, of the array **ipiv** must be at least  $\max(1, \mathbf{n})$ .

*On entry:* if **fact** = Nag\_Factored, **ipiv** contains details of the interchanges and the block structure of  $D$ , as determined by nag\_zhetrf (f07mrc).

if  $\mathbf{ipiv}[i-1] = k > 0$ ,  $d_{ii}$  is a 1 by 1 pivot block and the  $i$ th row and column of  $A$  were interchanged with the  $k$ th row and column;

if **uplo** = Nag\_Upper and  $\mathbf{ipiv}[i-2] = \mathbf{ipiv}[i-1] = -l < 0$ ,  $\begin{pmatrix} d_{i-1,i-1} & \bar{d}_{i,i-1} \\ \bar{d}_{i,i-1} & d_{ii} \end{pmatrix}$  is a 2 by 2 pivot block and the  $(i-1)$ th row and column of  $A$  were interchanged with the  $l$ th row and column;

if **uplo** = Nag\_Lower and  $\mathbf{ipiv}[i-1] = \mathbf{ipiv}[i] = -m < 0$ ,  $\begin{pmatrix} d_{ii} & d_{i+1,i} \\ d_{i+1,i} & d_{i+1,i+1} \end{pmatrix}$  is a 2 by 2 pivot block and the  $(i+1)$ th row and column of  $A$  were interchanged with the  $m$ th row and column.

*On exit:* if **fact** = Nag\_NotFactored, **ipiv** contains details of the interchanges and the block structure of  $D$ , as determined by nag\_zhetrf (f07mrc), as described above.

11: **b**[*dim*] – const Complex *Input*

**Note:** the dimension, *dim*, of the array **b** must be at least

$\max(1, \mathbf{pdb} \times \mathbf{nrhs})$  when **order** = Nag\_ColMajor;  
 $\max(1, \mathbf{n} \times \mathbf{pdb})$  when **order** = Nag\_RowMajor.

The  $(i, j)$ th element of the matrix  $B$  is stored in

$\mathbf{b}[(j-1) \times \mathbf{pdb} + i - 1]$  when **order** = Nag\_ColMajor;  
 $\mathbf{b}[(i-1) \times \mathbf{pdb} + j - 1]$  when **order** = Nag\_RowMajor.

*On entry:* the  $n$  by  $r$  right-hand side matrix  $B$ .

12: **pdb** – Integer *Input*

*On entry:* the stride separating row or column elements (depending on the value of **order**) in the array **b**.

*Constraints:*

if **order** = Nag\_ColMajor,  $\mathbf{pdb} \geq \max(1, \mathbf{n})$ ;  
 if **order** = Nag\_RowMajor,  $\mathbf{pdb} \geq \max(1, \mathbf{nrhs})$ .

13: **x**[*dim*] – Complex *Output*

**Note:** the dimension, *dim*, of the array **x** must be at least

$\max(1, \mathbf{pdx} \times \mathbf{nrhs})$  when **order** = Nag\_ColMajor;  
 $\max(1, \mathbf{n} \times \mathbf{pdx})$  when **order** = Nag\_RowMajor.

The (*i*, *j*)th element of the matrix *X* is stored in

**x**[(*j* – 1) × **pdx** + *i* – 1] when **order** = Nag\_ColMajor;  
**x**[(*i* – 1) × **pdx** + *j* – 1] when **order** = Nag\_RowMajor.

*On exit:* if **fail.code** = NE\_NOERROR or NE\_SINGULAR\_WP, the *n* by *r* solution matrix *X*.

14: **pdx** – Integer *Input*

*On entry:* the stride separating row or column elements (depending on the value of **order**) in the array **x**.

*Constraints:*

if **order** = Nag\_ColMajor, **pdx** ≥ max(1, **n**);  
 if **order** = Nag\_RowMajor, **pdx** ≥ max(1, **nrhs**).

15: **rcond** – double \* *Output*

*On exit:* the estimate of the reciprocal condition number of the matrix *A*. If **rcond** = 0.0, the matrix may be exactly singular. This condition is indicated by **fail.code** = NE\_SINGULAR. Otherwise, if **rcond** is less than the *machine precision*, the matrix is singular to working precision. This condition is indicated by **fail.code** = NE\_SINGULAR\_WP.

16: **ferr**[*dim*] – double *Output*

**Note:** the dimension, *dim*, of the array **ferr** must be at least max(1, **nrhs**).

*On exit:* if **fail.code** = NE\_NOERROR or NE\_SINGULAR\_WP, an estimate of the forward error bound for each computed solution vector, such that  $\|\hat{x}_j - x_j\|_\infty / \|x_j\|_\infty \leq \mathbf{ferr}[j - 1]$  where  $\hat{x}_j$  is the *j*th column of the computed solution returned in the array **x** and  $x_j$  is the corresponding column of the exact solution *X*. The estimate is as reliable as the estimate for **rcond**, and is almost always a slight overestimate of the true error.

17: **berr**[*dim*] – double *Output*

**Note:** the dimension, *dim*, of the array **berr** must be at least max(1, **nrhs**).

*On exit:* if **fail.code** = NE\_NOERROR or NE\_SINGULAR\_WP, an estimate of the component-wise relative backward error of each computed solution vector  $\hat{x}_j$  (i.e., the smallest relative change in any element of *A* or *B* that makes  $\hat{x}_j$  an exact solution).

18: **fail** – NagError \* *Input/Output*

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in How to Use the NAG Library and its Documentation for further information.

### NE\_BAD\_PARAM

On entry, argument *<value>* had an illegal value.

**NE\_INT**

On entry, **n** =  $\langle value \rangle$ .

Constraint: **n**  $\geq 0$ .

On entry, **nrhs** =  $\langle value \rangle$ .

Constraint: **nrhs**  $\geq 0$ .

On entry, **pda** =  $\langle value \rangle$ .

Constraint: **pda**  $> 0$ .

On entry, **pdaf** =  $\langle value \rangle$ .

Constraint: **pdaf**  $> 0$ .

On entry, **pdb** =  $\langle value \rangle$ .

Constraint: **pdb**  $> 0$ .

On entry, **pdx** =  $\langle value \rangle$ .

Constraint: **pdx**  $> 0$ .

**NE\_INT\_2**

On entry, **pda** =  $\langle value \rangle$  and **n** =  $\langle value \rangle$ .

Constraint: **pda**  $\geq \max(1, \mathbf{n})$ .

On entry, **pdaf** =  $\langle value \rangle$  and **n** =  $\langle value \rangle$ .

Constraint: **pdaf**  $\geq \max(1, \mathbf{n})$ .

On entry, **pdb** =  $\langle value \rangle$  and **n** =  $\langle value \rangle$ .

Constraint: **pdb**  $\geq \max(1, \mathbf{n})$ .

On entry, **pdb** =  $\langle value \rangle$  and **nrhs** =  $\langle value \rangle$ .

Constraint: **pdb**  $\geq \max(1, \mathbf{nrhs})$ .

On entry, **pdx** =  $\langle value \rangle$  and **n** =  $\langle value \rangle$ .

Constraint: **pdx**  $\geq \max(1, \mathbf{n})$ .

On entry, **pdx** =  $\langle value \rangle$  and **nrhs** =  $\langle value \rangle$ .

Constraint: **pdx**  $\geq \max(1, \mathbf{nrhs})$ .

**NE\_INTERNAL\_ERROR**

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in How to Use the NAG Library and its Documentation for further information.

**NE\_NO\_LICENCE**

Your licence key may have expired or may not have been installed correctly.

See Section 3.6.5 in How to Use the NAG Library and its Documentation for further information.

**NE\_SINGULAR**

Element  $\langle value \rangle$  of the diagonal is exactly zero. The factorization has been completed, but the factor  $D$  is exactly singular, so the solution and error bounds could not be computed. **rcond** = 0.0 is returned.

**NE\_SINGULAR\_WP**

$D$  is nonsingular, but **rcond** is less than *machine precision*, meaning that the matrix is singular to working precision. Nevertheless, the solution and error bounds are computed because there are a number of situations where the computed solution can be more accurate than the value of **rcond** would suggest.

## 7 Accuracy

For each right-hand side vector  $b$ , the computed solution  $\hat{x}$  is the exact solution of a perturbed system of equations  $(A + E)\hat{x} = b$ , where

$$\|E\|_1 = O(\epsilon)\|A\|_1,$$

where  $\epsilon$  is the *machine precision*. See Chapter 11 of Higham (2002) for further details.

If  $\hat{x}$  is the true solution, then the computed solution  $x$  satisfies a forward error bound of the form

$$\frac{\|x - \hat{x}\|_\infty}{\|\hat{x}\|_\infty} \leq w_c \text{cond}(A, \hat{x}, b)$$

where  $\text{cond}(A, \hat{x}, b) = \frac{\| |A^{-1}|(|A\|\hat{x}\| + |b|)\|_\infty}{\|\hat{x}\|_\infty} \leq \text{cond}(A) = \| |A^{-1}| |A| \|_\infty \leq \kappa_\infty(A)$ . If  $\hat{x}$  is the  $j$ th column of  $X$ , then  $w_c$  is returned in **herr**[ $j - 1$ ] and a bound on  $\|x - \hat{x}\|_\infty / \|\hat{x}\|_\infty$  is returned in **ferr**[ $j - 1$ ]. See Section 4.4 of Anderson *et al.* (1999) for further details.

## 8 Parallelism and Performance

nag\_zhesvx (f07mpc) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

nag\_zhesvx (f07mpc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

## 9 Further Comments

The factorization of  $A$  requires approximately  $\frac{4}{3}n^3$  floating-point operations.

For each right-hand side, computation of the backward error involves a minimum of  $16n^2$  floating-point operations. Each step of iterative refinement involves an additional  $24n^2$  operations. At most five steps of iterative refinement are performed, but usually only one or two steps are required. Estimating the forward error involves solving a number of systems of equations of the form  $Ax = b$ ; the number is usually 4 or 5 and never more than 11. Each solution involves approximately  $8n^2$  operations.

The real analogue of this function is nag\_dsylvx (f07mbe). The complex symmetric analogue of this function is nag\_zsysvx (f07npc).

## 10 Example

This example solves the equations

$$AX = B,$$

where  $A$  is the Hermitian matrix

$$A = \begin{pmatrix} -1.84 & 0.11 - 0.11i & -1.78 - 1.18i & 3.91 - 1.50i \\ 0.11 + 0.11i & -4.63 & -1.84 + 0.03i & 2.21 + 0.21i \\ -1.78 + 1.18i & -1.84 - 0.03i & -8.87 & 1.58 - 0.90i \\ 3.91 + 1.50i & 2.21 - 0.21i & 1.58 + 0.90i & -1.36 \end{pmatrix}$$

and

$$B = \begin{pmatrix} 2.98 - 10.18i & 28.68 - 39.89i \\ -9.58 + 3.88i & -24.79 - 8.40i \\ -0.77 - 16.05i & 4.23 - 70.02i \\ 7.79 + 5.48i & -35.39 + 18.01i \end{pmatrix}.$$

Error estimates for the solutions, and an estimate of the reciprocal of the condition number of the matrix  $A$  are also output.

## 10.1 Program Text

```

/* nag_zhesvx (f07mpc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <stdio.h>
#include <nag.h>
#include <nagx04.h>
#include <nag_stdlib.h>
#include <nagf07.h>

int main(void)
{
    /* Scalars */
    double rcond;
    Integer exit_status = 0, i, j, n, nrhs, pda, pdaf, pdb, pdx;

    /* Arrays */
    Complex *a = 0, *af = 0, *b = 0, *x = 0;
    double *berr = 0, *ferr = 0;
    Integer *ipiv = 0;
    char nag_enum_arg[40];

    /* Nag Types */
    NagError fail;
    Nag_UploType uplo;
    Nag_OrderType order;

#ifdef NAG_COLUMN_MAJOR
#define A(I, J) a[(J-1)*pda + I - 1]
#define B(I, J) b[(J-1)*pdb + I - 1]
    order = Nag_ColMajor;
#else
#define A(I, J) a[(I-1)*pda + J - 1]
#define B(I, J) b[(I-1)*pdb + J - 1]
    order = Nag_RowMajor;
#endif

    INIT_FAIL(fail);

    printf("nag_zhesvx (f07mpc) Example Program Results\n\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n]");
#else
    scanf("%*[\n]");
#endif
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%" NAG_IFMT "%*[\n]", &n, &nrhs);
#else
    scanf("%" NAG_IFMT "%" NAG_IFMT "%*[\n]", &n, &nrhs);
#endif
    if (n < 0 || nrhs < 0) {
        printf("Invalid n or nrhs\n");
        exit_status = 1;
        goto END;
    }
#ifdef _WIN32
    scanf_s(" %39s%*[\n]", nag_enum_arg, (unsigned)_countof(nag_enum_arg));

```

```

#else
    scanf(" %39s%*[\n]", nag_enum_arg);
#endif
/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
uplo = (Nag_UploType) nag_enum_name_to_value(nag_enum_arg);

/* Allocate memory */
if (!(a = NAG_ALLOC(n * n, Complex)) ||
    !(af = NAG_ALLOC(n * n, Complex)) ||
    !(b = NAG_ALLOC(n * nrhs, Complex)) ||
    !(x = NAG_ALLOC(n * nrhs, Complex)) ||
    !(berr = NAG_ALLOC(nrhs, double)) ||
    !(ferr = NAG_ALLOC(nrhs, double)) || !(ipiv = NAG_ALLOC(n, Integer)))
{
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
}

pda = n;
pdaf = n;
#ifdef NAG_COLUMN_MAJOR
    pdb = n;
    pdx = n;
#else
    pdb = nrhs;
    pdx = nrhs;
#endif

/* Read the triangular part of A from data file */
if (uplo == Nag_Upper)
    for (i = 1; i <= n; ++i)
        for (j = i; j <= n; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#endif
else
    for (i = 1; i <= n; ++i)
        for (j = 1; j <= i; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#endif
#ifdef _WIN32
    scanf_s("%*[\n]");
#else
    scanf("%*[\n]");
#endif

/* Read B from data file */
for (i = 1; i <= n; ++i)
    for (j = 1; j <= nrhs; ++j)
#ifdef _WIN32
        scanf_s(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#else
        scanf(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#endif
#ifdef _WIN32
    scanf_s("%*[\n]");
#else
    scanf("%*[\n]");
#endif

/* Solve the equations AX = B for X using nag_zhesvx (f07mpc). */
nag_zhesvx(order, Nag_NotFactored, uplo, n, nrhs, a, pda, af, pdaf, ipiv,
           b, pdb, x, pdx, &rcond, ferr, berr, &fail);

```



```

if (fail.code != NE_NOERROR && fail.code != NE_SINGULAR) {
    printf("Error from nag_zhesvx (f07mpc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Print solution using nag_gen_complx_mat_print_comp (x04dbc). */
fflush(stdout);
nag_gen_complx_mat_print_comp(order, Nag_GeneralMatrix, Nag_NonUnitDiag, n,
                              nrhs, x, pdx, Nag_BracketForm, "%7.4f",
                              "Solution(s)", Nag_IntegerLabels, 0,
                              Nag_IntegerLabels, 0, 80, 0, 0, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_complx_mat_print_comp (x04dbc).\n%s\n",
          fail.message);
    exit_status = 1;
    goto END;
}

/* Print error bounds and condition number */
printf("\nBackward errors (machine-dependent)\n");
for (j = 0; j < nrhs; ++j)
    printf("%11.1e%s", berr[j], j % 7 == 6 ? "\n" : " ");

printf("\n\nEstimated forward error bounds (machine-dependent)\n");
for (j = 0; j < nrhs; ++j)
    printf("%11.1e%s", ferr[j], j % 7 == 6 ? "\n" : " ");

printf("\n\nEstimate of reciprocal condition number\n%11.1e\n\n", rcond);
if (fail.code == NE_SINGULAR) {
    printf("Error from nag_zhesvx (f07mpc).\n%s\n", fail.message);
    exit_status = 1;
}
}
END:
NAG_FREE(a);
NAG_FREE(af);
NAG_FREE(b);
NAG_FREE(x);
NAG_FREE(berr);
NAG_FREE(ferr);
NAG_FREE(ipiv);

return exit_status;
}

#undef B
#undef A

```

## 10.2 Program Data

```

nag_zhesvx (f07mpc) Example Program Data
  4          2          : n, nrhs
  Nag_Upper          : uplo
( -1.84,  0.00) (  0.11, -0.11) ( -1.78, -1.18) (  3.91, -1.50)
                   ( -4.63,  0.00) ( -1.84,  0.03) (  2.21,  0.21)
                   ( -8.87,  0.00) (  1.58, -0.90)
                                     ( -1.36,  0.00) : matrix A

(  2.98,-10.18) ( 28.68,-39.89)
( -9.58,  3.88) (-24.79, -8.40)
( -0.77,-16.05) (  4.23,-70.02)
(  7.79,  5.48) (-35.39, 18.01)          : matrix B

```

### 10.3 Program Results

nag\_zhesvx (f07mpc) Example Program Results

Solution(s)

	1	2
1	( 2.0000, 1.0000)	(-8.0000, 6.0000)
2	( 3.0000,-2.0000)	( 7.0000,-2.0000)
3	(-1.0000, 2.0000)	(-1.0000, 5.0000)
4	( 1.0000,-1.0000)	( 3.0000,-4.0000)

Backward errors (machine-dependent)

5.1e-17      5.9e-17

Estimated forward error bounds (machine-dependent)

2.5e-15      3.0e-15

Estimate of reciprocal condition number

1.5e-01

---