

# NAG Library Function Document

## nag\_monotonic\_intg (e01bhc)

### 1 Purpose

nag\_monotonic\_intg (e01bhc) evaluates the definite integral of a piecewise cubic Hermite interpolant over the interval  $[a, b]$ .

### 2 Specification

```
#include <nag.h>
#include <nage01.h>

void nag_monotonic_intg (Integer n, const double x[], const double f[],
                        const double d[], double a, double b, double *integral, NagError *fail)
```

### 3 Description

nag\_monotonic\_intg (e01bhc) evaluates the definite integral of a piecewise cubic Hermite interpolant, as computed by nag\_monotonic\_interpolant (e01bec), over the interval  $[a, b]$ .

If either  $a$  or  $b$  lies outside the interval from  $\mathbf{x}[0]$  to  $\mathbf{x}[n - 1]$ , computation of the integral involves extrapolation and a warning is returned.

The function is derived from routine PCHIA in Fritsch (1982).

### 4 References

Fritsch F N (1982) PCHIP final specifications *Report UCID-30194* Lawrence Livermore National Laboratory

### 5 Arguments

- |    |   |                     |
|----|---|---------------------|
| 1: | <b>n</b> – Integer  | <i>Input</i>        |
|    | <i>On entry:</i> <b>n</b> must be unchanged from the previous call of nag_monotonic_interpolant (e01bec).                         |                     |
| 2: | <b>x[n]</b> – const double  | <i>Input</i>        |
| 3: | <b>f[n]</b> – const double  | <i>Input</i>        |
| 4: | <b>d[n]</b> – const double  | <i>Input</i>        |
|    | <i>On entry:</i> <b>x</b> , <b>f</b> and <b>d</b> must be unchanged from the previous call of nag_monotonic_interpolant (e01bec). |                     |
| 5: | <b>a</b> – double   | <i>Input</i>        |
| 6: | <b>b</b> – double   | <i>Input</i>        |
|    | <i>On entry:</i> the interval $[a, b]$ over which integration is to be performed.   |                     |
| 7: | <b>integral</b> – double *  | <i>Output</i>       |
|    | <i>On exit:</i> the value of the definite integral of the interpolant over the interval $[a, b]$ .                                |                     |
| 8: | <b>fail</b> – NagError *  | <i>Input/Output</i> |
|    | The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).                                     |                     |

## 6 Error Indicators and Warnings

### NE\_INT\_ARG\_LT

On entry,  $\mathbf{n} = \langle \text{value} \rangle$ .  
Constraint:  $\mathbf{n} \geq 2$ .

### NE\_NOT\_MONOTONIC

On entry,  $\mathbf{x}[r-1] \geq \mathbf{x}[r]$  for  $r = \langle \text{value} \rangle : \mathbf{x}[r-1] = \langle \text{value} \rangle, \mathbf{x}[r] = \langle \text{value} \rangle$ .  
The values of  $\mathbf{x}[r]$ , for  $r = 0, 1, \dots, n-1$ , are not in strictly increasing order.

### NW\_INTERVAL\_EXTRAPOLATE

On entry, limits  $\mathbf{a}, \mathbf{b}$  must not be outside interval  $[\mathbf{x}[0], \mathbf{x}[n-1]]$ ,  $\mathbf{a} = \langle \text{value} \rangle, \mathbf{b} = \langle \text{value} \rangle$ ,  
 $\mathbf{x}[0] = \langle \text{value} \rangle, \mathbf{x}[\langle \text{value} \rangle] = \langle \text{value} \rangle$ . Extrapolation was performed to compute the integral. The  
value returned is therefore unreliable.

## 7 Accuracy

The computational error in the value returned for **integral** should be negligible in most practical situations.

## 8 Parallelism and Performance

nag\_monotonic\_intg (e01bhc) is not threaded in any implementation.

## 9 Further Comments

The time taken by nag\_monotonic\_intg (e01bhc) is approximately proportional to the number of data points included within the interval  $[a, b]$ .

## 10 Example

This example program reads in values of  $\mathbf{n}, \mathbf{x}, \mathbf{f}$  and  $\mathbf{d}$ . It then reads in pairs of values for  $\mathbf{a}$  and  $\mathbf{b}$ , and evaluates the definite integral of the interpolant over the interval  $(\mathbf{a}, \mathbf{b})$  until end-of-file is reached.

### 10.1 Program Text

```
/* nag_monotonic_intg (e01bhc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nage01.h>

int main(void)
{
    Integer exit_status = 0, n, r;
    NagError fail;
    double a, b, *d = 0, *f = 0, integral, *x = 0;

    INIT_FAIL(fail);

    printf("nag_monotonic_intg (e01bhc) Example Program Results\n");
#ifdef _WIN32
```

```

scanf_s("%*[\n]"); /* Skip heading in data file */
#else
scanf("%*[\n]"); /* Skip heading in data file */
#endif
#ifdef _WIN32
scanf_s("%" NAG_IFMT "", &n);
#else
scanf("%" NAG_IFMT "", &n);
#endif
if (n >= 2) {
if (!(d = NAG_ALLOC(n, double)) ||
!(f = NAG_ALLOC(n, double)) || !(x = NAG_ALLOC(n, double)))
{
printf("Allocation failure\n");
exit_status = -1;
goto END;
}
}
else {
printf("Invalid n.\n");
exit_status = 1;
return exit_status;
}
for (r = 0; r < n; r++)
#ifdef _WIN32
scanf_s("%lf%lf%lf", &x[r], &f[r], &d[r]);
#else
scanf("%lf%lf%lf", &x[r], &f[r], &d[r]);
#endif
printf("
a
b
Integral\n");
printf("
a
b
over (a,b)\n");
/* Read a, b pairs until end of file and compute
* definite integrals.
*/
#ifdef _WIN32
while (scanf_s("%lf%lf", &a, &b) != EOF)
#else
while (scanf("%lf%lf", &a, &b) != EOF)
#endif
{
/* nag_monotonic_intg (e01bhc).
* Evaluation of interpolant computed by
* nag_monotonic_interpolant (e01bec), definite integral
*/
nag_monotonic_intg(n, x, f, d, a, b, &integral, &fail);
if (fail.code != NE_NOERROR) {
printf("Error from nag_monotonic_intg (e01bhc).\n%s\n", fail.message);
exit_status = 1;
goto END;
}
printf("%13.4f %13.4f %13.4f\n", a, b, integral);
}
END:
NAG_FREE(d);
NAG_FREE(f);
NAG_FREE(x);
return exit_status;
}

```

## 10.2 Program Data

nag\_monotonic\_intg (e01bhc) Example Program Data

9			
7.990	0.00000E+0	0.00000E+0	
8.090	0.27643E-4	5.52510E-4	
8.190	0.43749E-1	0.33587E+0	
8.700	0.16918E+0	0.34944E+0	
9.200	0.46943E+0	0.59696E+0	
10.00	0.94374E+0	6.03260E-2	
12.00	0.99864E+0	8.98335E-4	

15.00	0.99992E+0	2.93954E-5
20.00	0.99999E+0	0.00000E+0
7.99	20.0	
10.0	12.0	
12.0	10.0	
15.0	15.0	

### 10.3 Program Results

nag\_monotonic\_intg (e01bhc) Example Program Results

a	b	Integral over (a,b)
7.9900	20.0000	10.7648
10.0000	12.0000	1.9622
12.0000	10.0000	-1.9622
15.0000	15.0000	0.0000

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