

NAG Library Function Document

nag_real_symm_eigenvalues (f02aac)

1 Purpose

nag_real_symm_eigenvalues (f02aac) calculates all the eigenvalues of a real symmetric matrix.

2 Specification

```
#include <nag.h>
#include <nagf02.h>
void nag_real_symm_eigenvalues (Integer n, double a[], Integer tda,
    double r[], NagError *fail)
```

3 Description

nag_real_symm_eigenvalues (f02aac) reduces the real symmetric matrix A to a real symmetric tridiagonal matrix using Householder's method. The eigenvalues of the tridiagonal matrix are then determined using the QL algorithm.

4 References

Wilkinson J H and Reinsch C (1971) *Handbook for Automatic Computation II, Linear Algebra* Springer-Verlag

5 Arguments

- 1: **n** – Integer *Input*
On entry: n , the order of the matrix A .
Constraint: $n \geq 1$.
- 2: **a**[$n \times tda$] – double *Input/Output*
Note: the (i, j) th element of the matrix A is stored in $\mathbf{a}[(i - 1) \times tda + j - 1]$.
On entry: the lower triangle of the n by n symmetric matrix A . The elements of the array above the diagonal need not be set.
On exit: the elements of A below the diagonal are overwritten, and the rest of the array is unchanged.
- 3: **tda** – Integer *Input*
On entry: the stride separating matrix column elements in the array \mathbf{a} .
Constraint: $tda \geq n$.
- 4: **r**[n] – double *Output*
On exit: the eigenvalues in ascending order.
- 5: **fail** – NagError * *Input/Output*
The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE_2_INT_ARG_LT

On entry, $\mathbf{tda} = \langle \text{value} \rangle$ while $\mathbf{n} = \langle \text{value} \rangle$. These arguments must satisfy $\mathbf{tda} \geq \mathbf{n}$.

NE_ALLOC_FAIL

Dynamic memory allocation failed.

NE_INT_ARG_LT

On entry, $\mathbf{n} = \langle \text{value} \rangle$.
Constraint: $\mathbf{n} \geq 1$.

NE_TOO_MANY_ITERATIONS

More than $\langle \text{value} \rangle$ iterations are required to isolate all the eigenvalues.

7 Accuracy

The accuracy of the eigenvalues depends on the sensitivity of the matrix to rounding errors produced in tridiagonalisation. For a detailed error analysis see pages 222 and 235 of Wilkinson and Reinsch (1971).

8 Parallelism and Performance

Not applicable.

9 Further Comments

The time taken by `nag_real_symm_eigenvalues` (f02aac) is approximately proportional to n^3 .

10 Example

To calculate all the eigenvalues of the real symmetric matrix

$$\begin{pmatrix} 0.5 & 0.0 & 2.3 & -2.6 \\ 0.0 & 0.5 & -1.4 & -0.7 \\ 2.3 & -1.4 & 0.5 & 0.0 \\ -2.6 & -0.7 & 0.0 & 0.5 \end{pmatrix}.$$

10.1 Program Text

```

/* nag_real_symm_eigenvalues (f02aac) Example Program.
 *
 * Copyright 1990 Numerical Algorithms Group.
 *
 * Mark 1, 1990.
 * Mark 8 revised, 2004.
 */

#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagf02.h>

#define A(I, J) a[(I) *tda + J]
int main(void)
{

    Integer  exit_status = 0, i, j, n, tda;
    NagError fail;

```

```

double    *a = 0, *r = 0;

INIT_FAIL(fail);

printf(
  "nag_real_symm_eigenvalues (f02aac) Example Program Results\n");
/* Skip heading in data file */
scanf("%*[\n]");
scanf("%ld", &n);

if (n >= 1)
  {
    if (!(a = NAG_ALLOC(n*n, double)) ||
        !(r = NAG_ALLOC(n, double)))
      {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
      }
    tda = n;
  }
else
  {
    printf("Invalid n.\n");
    exit_status = 1;
    return exit_status;
  }
for (i = 0; i < n; i++)
  for (j = 0; j < n; j++)
    scanf("%lf", &A(i, j));
/* nag_real_symm_eigenvalues (f02aac).
 * All eigenvalues of real symmetric matrix
 */
nag_real_symm_eigenvalues(n, a, tda, r, &fail);
if (fail.code != NE_NOERROR)
  {
    printf("Error from nag_real_symm_eigenvalues (f02aac).\n%s\n",
          fail.message);
    exit_status = 1;
    goto END;
  }
printf("Eigenvalues\n");
for (i = 0; i < n; i++)
  printf("%9.4f%s", r[i], (i%8 == 7 || i == n-1)? "\n": " ");
END:
NAG_FREE(a);
NAG_FREE(r);
return exit_status;
}

```

10.2 Program Data

```

nag_real_symm_eigenvalues (f02aac) Example Program Data
4
0.5  0.0  2.3 -2.6
0.0  0.5 -1.4 -0.7
2.3 -1.4  0.5  0.0
-2.6 -0.7  0.0  0.5

```

10.3 Program Results

```

nag_real_symm_eigenvalues (f02aac) Example Program Results
Eigenvalues
-3.0000  -1.0000   2.0000   4.0000

```
