NAG Library Function Document

nag_dormrq (f08ckc)

1 Purpose

nag_dormrq (f08ckc) multiplies a general real m by n matrix C by the real orthogonal matrix Q from an RQ factorization computed by nag_dgerqf (f08chc).

2 Specification

```
#include <nag.h>
#include <nagf08.h>
```

```
void nag_dormrq (Nag_OrderType order, Nag_SideType side,
    Nag_TransType trans, Integer m, Integer n, Integer k, double a[],
    Integer pda, const double tau[], double c[], Integer pdc,
    NagError *fail)
```

3 Description

nag_dormrq (f08ckc) is intended to be used following a call to nag_dgerqf (f08chc), which performs an RQ factorization of a real matrix A and represents the orthogonal matrix Q as a product of elementary reflectors.

This function may be used to form one of the matrix products

 $QC, \quad Q^{\mathrm{T}}C, \quad CQ, \quad CQ^{\mathrm{T}},$

overwriting the result on C, which may be any real rectangular m by n matrix.

A common application of this function is in solving underdetermined linear least squares problems, as described in the f08 Chapter Introduction, and illustrated in Section 10 in nag_dgerqf (f08chc).

4 References

Anderson E, Bai Z, Bischof C, Blackford S, Demmel J, Dongarra J J, Du Croz J J, Greenbaum A, Hammarling S, McKenney A and Sorensen D (1999) *LAPACK Users' Guide* (3rd Edition) SIAM, Philadelphia http://www.netlib.org/lapack/lug

Golub G H and Van Loan C F (1996) Matrix Computations (3rd Edition) Johns Hopkins University Press, Baltimore

5 Arguments

1: **order** – Nag_OrderType

On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., rowmajor ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 3.2.1.3 in the Essential Introduction for a more detailed explanation of the use of this argument.

Constraint: **order** = Nag_RowMajor or Nag_ColMajor.

2: **side** – Nag SideType

On entry: indicates how Q or Q^{T} is to be applied to C.

side = Nag_LeftSide

Q or Q^{T} is applied to C from the left.

Input

Input

	side = Nag_RightSide Q or Q^{T} is applied to C from the right.
	Constraint: side = Nag_LeftSide or Nag_RightSide.
3:	trans – Nag_TransType Input
	On entry: indicates whether Q or Q^{T} is to be applied to C.
	trans = Nag_NoTrans Q is applied to C .
	trans = Nag_Trans Q^{T} is applied to C.
	Constraint: trans = Nag_NoTrans or Nag_Trans.
4:	m – Integer
	On entry: m , the number of rows of the matrix C .
	Constraint: $\mathbf{m} \ge 0$.
5:	n – Integer Input
	On entry: n, the number of columns of the matrix C.
	Constraint: $\mathbf{n} \ge 0$.
6:	k – Integer Input
	On entry: k , the number of elementary reflectors whose product defines the matrix Q .
	Constraints:
	if side = Nag_LeftSide, $\mathbf{m} \ge \mathbf{k} \ge 0$; if side = Nag_RightSide, $\mathbf{n} \ge \mathbf{k} \ge 0$.
7:	a [dim] – double Input/Output
	Note: the dimension, dim, of the array a must be at least
	$max(1, pda \times m)$ when side = Nag_LeftSide and order = Nag_ColMajor; $max(1, \mathbf{k} \times pda)$ when side = Nag_LeftSide and order = Nag_RowMajor; $max(1, pda \times n)$ when side = Nag_RightSide and order = Nag_ColMajor; $max(1, \mathbf{k} \times pda)$ when side = Nag_RightSide and order = Nag_RowMajor.
	The (i, j) th element of the matrix A is stored in
	$\mathbf{a}[(j-1) \times \mathbf{pda} + i - 1]$ when $\mathbf{order} = \operatorname{Nag_ColMajor};$ $\mathbf{a}[(i-1) \times \mathbf{pda} + j - 1]$ when $\mathbf{order} = \operatorname{Nag_RowMajor}.$
	On entry: the <i>i</i> th row of a must contain the vector which defines the elementary reflector H_i , for $i = 1, 2,, k$, as returned by nag_dgerqf (f08chc).
	On exit: is modified by nag_dormrq (f08ckc) but restored on exit.
8:	pda – Integer Input
	On entry: the stride separating row or column elements (depending on the value of order) in the array a .
	Constraints:
	if order = Nag_ColMajor, $pda \ge max(1, k)$; if order = Nag_RowMajor,

if side = Nag_LeftSide, $pda \ge max(1, m)$; if side = Nag_RightSide, $pda \ge max(1, n)$..

9: tau[dim] - const double

Note: the dimension, *dim*, of the array tau must be at least $max(1, \mathbf{k})$.

On entry: tau[i-1] must contain the scalar factor of the elementary reflector H_i , as returned by nag dgerqf (f08chc).

10:
$$\mathbf{c}[dim] - double$$

Note: the dimension, dim, of the array c must be at least

 $\max(1, \mathbf{pdc} \times \mathbf{n})$ when $\mathbf{order} = \operatorname{Nag_ColMajor};$ $\max(1, \mathbf{m} \times \mathbf{pdc})$ when $\mathbf{order} = \operatorname{Nag_RowMajor}.$

The (i, j)th element of the matrix C is stored in

 $\mathbf{c}[(j-1) \times \mathbf{pdc} + i - 1]$ when $\mathbf{order} = \text{Nag_ColMajor};$ $\mathbf{c}[(i-1) \times \mathbf{pdc} + j - 1]$ when $\mathbf{order} = \text{Nag_RowMajor}.$

On entry: the m by n matrix C.

On exit: **c** is overwritten by QC or $Q^{T}C$ or CQ or CQ^{T} as specified by side and trans.

11: **pdc** – Integer

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **c**.

Constraints:

if order = Nag_ColMajor, $pdc \ge max(1, m)$; if order = Nag_RowMajor, $pdc \ge max(1, n)$.

12: fail – NagError *

The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed. See Section 3.2.1.2 in the Essential Introduction for further information.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_ENUM_INT_3

On entry, $side = \langle value \rangle$, $\mathbf{m} = \langle value \rangle$, $\mathbf{n} = \langle value \rangle$ and $\mathbf{k} = \langle value \rangle$. Constraint: if $side = \text{Nag}_\text{LeftSide}$, $\mathbf{m} \ge \mathbf{k} \ge 0$; if $side = \text{Nag}_\text{RightSide}$, $\mathbf{n} \ge \mathbf{k} \ge 0$.

On entry, $side = \langle value \rangle$, $pda = \langle value \rangle$, $m = \langle value \rangle$ and $n = \langle value \rangle$. Constraint: if $side = Nag_LeftSide$, $pda \ge max(1, m)$; if $side = Nag_RightSide$, $pda \ge max(1, n)$.

NE_INT

On entry, $\mathbf{m} = \langle value \rangle$. Constraint: $\mathbf{m} \ge 0$. On entry, $\mathbf{n} = \langle value \rangle$.

Constraint: $\mathbf{n} \ge 0$.

Input

Input/Output

Input

Input/Output

On entry, $\mathbf{pda} = \langle value \rangle$. Constraint: $\mathbf{pda} > 0$.

On entry, $\mathbf{pdc} = \langle value \rangle$. Constraint: $\mathbf{pdc} > 0$.

NE_INT_2

On entry, $\mathbf{pda} = \langle value \rangle$ and $\mathbf{k} = \langle value \rangle$. Constraint: $\mathbf{pda} \geq \max(1, \mathbf{k})$.

On entry, $\mathbf{pdc} = \langle value \rangle$ and $\mathbf{m} = \langle value \rangle$. Constraint: $\mathbf{pdc} \geq \max(1, \mathbf{m})$.

On entry, $\mathbf{pdc} = \langle value \rangle$ and $\mathbf{n} = \langle value \rangle$. Constraint: $\mathbf{pdc} \geq \max(1, \mathbf{n})$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG. See Section 3.6.6 in the Essential Introduction for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly. See Section 3.6.5 in the Essential Introduction for further information.

7 Accuracy

The computed result differs from the exact result by a matrix E such that

$$||E||_2 = O\epsilon ||C||_2$$

where ϵ is the *machine precision*.

8 Parallelism and Performance

nag_dormrq (f08ckc) is not threaded by NAG in any implementation.

nag_dormrq (f08ckc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

The total number of floating-point operations is approximately 2nk(2m-k) if side = Nag_LeftSide and 2mk(2n-k) if side = Nag_RightSide.

The complex analogue of this function is nag_zunmrq (f08cxc).

10 Example

See Section 10 in nag_dgerqf (f08chc).