

# NAG Library Function Document

## nag\_mv\_distance\_mat (g03eac)

### 1 Purpose

nag\_mv\_distance\_mat (g03eac) computes a distance (dissimilarity) matrix.

### 2 Specification

```
#include <nag.h>
#include <nagg03.h>

void nag_mv_distance_mat (Nag_MatUpdate update, Nag_DistanceType dist,
    Nag_VarScaleType scale, Integer n, Integer m, const double x[],
    Integer tdx, const Integer isx[], double s[], double d[],
    NagError *fail)
```

### 3 Description

Given  $n$  objects, a distance or dissimilarity matrix, is a symmetric matrix with zero diagonal elements such that the  $ij$ th element represents how far apart or how dissimilar the  $i$ th and  $j$ th objects are.

Let  $X$  be an  $n$  by  $p$  data matrix of observations of  $p$  variables on  $n$  objects, then the distance between object  $j$  and object  $k$ ,  $d_{jk}$ , can be defined as:

$$d_{jk} = \left\{ \sum_{i=1}^p D(x_{ji}/s_i, x_{ki}/s_i) \right\}^{\alpha},$$

where  $x_{ji}$  and  $x_{ki}$  are the  $(j, i)$ th and  $(k, i)$ th elements of  $X$ ,  $s_i$  is a standardization for the  $i$ th variable and  $D(u, v)$  is a suitable function. Three functions are provided in nag\_mv\_distance\_mat (g03eac):

- Euclidean distance:  $D(u, v) = (u - v)^2$  and  $\alpha = \frac{1}{2}$ .
- Euclidean squared distance:  $D(u, v) = (u - v)^2$  and  $\alpha = 1$ .
- Absolute distance (city block metric):  $D(u, v) = |u - v|$  and  $\alpha = 1$ .

Three standardizations are available:

- Standard deviation:  $s_i = \sqrt{\sum_{j=1}^n (x_{ji} - \bar{x})^2 / (n - 1)}$
- Range:  $s_i = \max(x_{1i}, x_{2i}, \dots, x_{ni}) - \min(x_{1i}, x_{2i}, \dots, x_{ni})$
- User-supplied values of  $s_i$ .

In addition to the above distances there are a large number of other dissimilarity measures, particularly for dichotomous variables (see Krzanowski (1990) and Everitt (1974)). For the dichotomous case these measures are simple to compute and can, if suitable scaling is used, be combined with the distances computed by nag\_mv\_distance\_mat (g03eac) using the updating option.

Dissimilarity measures for variables can be based on the correlation coefficient for continuous variables and contingency table statistics for dichotomous data, see the g02 Chapter Introduction and the g11 Chapter Introduction respectively.

nag\_mv\_distance\_mat (g03eac) returns the strictly lower triangle of the distance matrix.

### 4 References

Everitt B S (1974) *Cluster Analysis* Heinemann

Krzanowski W J (1990) *Principles of Multivariate Analysis* Oxford University Press

## 5 Arguments

- 1: **update** – Nag\_MatUpdate *Input*  
*On entry:* indicates whether or not an existing matrix is to be updated.  
**update** = Nag\_MatUp  
 The matrix  $D$  is updated and distances are added to  $D$ .  
**update** = Nag\_NoMatUp  
 The matrix  $D$  is initialized to zero before the distances are added to  $D$ .  
*Constraint:* **update** = Nag\_MatUp or Nag\_NoMatUp.
- 2: **dist** – Nag\_DistanceType *Input*  
*On entry:* indicates which type of distances are computed.  
**dist** = Nag\_DistAbs  
 Absolute distances.  
**dist** = Nag\_DistEuclid  
 Euclidean distances.  
**dist** = Nag\_DistSquared  
 Euclidean squared distances.  
*Constraint:* **dist** = Nag\_DistAbs, Nag\_DistEuclid or Nag\_DistSquared.
- 3: **scale** – Nag\_VarScaleType *Input*  
*On entry:* indicates the standardization of the variables to be used.  
**scale** = Nag\_VarScaleStd  
 Standard deviation.  
**scale** = Nag\_VarScaleRange  
 Range.  
**scale** = Nag\_VarScaleUser  
 Standardizations given in array  $S$ .  
**scale** = Nag\_NoVarScale  
 Unscaled.  
*Constraint:* **scale** = Nag\_VarScaleStd, Nag\_VarScaleRange, Nag\_VarScaleUser or Nag\_NoVarScale.
- 4: **n** – Integer *Input*  
*On entry:* the number of observations,  $n$ .  
*Constraint:*  $n \geq 2$ .
- 5: **m** – Integer *Input*  
*On entry:* the total number of variables in array  $x$ .  
*Constraint:*  $m > 0$ .
- 6: **x[n × tdx]** – const double *Input*  
*On entry:*  $x[(i - 1) \times \mathbf{tdx} + j - 1]$  must contain the value of the  $j$ th variable for the  $i$ th object, for  $i = 1, 2, \dots, n$  and  $j = 1, 2, \dots, \mathbf{m}$ .

- 7: **tdx** – Integer *Input*  
*On entry:* the stride separating matrix column elements in the array **x**.  
*Constraint:* **tdx**  $\geq$  **m**.
- 8: **isx[m]** – const Integer *Input*  
*On entry:* **isx[j - 1]** indicates whether or not the *j*th variable in **x** is to be included in the distance computations.  
 If **isx[j - 1]**  $>$  0 the *j*th variable is included, for  $j = 1, 2, \dots, \mathbf{m}$ ; otherwise it is not referenced.  
*Constraint:* **isx[j - 1]**  $>$  0 for at least one *j*, , for  $j = 1, 2, \dots, \mathbf{m}$ .
- 9: **s[m]** – double *Input/Output*  
*On entry:* if **scale** = Nag\_VarScaleUser and **isx[j - 1]**  $>$  0 then **s[j - 1]** must contain the scaling for variable *j*, for  $j = 1, 2, \dots, \mathbf{m}$ .  
*Constraint:* if **scale** = Nag\_VarScaleUser and **isx[j - 1]**  $>$  0, **s[j - 1]**  $>$  0.0, for  $j = 1, 2, \dots, \mathbf{m}$ .  
*On exit:* if **scale** = Nag\_VarScaleStd and **isx[j - 1]**  $>$  0 then **s[j - 1]** contains the standard deviation of the variable in the *j*th column of **x**.  
 If **scale** = Nag\_VarScaleRange and **isx[j - 1]**  $>$  0 then **s[j - 1]** contains the range of the variable in the *j*th column of **x**.  
 If **scale** = Nag\_NoVarScale and **isx[j - 1]**  $>$  0 then **s[j - 1]** = 1.0 and if **scale** = Nag\_VarScaleUser then **s** is unchanged.
- 10: **d[n × (n - 1)/2]** – double *Input/Output*  
*On entry:* if **update** = Nag\_MatUp then **d** must contain the strictly lower triangle of the distance matrix *D* to be updated. *D* must be stored packed by rows, i.e., **d[(i - 1)(i - 2)/2 + j - 1]**,  $i > j$  must contain  $d_{ij}$ .  
*Constraint:* if **update** = Nag\_MatUp, **d[j - 1]**  $\geq$  0.0, for  $j = 1, 2, \dots, n(n - 1)/2$ .  
*On exit:* the strictly lower triangle of the distance matrix *D* stored packed by rows, i.e.,  $d_{ij}$  is contained in **d[(i - 1)(i - 2)/2 + j - 1]**,  $i > j$ .
- 11: **fail** – NagError \* *Input/Output*  
 The NAG error argument (see Section 3.6 in the Essential Introduction).

## 6 Error Indicators and Warnings

### NE\_2\_INT\_ARG\_LT

On entry, **tdx** = *<value>* while **m** = *<value>*. These arguments must satisfy **tdx**  $\geq$  **m**.

### NE\_BAD\_PARAM

On entry, argument **dist** had an illegal value.

On entry, argument **scale** had an illegal value.

On entry, argument **update** had an illegal value.

### NE\_IDEN\_ELEM\_COND

On entry, **scale** = Nag\_VarScaleRange or **scale** = Nag\_VarScaleStd, and  $\mathbf{x}[(i - 1) \times \mathbf{tdx} + j - 1] = \mathbf{x}[i \times \mathbf{tdx} + j - 1]$ , for  $i = 1, 2, \dots, n - 1$ , for some *j* with **isx[i - 1]**  $>$  0.

**NE\_INT\_ARG\_LE**

On entry,  $\mathbf{m} = \langle \text{value} \rangle$ .  
 Constraint:  $\mathbf{m} > 0$ .

**NE\_INT\_ARG\_LT**

On entry,  $\mathbf{n} = \langle \text{value} \rangle$ .  
 Constraint:  $\mathbf{n} \geq 2$ .

**NE\_INTARR**

On entry,  $\mathbf{isx}[\langle \text{value} \rangle] = \langle \text{value} \rangle$ .  
 Constraint:  $\mathbf{isx}[i - 1] > 0$ , for at least one  $i, i = 1, 2, \dots, \mathbf{m}$ .

**NE\_INTERNAL\_ERROR**

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

**NE\_REALARR**

On entry,  $\mathbf{d}[\langle \text{value} \rangle] = \langle \text{value} \rangle$ .  
 Constraint:  $\mathbf{d}[i - 1] \geq 0$ , for  $i = 1, 2, \dots, \mathbf{n} \times (\mathbf{n} - 1)/2$ , when **update** = Nag\_MatUp.  
 On entry,  $\mathbf{s}[\langle \text{value} \rangle] = \langle \text{value} \rangle$ .  
 Constraint:  $\mathbf{s}[j - 1] > 0$ , for  $j = 1, 2, \dots, \mathbf{m}$ , when **scale** = Nag\_VarScaleUser and  $\mathbf{isx}[j - 1] > 0$ .

**7 Accuracy**

The computations are believed to be stable.

**8 Parallelism and Performance**

Not applicable.

**9 Further Comments**

nag\_mv\_hierar\_cluster\_analysis (g03ecc) can be used to perform cluster analysis on the computed distance matrix.

**10 Example**

A data matrix of five observations and three variables is read in and a distance matrix is calculated from variables 2 and 3 using squared Euclidean distance with no scaling. This matrix is then printed.

**10.1 Program Text**

```
/* nag_mv_distance_mat (g03eac) Example Program.
 *
 * Copyright 1998 Numerical Algorithms Group.
 *
 * Mark 5, 1998.
 * Mark 8 revised, 2004.
 *
 */

#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagg03.h>

#define X(I, J) x[(I) * tdx + J]
```

```

int main(void)
{
    Integer          exit_status = 0, i, *isx = 0, j, m, n, tdx;
    double           *d = 0, *s = 0, *x = 0;
    char             nag_enum_arg[40];
    Nag_DistanceType dist;
    Nag_MatUpdate    update;
    Nag_VarScaleType scale;
    NagError         fail;

    INIT_FAIL(fail);

    printf("nag_mv_distance_mat (g03eac) Example Program Results\n\n");

    /* Skip heading in data file */
    scanf("%*[\n]");
    scanf("%ld", &n);
    scanf("%ld", &m);
    if (n >= 2 && m >= 1)
    {
        if (!(d = NAG_ALLOC(n*(n-1)/2, double)) ||
            !(s = NAG_ALLOC(m, double)) ||
            !(x = NAG_ALLOC((n)*(m), double)) ||
            !(isx = NAG_ALLOC(m, Integer)))
        {
            printf("Allocation failure\n");
            exit_status = -1;
            goto END;
        }
        tdx = m;
    }
    else
    {
        printf("Invalid n or m.\n");
        exit_status = 1;
        return exit_status;
    }
    scanf("%39s", nag_enum_arg);
    /* nag_enum_name_to_value (x04nac).
     * Converts NAG enum member name to value
     */
    update = (Nag_MatUpdate) nag_enum_name_to_value(nag_enum_arg);
    scanf("%39s", nag_enum_arg);
    dist = (Nag_DistanceType) nag_enum_name_to_value(nag_enum_arg);
    scanf("%39s", nag_enum_arg);
    scale = (Nag_VarScaleType) nag_enum_name_to_value(nag_enum_arg);
    for (j = 0; j < n; ++j)
    {
        for (i = 0; i < m; ++i)
            scanf("%lf", &x(j, i));
    }
    for (i = 0; i < m; ++i)
        scanf("%ld", &isx[i]);
    for (i = 0; i < m; ++i)
        scanf("%lf", &s[i]);

    /* nag_mv_distance_mat (g03eac).
     * Compute distance (dissimilarity) matrix
     */
    nag_mv_distance_mat(update, dist, scale, n, m, x, tdx, isx, s, d, &fail);
    if (fail.code != NE_NOERROR)
    {
        printf("Error from nag_mv_distance_mat (g03eac).\n%s\n",
            fail.message);
        exit_status = 1;
        goto END;
    }

    /* Print the distance matrix */

    printf("\n");

```

```

printf(" Distance Matrix ");
printf("\n");
printf("\n");
printf("      %s\n", "      1      2      3      4");
printf("\n");
for (i = 2; i <= n; ++i)
  {
    printf("%2ld      ", i);
    for (j = (i-1)*(i-2)/2+1; j <= i*(i - 1)/2; ++j)
      printf("%5.2f      ", d[j-1]);
    printf("\n");
  }

END:
NAG_FREE(d);
NAG_FREE(s);
NAG_FREE(x);
NAG_FREE(isx);

return exit_status;
}

```

## 10.2 Program Data

```

nag_mv_distance_mat (g03eac) Example Program Data
5 3
Nag_NoMatUp Nag_DistSquared Nag_NoVarScale
1.0 1.0 1.0
2.0 1.0 2.0
3.0 6.0 3.0
4.0 8.0 2.0
5.0 8.0 0.0
0 1 1
1.0 1.0 1.0

```

## 10.3 Program Results

```

nag_mv_distance_mat (g03eac) Example Program Results

```

```

Distance Matrix

      1      2      3      4

2      1.00
3      29.00     26.00
4      50.00     49.00      5.00
5      50.00     53.00     13.00      4.00

```

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