

# NAG Library Function Document

## nag\_sparse\_nsym\_jacobi (f11dkc)

### 1 Purpose

nag\_sparse\_nsym\_jacobi (f11dkc) computes the **approximate** solution of a real, symmetric or nonsymmetric, sparse system of linear equations applying a number of Jacobi iterations. It is expected that nag\_sparse\_nsym\_jacobi (f11dkc) will be used as a preconditioner for the iterative solution of real sparse systems of equations.

### 2 Specification

```
#include <nag.h>
#include <nagf11.h>

void nag_sparse_nsym_jacobi (Nag_SparseNsym_Store store,
    Nag_TransType trans, Nag_InitializeA init, Integer niter, Integer n,
    Integer nnz, const double a[], const Integer irow[],
    const Integer icol[], Nag_SparseNsym_CheckData check, const double b[],
    double x[], double diag[], NagError *fail)
```

### 3 Description

nag\_sparse\_nsym\_jacobi (f11dkc) computes the **approximate** solution of the real sparse system of linear equations  $Ax = b$  using **niter** iterations of the Jacobi algorithm (see also Golub and Van Loan (1996) and Young (1971)):

$$x_{k+1} = x_k + D^{-1}(b - Ax_k) \quad (1)$$

where  $k = 1, 2, \dots, \mathbf{niter}$  and  $x_0 = 0$ .

nag\_sparse\_nsym\_jacobi (f11dkc) can be used both for nonsymmetric and symmetric systems of equations. For symmetric matrices, either all nonzero elements of the matrix  $A$  can be supplied using coordinate storage (CS), or only the nonzero elements of the lower triangle of  $A$ , using symmetric coordinate storage (SCS) (see the f11 Chapter Introduction).

It is expected that nag\_sparse\_nsym\_jacobi (f11dkc) will be used as a preconditioner for the iterative solution of real sparse systems of equations. This may be with either the symmetric or nonsymmetric suites of functions.

For symmetric systems the suite consists of:

```
nag_sparse_sym_basic_setup (f11gdc),
nag_sparse_sym_basic_solver (f11gec),
nag_sparse_sym_basic_diagnostic (f11gfc).
```

For nonsymmetric systems the suite consists of:

```
nag_sparse_nsym_basic_setup (f11bdc),
nag_sparse_nsym_basic_solver (f11bec),
nag_sparse_nsym_basic_diagnostic (f11bfc).
```

### 4 References

Golub G H and Van Loan C F (1996) *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

Young D (1971) *Iterative Solution of Large Linear Systems* Academic Press, New York

## 5 Arguments

- 1: **store** – Nag\_SparseNsym\_Store *Input*  
*On entry:* specifies whether the matrix  $A$  is stored using symmetric coordinate storage (SCS) (applicable only to a symmetric matrix  $A$ ) or coordinate storage (CS) (applicable to both symmetric and non-symmetric matrices).  
**store** = Nag\_SparseNsym\_StoreCS  
 The complete matrix  $A$  is stored in CS format.  
**store** = Nag\_SparseNsym\_StoreSCS  
 The lower triangle of the symmetric matrix  $A$  is stored in SCS format.  
*Constraint:* **store** = Nag\_SparseNsym\_StoreCS or Nag\_SparseNsym\_StoreSCS.
- 2: **trans** – Nag\_TransType *Input*  
*On entry:* if **store** = Nag\_SparseNsym\_StoreCS, specifies whether the approximate solution of  $Ax = b$  or of  $A^T x = b$  is required.  
**trans** = Nag\_NoTrans  
 The approximate solution of  $Ax = b$  is calculated.  
**trans** = Nag\_Trans  
 The approximate solution of  $A^T x = b$  is calculated.  
*Suggested value:* if the matrix  $A$  is symmetric and stored in CS format, it is recommended that **trans** = Nag\_NoTrans for reasons of efficiency.  
*Constraint:* **trans** = Nag\_NoTrans or Nag\_Trans.
- 3: **init** – Nag\_InitializeA *Input*  
*On entry:* on first entry, **init** should be set to Nag\_InitializeI, unless the diagonal elements of  $A$  are already stored in the array **diag**. If **diag** already contains the diagonal of  $A$ , it must be set to Nag\_InputA.  
**init** = Nag\_InputA  
**diag** must contain the diagonal of  $A$ .  
**init** = Nag\_InitializeI  
**diag** will store the diagonal of  $A$  on exit.  
*Suggested value:* **init** = Nag\_InitializeI on first entry; **init** = Nag\_InputA, subsequently, unless **diag** has been overwritten.  
*Constraint:* **init** = Nag\_InputA or Nag\_InitializeI.
- 4: **niter** – Integer *Input*  
*On entry:* the number of Jacobi iterations requested.  
*Constraint:* **niter**  $\geq$  1.
- 5: **n** – Integer *Input*  
*On entry:*  $n$ , the order of the matrix  $A$ .  
*Constraint:* **n**  $\geq$  1.
- 6: **nnz** – Integer *Input*  
*On entry:* if **store** = Nag\_SparseNsym\_StoreCS, the number of nonzero elements in the matrix  $A$ .  
 If **store** = Nag\_SparseNsym\_StoreSCS, the number of nonzero elements in the lower triangle of the matrix  $A$ .

*Constraints:*

if **store** = Nag\_SparseNsym\_StoreCS,  $1 \leq \mathbf{nnz} \leq \mathbf{n}^2$ ;  
 if **store** = Nag\_SparseNsym\_StoreSCS,  $1 \leq \mathbf{nnz} \leq \mathbf{n} \times (\mathbf{n} + 1)/2$ .

7: **a**[**nnz**] – const double *Input*

*On entry:* if **store** = Nag\_SparseNsym\_StoreCS, the nonzero elements in the matrix  $A$  (CS format).

If **store** = Nag\_SparseNsym\_StoreSCS, the nonzero elements in the lower triangle of the matrix  $A$  (SCS format).

In both cases, the elements of either  $A$  or of its lower triangle must be ordered by increasing row index and by increasing column index within each row. Multiple entries for the same row and columns indices are not permitted. The function nag\_sparse\_nsym\_sort (f11zac) or nag\_sparse\_sym\_sort (f11zbc) may be used to reorder the elements in this way for CS and SCS storage, respectively.

8: **irow**[**nnz**] – const Integer *Input*

9: **icol**[**nnz**] – const Integer *Input*

*On entry:* if **store** = Nag\_SparseNsym\_StoreCS, the row and column indices of the nonzero elements supplied in **a**.

If **store** = Nag\_SparseNsym\_StoreSCS, the row and column indices of the nonzero elements of the lower triangle of the matrix  $A$  supplied in **a**.

*Constraints:*

$1 \leq \mathbf{irow}[i] \leq \mathbf{n}$ , for  $i = 0, 1, \dots, \mathbf{nnz} - 1$ ;  
 if **store** = Nag\_SparseNsym\_StoreCS,  $1 \leq \mathbf{icol}[i] \leq \mathbf{n}$ , for  $i = 0, 1, \dots, \mathbf{nnz} - 1$ ;  
 if **store** = Nag\_SparseNsym\_StoreSCS,  $1 \leq \mathbf{icol}[i] \leq \mathbf{irow}[i]$ , for  $i = 0, 1, \dots, \mathbf{nnz} - 1$ ;  
 either  $\mathbf{irow}[i - 1] < \mathbf{irow}[i]$  or both  $\mathbf{irow}[i - 1] = \mathbf{irow}[i]$  and  $\mathbf{icol}[i - 1] < \mathbf{icol}[i]$ , for  $i = 1, 2, \dots, \mathbf{nnz} - 1$ .

10: **check** – Nag\_SparseNsym\_CheckData *Input*

*On entry:* specifies whether or not the CS or SCS representation of the matrix  $A$  should be checked.

**check** = Nag\_SparseNsym\_Check

Checks are carried out on the values of **n**, **nnz**, **irow**, **icol**; if **init** = Nag\_InputA, **diag** is also checked.

**check** = Nag\_SparseNsym\_NoCheck

None of these checks are carried out.

See also Section 9.2.

*Constraint:* **check** = Nag\_SparseNsym\_Check or Nag\_SparseNsym\_NoCheck.

11: **b**[**n**] – const double *Input*

*On entry:* the right-hand side vector  $b$ .

12: **x**[**n**] – double *Output*

*On exit:* the approximate solution vector  $x_{\mathbf{niter}}$ .

13: **diag**[**n**] – double *Input/Output*

*On entry:* if **init** = Nag\_InputA, the diagonal elements of  $A$ .

*On exit:* if **init** = Nag\_InputA, unchanged on exit.

If **init** = Nag\_InitializeI, the diagonal elements of  $A$ .

14: **fail** – NagError \*

Input/Output

The NAG error argument (see Section 3.6 in the Essential Introduction).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in the Essential Introduction for further information.

### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

### NE\_INT

On entry,  $\mathbf{n} = \langle value \rangle$ .

Constraint:  $\mathbf{n} \geq 1$ .

On entry,  $\mathbf{niter} = \langle value \rangle$ .

Constraint:  $\mathbf{niter} \geq 1$ .

On entry,  $\mathbf{nnz} = \langle value \rangle$ .

Constraint:  $\mathbf{nnz} \geq 1$ .

### NE\_INT\_2

On entry,  $\mathbf{nnz} = \langle value \rangle$  and  $\mathbf{n} = \langle value \rangle$ .

Constraint:  $\mathbf{nnz} \leq \mathbf{n} \times (\mathbf{n} + 1)/2$ .

On entry,  $\mathbf{nnz} = \langle value \rangle$  and  $\mathbf{n} = \langle value \rangle$ .

Constraint:  $\mathbf{nnz} \leq \mathbf{n}^2$ .

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in the Essential Introduction for further information.

### NE\_INVALID\_CS

On entry,  $I = \langle value \rangle$ ,  $\mathbf{icol}[I - 1] = \langle value \rangle$  and  $\mathbf{irow}[I - 1] = \langle value \rangle$ .

Constraint:  $\mathbf{icol}[I - 1] \geq 1$  and  $\mathbf{icol}[I - 1] \leq \mathbf{irow}[I - 1]$ .

On entry,  $I = \langle value \rangle$ ,  $\mathbf{icol}[I - 1] = \langle value \rangle$  and  $\mathbf{n} = \langle value \rangle$ .

Constraint:  $\mathbf{icol}[I - 1] \geq 1$  and  $\mathbf{icol}[I - 1] \leq \mathbf{n}$ .

On entry,  $I = \langle value \rangle$ ,  $\mathbf{irow}[I - 1] = \langle value \rangle$  and  $\mathbf{n} = \langle value \rangle$ .

Constraint:  $\mathbf{irow}[I - 1] \geq 1$  and  $\mathbf{irow}[I - 1] \leq \mathbf{n}$ .

### NE\_NO\_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 3.6.5 in the Essential Introduction for further information.

### NE\_NOT\_STRICTLY\_INCREASING

On entry,  $\mathbf{a}[i - 1]$  is out of order:  $i = \langle value \rangle$ .

On entry, the location  $(\mathbf{irow}[I - 1], \mathbf{icol}[I - 1])$  is a duplicate:  $I = \langle value \rangle$ .

**NE\_ZERO\_DIAG\_ELEM**

On entry, the diagonal element of the  $I$ -th row is zero or missing:  $I = \langle value \rangle$ .

On entry, the element **diag**[ $I - 1$ ] is zero:  $I = \langle value \rangle$ .

**7 Accuracy**

In general, the Jacobi method cannot be used on its own to solve systems of linear equations. The rate of convergence is bound by its spectral properties (see, for example, Golub and Van Loan (1996)) and as a solver, the Jacobi method can only be applied to a limited set of matrices. One condition that guarantees convergence is strict diagonal dominance.

However, the Jacobi method can be used successfully as a preconditioner to a wider class of systems of equations. The Jacobi method has good vector/parallel properties, hence it can be applied very efficiently. Unfortunately, it is not possible to provide criteria which define the applicability of the Jacobi method as a preconditioner, and its usefulness must be judged for each case.

**8 Parallelism and Performance**

`nag_sparse_nsym_jacobi` (f11dkc) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

`nag_sparse_nsym_jacobi` (f11dkc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

**9 Further Comments****9.1 Timing**

The time taken for a call to `nag_sparse_nsym_jacobi` (f11dkc) is proportional to **niter**  $\times$  **nnz**.

**9.2 Use of check**

It is expected that a common use of `nag_sparse_nsym_jacobi` (f11dkc) will be as preconditioner for the iterative solution of real, symmetric or nonsymmetric, linear systems. In this situation, `nag_sparse_nsym_jacobi` (f11dkc) is likely to be called many times. In the interests of both reliability and efficiency, you are recommended to set **check** = `Nag_SparseNsym_Check` for the first of such calls, and to set **check** = `Nag_SparseNsym_NoCheck` for all subsequent calls.

**10 Example**

This example solves the real sparse nonsymmetric system of equations  $Ax = b$  iteratively using `nag_sparse_nsym_jacobi` (f11dkc) as a preconditioner.

**10.1 Program Text**

```
/* nag_sparse_nsym_jacobi (f11dkc) Example Program.
 *
 * Copyright 2014 Numerical Algorithms Group.
 *
 * Mark 23, 2011.
 */
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf11.h>
int main(void)
{
```

```

/* Scalars */
Integer          exit_status = 0;
double           anorm, sigmax, stplhs, stprhs, tol;
Integer         i, irevcm, item, itn, lwork, lwreq, m, maxitn, monit,
                n, niter, nnz;

/* Arrays */
char            nag_enum_arg[100];
double          *a = 0, *b = 0, *diag = 0, *wgt = 0, *work = 0,
                *x = 0;
Integer         *icol = 0, *irow = 0;

/* NAG types */
Nag_InitializeA  init;
Nag_SparseNsym_Method  method;
Nag_SparseNsym_PrecType  precon;
Nag_NormType      norm;
Nag_SparseNsym_Weight  weight;
Nag_Error         fail, fail1;

INIT_FAIL(fail);
INIT_FAIL(fail1);

printf("nag_sparse_nsym_jacobi (f11dkc) Example Program Results \n");
/* Skip heading in data file */
#ifdef _WIN32
scanf_s("%*[\n]");
#else
scanf("%*[\n]");
#endif
#ifdef _WIN32
scanf_s("%"NAG_IFMT"%*[\n]", &n);
#else
scanf("%"NAG_IFMT"%*[\n]", &n);
#endif
#ifdef _WIN32
scanf_s("%"NAG_IFMT"%*[\n]", &nnz);
#else
scanf("%"NAG_IFMT"%*[\n]", &nnz);
#endif
lwork = 200;
if (
    !(a = NAG_ALLOC((nnz), double)) ||
    !(b = NAG_ALLOC((n), double)) ||
    !(diag = NAG_ALLOC((n), double)) ||
    !(wgt = NAG_ALLOC((n), double)) ||
    !(work = NAG_ALLOC((lwork), double)) ||
    !(x = NAG_ALLOC((n), double)) ||
    !(icol = NAG_ALLOC((nnz), Integer)) ||
    !(irow = NAG_ALLOC((nnz), Integer))
)
{
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
}
/* Read or initialize the parameters for the iterative solver */
#ifdef _WIN32
scanf_s("%99s%*[\n]", nag_enum_arg, _countof(nag_enum_arg));
#else
scanf("%99s%*[\n]", nag_enum_arg);
#endif
/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
method = (Nag_SparseNsym_Method) nag_enum_name_to_value(nag_enum_arg);
#ifdef _WIN32
scanf_s("%99s%*[\n]", nag_enum_arg, _countof(nag_enum_arg));
#else
scanf("%99s%*[\n]", nag_enum_arg);
#endif
precon = (Nag_SparseNsym_PrecType) nag_enum_name_to_value(nag_enum_arg);
#ifdef _WIN32

```

```

    scanf_s("%99s%[\n]", nag_enum_arg, _countof(nag_enum_arg));
#else
    scanf("%99s%[\n]", nag_enum_arg);
#endif
    norm = (Nag_NormType) nag_enum_name_to_value(nag_enum_arg);
#ifdef _WIN32
    scanf_s("%99s%[\n]", nag_enum_arg, _countof(nag_enum_arg));
#else
    scanf("%99s%[\n]", nag_enum_arg);
#endif
    weight = (Nag_SparseNsym_Weight) nag_enum_name_to_value(nag_enum_arg);

#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%[\n]", &iterm);
#else
    scanf("%"NAG_IFMT"%[\n]", &iterm);
#endif
#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%lf%"NAG_IFMT"%[\n]", &m, &tol, &maxitn);
#else
    scanf("%"NAG_IFMT"%lf%"NAG_IFMT"%[\n]", &m, &tol, &maxitn);
#endif
#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%[\n]", &monit);
#else
    scanf("%"NAG_IFMT"%[\n]", &monit);
#endif

    /* Read the parameters for the preconditioner */
#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%[\n]", &niter);
#else
    scanf("%"NAG_IFMT"%[\n]", &niter);
#endif
    anorm = 0.0;
    sigmax = 0.0;

    /* Read the non-zero elements of the matrix A */
    for (i = 0; i <= nnz - 1; i++)
#ifdef _WIN32
        scanf_s("%lf%"NAG_IFMT%"NAG_IFMT"%[\n]", &a[i], &irow[i], &icol[i]);
#else
        scanf("%lf%"NAG_IFMT%"NAG_IFMT"%[\n]", &a[i], &irow[i], &icol[i]);
#endif

    /* Read right-hand side vector b and initial approximate solution */
#ifdef _WIN32
    for (i = 0; i <= n - 1; i++) scanf_s("%lf", &b[i]);
#else
    for (i = 0; i <= n - 1; i++) scanf("%lf", &b[i]);
#endif
#ifdef _WIN32
    scanf_s("%*[\n]");
#else
    scanf("%*[\n]");
#endif
#ifdef _WIN32
    for (i = 0; i <= n - 1; i++) scanf_s("%lf", &x[i]);
#else
    for (i = 0; i <= n - 1; i++) scanf("%lf", &x[i]);
#endif

    /* nag_sparse_nsym_basic_setup (f11bdc)
     * Real sparse nonsymmetric linear systems, setup routine
     */
    nag_sparse_nsym_basic_setup(method, precon, norm, weight, iterm, n, m, tol,
                                maxitn, anorm, sigmax, monit, &lwreq, work,
                                lwork, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_sparse_nsym_basic_setup (f11bdc).\n%s\n",
              fail.message);
    }

```

```

    exit_status = 1;
    goto END;
}
/* call solver repeatedly to solve the equations
 * Note that the arrays b and x are overwritten
 * On final exit, x will contain the solution and b the residual vector
 */
irevcm = 0;
lwreq = lwork;
init = Nag_InitializeI;
while (irevcm != 4) {
    /* nag_sparse_nsym_basic_solver (f11bec)
     * Real sparse nonsymmetric linear systems, solver routine
     * preconditioned RGMRES, CGS, Bi-CGSTAB or TFQMR method
     */
    nag_sparse_nsym_basic_solver(&irevcm, x, b, wgt, work, lwreq, &fail);
    switch (irevcm) {
    case -1:
        /* nag_sparse_nsym_matvec (f11xac)
         * Real sparse nonsymmetric matrix vector multiply
         */
        nag_sparse_nsym_matvec(Nag_Trans, n, nnz, a, irow, icol,
                               Nag_SparseNsym_NoCheck, x, b, &fail1);

        break;
    case 1:
        nag_sparse_nsym_matvec(Nag_NoTrans, n, nnz, a, irow, icol,
                               Nag_SparseNsym_NoCheck, x, b, &fail1);

        break;
    case 2:
        /* nag_sparse_nsym_jacobi (f11dkc)
         * Real sparse nonsymmetric linear systems, line Jacobi preconditioner
         */
        nag_sparse_nsym_jacobi(Nag_SparseNsym_StoreCS, Nag_NoTrans, init,
                               niter, n, nnz, a, irow, icol,
                               Nag_SparseNsym_Check, x, b, diag, &fail1);

        init = Nag_InputA;
        break;
    case 3:
        /* nag_sparse_nsym_basic_diagnostic (f11bfc)
         * Real sparse nonsymmetric linear systems, diagnostic for f11bec
         */
        nag_sparse_nsym_basic_diagnostic(&itn, &stplhs, &stprhs, &anorm, &sigmax,
                                          work, lwreq, &fail1);
        printf("%"NAG_IFMT" %f \n", itn, stplhs);
    }
    if (fail1.code != NE_NOERROR) irevcm = 6;
}
if (fail.code != NE_NOERROR)
{
    printf("Error from nag_sparse_nsym_basic_solver (f11bec)\n%s\n",
          fail.message);
    exit_status = 2;
    goto END;
}

/* Obtain information about the computation*/
nag_sparse_nsym_basic_diagnostic(&itn, &stplhs, &stprhs, &anorm, &sigmax,
                                work, lwreq, &fail);

/* Print the output data*/
printf("\nFinal Results\n");
printf("Number of iterations for convergence:      %5"NAG_IFMT" \n", itn);
printf("Residual norm:                               %14.4e\n", stplhs);
printf("Right-hand side of termination criterion: %14.4e\n", stprhs);
printf("1-norm of matrix A:                          %14.4e\n\n", anorm);

/* Output x*/
printf("%16s%16s\n", "Solution", "Residuals");
for (i = 0; i < n; i++) printf("%16.4f%16.4e\n", x[i], b[i]);

END:
    NAG_FREE(a);

```



```

NAG_FREE(b);
NAG_FREE(diag);
NAG_FREE(wgt);
NAG_FREE(work);
NAG_FREE(x);
NAG_FREE(icol);
NAG_FREE(irow);
return exit_status;
}

```

## 10.2 Program Data

nag\_sparse\_nsym\_jacobi (f11dkc) Example Program Data

```

8          : n
24         : nnz
Nag_SparseNsym_BiCGSTAB : method
Nag_SparseNsym_Prec     : precon
Nag_OneNorm            : norm
Nag_SparseNsym_UnWeighted : weight
1                   : iterm
2  1.0e-6  20        : m, tol, maxitn
1                   : monit
4                   : niter
4.0  1      1
-1.0  1      4
1.0  1      8
4.0  2      1
-5.0  2      2
2.0  2      5
-7.0  3      3
2.0  3      6
2.0  4      1
-1.0  4      3
6.0  4      4
2.0  4      7
-1.0  5      2
8.0  5      5
-2.0  5      7
-2.0  6      1
5.0  6      3
8.0  6      6
-2.0  7      3
-1.0  7      5
7.0  7      7
-1.0  8      2
2.0  8      6
6.0  8      8          : a[i], irow[i], icol[i], i=0,...,nnz-1
6.0  8.0  -9.0  46.0
17.0 21.0 22.0 34.0   : b[i], i=0,...,n-1
0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0   : x[i], i=0,...,n-1

```

## 10.3 Program Results

nag\_sparse\_nsym\_jacobi (f11dkc) Example Program Results

Final Results

```

Number of iterations for convergence:      2
Residual norm:                            1.1177e-04
Right-hand side of termination criterion:  5.4082e-04
1-norm of matrix A:                       1.5000e+01

```

Solution	Residuals
1.7035	3.2377e-07
1.0805	-1.7625e-05
1.8305	2.7964e-05

6.0251	-2.5914e-05
3.2942	7.8156e-06
1.9068	9.2064e-06
4.1365	-3.0848e-06
5.2111	1.9834e-05

---