NAG Library Function Document

nag_prob_beta_dist (g01eec)

1 Purpose

nag_prob_beta_dist (g01eec) computes the upper and lower tail probabilities and the probability density function of the beta distribution with parameters a and b.

2 Specification

```
#include <nag.h>
#include <nagg01.h>
void nag_prob_beta_dist (double x, double a, double b, double tol, double *p,
     double *q, double *pdf, NagError *fail)
```

3 Description

The probability density function of the beta distribution with parameters a and b is:

$$f(B : a, b) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} B^{a-1}(1-B)^{b-1}, \quad 0 \leq B \leq 1; a, b > 0.$$

The lower tail probability, $P(B \leq \beta : a, b)$ is defined by

$$P(B \leq \beta : a, b) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} \int_0^\beta B^{a-1}(1-B)^{b-1}\, dB = I_\beta(a, b), \quad 0 \leq \beta \leq 1; a, b > 0.$$

The function $I_x(a, b)$, also known as the incomplete beta function is calculated using nag_incomplete_beta (s14ccc).

4 References

Hastings N A J and Peacock J B (1975) *Statistical Distributions* Butterworth

5 Arguments

1: **x** – double *Input*

On entry: β, the value of the beta variate.

Constraint: $0.0 \leq \mathbf{x} \leq 1.0$.

2: **a** – double *Input*

On entry: a, the first parameter of the required beta distribution.

Constraint: $0.0 < \mathbf{a} \leq 10^6$.

3: **b** – double *Input*

On entry: b, the second parameter of the required beta distribution.

Constraint: $0.0 < \mathbf{b} \leq 10^6$.

4: **tol** – double *Input*

On entry: this argument is no longer referenced, but is included for backwards compatability.

5: **p** – double * *Output*

On exit: the lower tail probability, $P(B \leq \beta : a, b)$.

6: **q** – double * *Output*

On exit: the upper tail probability, $P(B \geq \beta : a, b)$.

7: **pdf** – double * *Output*

On exit: the probability density function, $f(B : a, b)$.

8: **fail** – NagError * *Input/Output*

The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

NE_BAD_PARAM

On entry, argument ⟨*value*⟩ had an illegal value.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

NE_REAL_ARG_GT

On entry, $\mathbf{x} = \langle value \rangle$.
Constraint: $\mathbf{x} \leq 1.0$.

NE_REAL_ARG_LE

On entry, $\mathbf{a} = \langle value \rangle$ and $\mathbf{b} = \langle value \rangle$.
Constraint: $\mathbf{a} > 0.0$.

On entry, $\mathbf{a} = \langle value \rangle$ and $\mathbf{b} = \langle value \rangle$.
Constraint: $\mathbf{b} > 0.0$.

NE_REAL_ARG_LT

On entry, $\mathbf{x} = \langle value \rangle$.
Constraint: $\mathbf{x} \geq 0.0$.

7 Accuracy

The accuracy is limited by the error in the incomplete beta function. See Section 7 in nag_incomplete_beta (s14ccc) for further details.

8 Parallelism and Performance

Not applicable.

9 Further Comments

None.

10 Example

This example reads values from a number of beta distributions and computes the associated upper and lower tail probabilities and the corresponding value of the probability density function.

10.1 Program Text

```
/* nag_prob_beta_dist (g01eec) Example Program.
 *
 * Copyright 1990 Numerical Algorithms Group.
 *
 * Mark 1 1990.
 */

#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagg01.h>

int main(void)
{
  Integer  exit_status = 0;
  double   a, b, p, pdf, q, tol, x;
  NagError fail;

  INIT_FAIL(fail);

  /* Skip heading in data file */
  scanf("%*[^\n]");
  printf("nag_prob_beta_dist (g01eec) Example Program Results\n");
  printf("   x         a           b            p            q"
         "          pdf\n\n");
  while (scanf("%lf %lf %lf %lf", &x, &a, &b, &tol) != EOF)
    {
      /* nag_prob_beta_dist (g01eec).
       * Upper and lower tail probabilities and probability
       * density function for the beta distribution
       */
      nag_prob_beta_dist(x, a, b, tol, &p, &q, &pdf, &fail);
      if (fail.code != NE_NOERROR)
        {
          printf("Error from nag_prob_beta_dist (g01eec).\n%s\n",
                  fail.message);
          exit_status = 1;
          goto END;
        }
      printf("%7.4f%13.4e%13.4e%13.4e%13.4e%13.4e\n", x, a, b, p, q,
             pdf);
    }

 END:
  return exit_status;
}
```

10.2 Program Data

```
nag_prob_beta_dist (g01eec) Example Program Data
 0.25  1.0  2.0  1.9
 0.75  1.5  1.5  0.0001
 0.5   2.0  1.0  1.01
```

10.3 Program Results

```
nag_prob_beta_dist (g01eec) Example Program Results
   x         a           b            p            q          pdf

 0.2500   1.0000e+00   2.0000e+00   4.3750e-01   5.6250e-01   1.5000e+00
 0.7500   1.5000e+00   1.5000e+00   8.0450e-01   1.9550e-01   1.1027e+00
```

```
 0.5000    2.0000e+00    1.0000e+00    2.5000e-01    7.5000e-01    1.0000e+00
```