NAG Library Function Document

nag_zsymm (f16ztc)

1   Purpose

nag_zsymm (f16ztc) performs matrix-matrix multiplication for a complex symmetric matrix.

2   Specification

```
#include <nag.h>
#include <nagf16.h>
```

```
void nag_zsymm (Nag_OrderType order, Nag_SideType side, Nag_UploType uplo,
     Integer m, Integer n, Complex alpha, const Complex a[], Integer pda,
     const Complex b[], Integer pdb, Complex beta, Complex c[], Integer pdc,
     NagError *fail)
```

3   Description

nag_zsymm (f16ztc) performs one of the matrix-matrix operations

$$C \leftarrow \alpha AB + \beta C \quad \text{or} \quad C \leftarrow \alpha BA + \beta C,$$

where A is a complex symmetric matrix, B and C are m by n complex matrices, and α and β are complex scalars.

4   References

Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001) *Basic Linear Algebra Subprograms Technical (BLAST) Forum Standard* University of Tennessee, Knoxville, Tennessee http://www.netlib.org/blas/blast-forum/blas-report.pdf

5   Arguments

1:    **order** – Nag_OrderType   *Input*

On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 3.2.1.3 in the Essential Introduction for a more detailed explanation of the use of this argument.

Constraint: **order** = Nag_RowMajor or Nag_ColMajor.

2:    **side** – Nag_SideType   *Input*

On entry: specifies whether B is operated on from the left or the right.

side = Nag_LeftSide
        B is pre-multiplied from the left.

side = Nag_RightSide
        B is post-multiplied from the right.

Constraint: **side** = Nag_LeftSide or Nag_RightSide.

3:    **uplo** – Nag_UploType   *Input*

On entry: specifies whether the upper or lower triangular part of A is stored.

uplo = Nag_Upper
   The upper triangular part of A is stored.

uplo = Nag_Lower
   The lower triangular part of A is stored.

Constraint: **uplo** = Nag_Upper or Nag_Lower.

4:    **m** – Integer   *Input*

On entry: m, the number of rows of the matrices B and C; the order of A if **side** = Nag_LeftSide.

Constraint: $\mathbf{m} \geq 0$.

5:    **n** – Integer   *Input*

On entry: n, the number of columns of the matrices B and C; the order of A if **side** = Nag_RightSide.

Constraint: $\mathbf{n} \geq 0$.

6:    **alpha** – Complex   *Input*

On entry: the scalar α.

7:    **a**[*dim*] – const Complex   *Input*

Note: the dimension, *dim*, of the array **a** must be at least

   $\max(1, \mathbf{pda} \times \mathbf{m})$ when **side** = Nag_LeftSide;
   $\max(1, \mathbf{pda} \times \mathbf{n})$ when **side** = Nag_RightSide.

On entry: the symmetric matrix A; A is m by m if **side** = Nag_LeftSide, or n by n if **side** = Nag_RightSide.

If **order** = Nag_ColMajor, A_{ij} is stored in $\mathbf{a}[(j-1) \times \mathbf{pda} + i - 1]$.

If **order** = Nag_RowMajor, A_{ij} is stored in $\mathbf{a}[(i-1) \times \mathbf{pda} + j - 1]$.

If **uplo** = Nag_Upper, the upper triangular part of A must be stored and the elements of the array below the diagonal are not referenced.

If **uplo** = Nag_Lower, the lower triangular part of A must be stored and the elements of the array above the diagonal are not referenced.

8:    **pda** – Integer   *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) of the matrix A in the array **a**.

Constraints:

   if **side** = Nag_LeftSide, $\mathbf{pda} \geq \max(1, \mathbf{m})$;
   if **side** = Nag_RightSide, $\mathbf{pda} \geq \max(1, \mathbf{n})$.

9:    **b**[*dim*] – const Complex   *Input*

Note: the dimension, *dim*, of the array **b** must be at least

   $\max(1, \mathbf{pdb} \times \mathbf{n})$ when **order** = Nag_ColMajor;
   $\max(1, \mathbf{m} \times \mathbf{pdb})$ when **order** = Nag_RowMajor.

If **order** = Nag_ColMajor, B_{ij} is stored in $\mathbf{b}[(j-1) \times \mathbf{pdb} + i - 1]$.

If **order** = Nag_RowMajor, B_{ij} is stored in $\mathbf{b}[(i-1) \times \mathbf{pdb} + j - 1]$.

On entry: the m by n matrix B.

10: **pdb** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **b**.

Constraints:

> if **order** = Nag_ColMajor, **pdb** $\geq \max(1, \mathbf{m})$;
> if **order** = Nag_RowMajor, **pdb** $\geq \max(1, \mathbf{n})$.

11: **beta** – Complex *Input*

On entry: the scalar β.

12: **c**[dim] – Complex *Input/Output*

Note: the dimension, dim, of the array **c** must be at least

> $\max(1, \mathbf{pdc} \times \mathbf{n})$ when **order** = Nag_ColMajor;
> $\max(1, \mathbf{m} \times \mathbf{pdc})$ when **order** = Nag_RowMajor.

If **order** = Nag_ColMajor, C_{ij} is stored in $\mathbf{c}[(j-1) \times \mathbf{pdc} + i - 1]$.

If **order** = Nag_RowMajor, C_{ij} is stored in $\mathbf{c}[(i-1) \times \mathbf{pdc} + j - 1]$.

On entry: the m by n matrix C.

If **beta** = 0, **c** need not be set.

On exit: the updated matrix C.

13: **pdc** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **c**.

Constraints:

> if **order** = Nag_ColMajor, **pdc** $\geq \max(1, \mathbf{m})$;
> if **order** = Nag_RowMajor, **pdc** $\geq \max(1, \mathbf{n})$.

14: **fail** – NagError * *Input/Output*

The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.
See Section 3.2.1.2 in the Essential Introduction for further information.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_ENUM_INT_2

On entry, **side** = $\langle value \rangle$, **m** = $\langle value \rangle$, **pda** = $\langle value \rangle$.
Constraint: if **side** = Nag_LeftSide, **pda** $\geq \max(1, \mathbf{m})$.

On entry, **side** = $\langle value \rangle$, **n** = $\langle value \rangle$, **pda** = $\langle value \rangle$.
Constraint: if **side** = Nag_RightSide, **pda** $\geq \max(1, \mathbf{n})$.

NE_INT

On entry, $\mathbf{m} = \langle value \rangle$.
Constraint: $\mathbf{m} \geq 0$.

On entry, $\mathbf{n} = \langle value \rangle$.
Constraint: $\mathbf{n} \geq 0$.

NE_INT_2

On entry, $\mathbf{pdb} = \langle value \rangle$, $\mathbf{m} = \langle value \rangle$.
Constraint: $\mathbf{pdb} \geq \max(1, \mathbf{m})$.

On entry, $\mathbf{pdb} = \langle value \rangle$ and $\mathbf{n} = \langle value \rangle$.
Constraint: $\mathbf{pdb} \geq \max(1, \mathbf{n})$.

On entry, $\mathbf{pdc} = \langle value \rangle$, $\mathbf{m} = \langle value \rangle$.
Constraint: $\mathbf{pdc} \geq \max(1, \mathbf{m})$.

On entry, $\mathbf{pdc} = \langle value \rangle$ and $\mathbf{n} = \langle value \rangle$.
Constraint: $\mathbf{pdc} \geq \max(1, \mathbf{n})$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.
See Section 3.6.6 in the Essential Introduction for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.
See Section 3.6.5 in the Essential Introduction for further information.

7 Accuracy

The BLAS standard requires accurate implementations which avoid unnecessary over/underflow (see Section 2.7 of Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001)).

8 Parallelism and Performance

Not applicable.

9 Further Comments

None.

10 Example

This example computes the matrix-matrix product

$$C = \alpha AB + \beta C$$

where

$$A = \begin{pmatrix} 1.0 + 0.0i & 1.0 + 2.0i & -2.0 + 3.0i \\ 1.0 - 2.0i & 2.0 + 0.0i & 1.0 + 2.0i \\ -2.0 - 3.0i & 1.0 - 2.0i & 3.0 + 0.0i \end{pmatrix},$$

$$B = \begin{pmatrix} 1.0 - 1.0i & 1.0 + 2.0i \\ -2.0 + 1.0i & 2.0 - 2.0i \\ 3.0 - 1.0i & -3.0 + 1.0i \end{pmatrix},$$

$$C = \begin{pmatrix} -3.5 - 0.5i & 1.5 + 2.0i \\ -4.5 + 1.5i & -2.0 + 3.5i \\ -5.5 + 3.5i & 3.0 - 1.5i \end{pmatrix},$$

$$\alpha = 1.0 + 0.0i \quad \text{and} \quad \beta = 2.0 + 0.0i.$$

10.1 Program Text

```
/* nag_zsymm (f16ztc) Example Program.
 *
 * Copyright 2014 Numerical Algorithms Group.
 *
 * Mark 8, 2005.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf16.h>
#include <nagx04.h>

int main(void)
{

  /* Scalars */
  Complex       alpha, beta;
  Integer       exit_status, i, j, m, n, pda, pdb, pdc;

  /* Arrays */
  Complex       *a = 0, *b = 0, *c = 0;
  char          nag_enum_arg[40];

  /* Nag Types */
  NagError      fail;
  Nag_OrderType order;
  Nag_SideType  side;
  Nag_UploType  uplo;


#ifdef NAG_COLUMN_MAJOR
#define A(I, J) a[(J-1)*pda + I - 1]
#define B(I, J) b[(J-1)*pdb + I - 1]
#define C(I, J) c[(J-1)*pdc + I - 1]
  order = Nag_ColMajor;
#else
#define A(I, J) a[(I-1)*pda + J - 1]
#define B(I, J) b[(I-1)*pdb + J - 1]
#define C(I, J) c[(I-1)*pdc + J - 1]
  order = Nag_RowMajor;
#endif

  exit_status = 0;
  INIT_FAIL(fail);

  printf("nag_zsymm (f16ztc) Example Program Results\n\n");

  /* Skip heading in data file */
#ifdef _WIN32
  scanf_s("%*[^\n] ");
```

```
#else
  scanf("%*[^\n] ");
#endif

  /* Read the problem dimensions */
#ifdef _WIN32
  scanf_s("%"NAG_IFMT"%"NAG_IFMT"%*[^\n] ",
          &m, &n);
#else
  scanf("%"NAG_IFMT"%"NAG_IFMT"%*[^\n] ",
          &m, &n);
#endif

  /* Read the  side parameter */
#ifdef _WIN32
  scanf_s("%39s%*[^\n] ", nag_enum_arg, _countof(nag_enum_arg));
#else
  scanf("%39s%*[^\n] ", nag_enum_arg);
#endif
  /* nag_enum_name_to_value (x04nac).
   * Converts NAG enum member name to value
   */
  side = (Nag_SideType) nag_enum_name_to_value(nag_enum_arg);
  /* Read uplo */
#ifdef _WIN32
  scanf_s("%39s%*[^\n] ", nag_enum_arg, _countof(nag_enum_arg));
#else
  scanf("%39s%*[^\n] ", nag_enum_arg);
#endif
  /* nag_enum_name_to_value (x04nac).
   * Converts NAG enum member name to value
   */
  uplo = (Nag_UploType) nag_enum_name_to_value(nag_enum_arg);
  /* Read scalar parameters */
#ifdef _WIN32
  scanf_s(" ( %lf , %lf ) ( %lf , %lf )%*[^\n] ",
          &alpha.re, &alpha.im, &beta.re, &beta.im);
#else
  scanf(" ( %lf , %lf ) ( %lf , %lf )%*[^\n] ",
          &alpha.re, &alpha.im, &beta.re, &beta.im);
#endif

  if (side == Nag_LeftSide)
    pda = m;
  else
    pda = n;
#ifdef NAG_COLUMN_MAJOR
  pdb = m;
  pdc = m;
#else
  pdb = n;
  pdc = n;
#endif

  if (m > 0 && n > 0)
    {
      /* Allocate memory */
      if (side == Nag_LeftSide)
        {
          if (!(a = NAG_ALLOC(m*m, Complex)))
            {
              printf("Allocation failure\n");
              exit_status = -1;
              goto END;
            }
        }
      else
        {
          if (!(a = NAG_ALLOC(n*n, Complex)))
            {
              printf("Allocation failure\n");
```

```
                        exit_status = -1;
                        goto END;
                      }
                  }
          if (!(b = NAG_ALLOC(m*n, Complex)) ||
              !(c = NAG_ALLOC(m*n, Complex)))
            {
              printf("Allocation failure\n");
              exit_status = -1;
              goto END;
            }
        }
    else
      {
        printf("Invalid m or n\n");
        exit_status = 1;
        return exit_status;
      }

  /* Input matrix A */
  if (uplo == Nag_Upper)
    {
      for (i = 1; i <= pda; ++i)
        {
          for (j = i; j <= pda; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#endif
#ifdef _WIN32
          scanf_s("%*[^\n] ");
#else
          scanf("%*[^\n] ");
#endif
        }
    }
  else
    {
      for (i = 1; i <= pda; ++i)
        {
          for (j = 1; j <= i; ++j)
#ifdef _WIN32
            scanf_s(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#else
            scanf(" ( %lf , %lf )", &A(i, j).re, &A(i, j).im);
#endif
#ifdef _WIN32
          scanf_s("%*[^\n] ");
#else
          scanf("%*[^\n] ");
#endif
        }
    }
  /* Input matrix B */
  for (i = 1; i <= m; ++i)
    {
      for (j = 1; j <= n; ++j)
#ifdef _WIN32
        scanf_s(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#else
        scanf(" ( %lf , %lf )", &B(i, j).re, &B(i, j).im);
#endif
#ifdef _WIN32
      scanf_s("%*[^\n] ");
#else
      scanf("%*[^\n] ");
#endif
    }
  /* Input matrix C */
  for (i = 1; i <= m; ++i)
```

```
    {
      for (j = 1; j <= n; ++j)
#ifdef _WIN32
        scanf_s(" ( %lf , %lf )", &C(i, j).re, &C(i, j).im);
#else
        scanf(" ( %lf , %lf )", &C(i, j).re, &C(i, j).im);
#endif
#ifdef _WIN32
      scanf_s("%*[^\n] ");
#else
      scanf("%*[^\n] ");
#endif
    }

  /* nag_zsymm (f16ztc).
   * Complex symmetric matrix-matrix multiply.
   *
   */
  nag_zsymm(order, side, uplo, m, n, alpha, a, pda,
            b, pdb, beta, c, pdc, &fail);
  if (fail.code != NE_NOERROR)
    {
      printf("Error from nag_zsymm.\n%s\n", fail.message);
      exit_status = 1;
      goto END;
    }

  /* Print result */
  /* nag_gen_complx_mat_print (x04dac).
   * Print Complex general matrix (easy-to-use)
   */
  fflush(stdout);
  nag_gen_complx_mat_print(order, Nag_GeneralMatrix, Nag_NonUnitDiag,
                           m, n, c, pdc, "Matrix Matrix Product",
                           0, &fail);
  if (fail.code != NE_NOERROR)
    {
      printf("Error from nag_gen_complx_mat_print (x04dac).\n%s\n",
             fail.message);
      exit_status = 1;
      goto END;
    }

 END:
  NAG_FREE(a);
  NAG_FREE(b);
  NAG_FREE(c);

  return exit_status;
}
```

10.2 Program Data

```
nag_zsymm (f16ztc) Example Program Data
  3 2                  :Values of m, n
  Nag_LeftSide       : side
  Nag_Lower          : uplo
  ( 1.0, 0.0) ( 2.0, 0.0)  : alpha, beta
  ( 1.0, 0.0)
  ( 1.0,-2.0) ( 2.0, 0.0)
  (-2.0,-3.0) ( 1.0,-2.0) ( 3.0, 0.0) : the end of matrix A
  ( 1.0,-1.0) ( 1.0, 2.0)
  (-2.0, 1.0) ( 2.0,-2.0)
  ( 3.0,-1.0) (-3.0, 1.0)  : the end of matrix B
  (-3.5,-0.5) ( 1.5, 2.0)
  (-4.5, 1.5) (-2.0, 3.5)
  (-5.5, 3.5) ( 3.0,-1.5)  : the end of matrix C
```

10.3 Program Results

```
nag_zsymm (f16ztc) Example Program Results

 Matrix Matrix Product
             1          2
 1    -15.0000     11.0000
       -4.0000      7.0000

 2    -13.0000      4.0000
       -5.0000     10.0000

 3     -7.0000     -1.0000
        8.0000    -13.0000
```