

## NAG Library Function Document

### **nag\_ode\_bvp\_ps\_lin\_grid\_vals (d02uwc)**

## 1 Purpose

`nag_ode_bvp_ps_lin_grid_vals (d02uwc)` interpolates from a set of function values on a supplied grid onto a set of values for a uniform grid on the same range. The interpolation is performed using barycentric Lagrange interpolation. `nag_ode_bvp_ps_lin_grid_vals (d02uwc)` is primarily a utility function to map a set of function values specified on a Chebyshev Gauss–Lobatto grid onto a uniform grid.

## 2 Specification

```
#include <nag.h>
#include <nagd02.h>
void nag_ode_bvp_ps_lin_grid_vals (Integer n, Integer nip, const double x[],
                                   const double f[], double xip[], double fip[], NagError *fail)
```

## 3 Description

`nag_ode_bvp_ps_lin_grid_vals (d02uwc)` interpolates from a set of  $n + 1$  function values,  $f(x_i)$ , on a supplied grid,  $x_i$ , for  $i = 0, 1, \dots, n$ , onto a set of  $m$  values,  $\hat{f}(\hat{x}_j)$ , on a uniform grid,  $\hat{x}_j$ , for  $j = 1, 2, \dots, m$ . The image  $\hat{x}$  has the same range as  $x$ , so that  $\hat{x}_j = x_{\min} + ((j - 1)/(m - 1)) \times (x_{\max} - x_{\min})$ , for  $j = 1, 2, \dots, m$ . The interpolation is performed using barycentric Lagrange interpolation as described in Berrut and Trefethen (2004).

`nag_ode_bvp_ps_lin_grid_vals (d02uwc)` is primarily a utility function to map a set of function values specified on a Chebyshev Gauss–Lobatto grid computed by `nag_ode_bvp_ps_lin_cgl_grid (d02ucc)` onto an evenly-spaced grid with the same range as the original grid.

## 4 References

Berrut J P and Trefethen L N (2004) Barycentric lagrange interpolation *SIAM Rev.* **46**(3) 501–517

## 5 Arguments

1: **n** – Integer *Input*

*On entry:*  $n$ , where the number of grid points for the input data is  $n + 1$ .

*Constraint:* **n** > 0 and **n** is even.

2: **nip** – Integer *Input*

*On entry:* the number,  $m$ , of grid points in the uniform mesh  $\hat{x}$  onto which function values are interpolated. If **nip** = 1 then on successful exit from `nag_ode_bvp_ps_lin_grid_vals (d02uwc)`, **fip[0]** will contain the value  $f(x_n)$ .

*Constraint:* **nip** > 0.

3: **x[n + 1]** – const double *Input*

*On entry:* the grid points,  $x_i$ , for  $i = 0, 1, \dots, n$ , at which the function is specified.

Usually this should be the array of Chebyshev Gauss–Lobatto points returned in `nag_ode_bvp_ps_lin_cgl_grid (d02ucc)`.

|   |                                |                     |
|---|--------------------------------|---------------------|
| 4:  | <b>f[n + 1]</b> – const double | <i>Input</i>        |
| <i>On entry:</i> the function values, $f(x_i)$ , for $i = 0, 1, \dots, n$ .   |                                |                     |
| 5:  | <b>xip[nip]</b> – double       | <i>Output</i>       |
| <i>On exit:</i> the evenly-spaced grid points, $\hat{x}_j$ , for $j = 1, 2, \dots, m$ .   |                                |                     |
| 6:  | <b>fip[nip]</b> – double       | <i>Output</i>       |
| <i>On exit:</i> the set of interpolated values $\hat{f}(\hat{x}_j)$ , for $j = 1, 2, \dots, m$ . Here $\hat{f}(\hat{x}_j) \approx f(x = \hat{x}_j)$ . |                                |                     |
| 7:  | <b>fail</b> – NagError *       | <i>Input/Output</i> |
| The NAG error argument (see Section 3.6 in the Essential Introduction).   |                                |                     |

## 6 Error Indicators and Warnings

### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

### NE\_INT

On entry,  $\mathbf{n} = \langle value \rangle$ .  
Constraint:  $\mathbf{n} > 0$ .

On entry,  $\mathbf{n} = \langle value \rangle$ .  
Constraint:  $\mathbf{n}$  is even.

On entry,  $\mathbf{nip} = \langle value \rangle$ .  
Constraint:  $\mathbf{nip} > 0$ .

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

## 7 Accuracy

nag\_ode\_bvp\_ps\_lin\_grid\_vals (d02uwc) is intended, primarily, for use with Chebyshev Gauss–Lobatto input grids. For such input grids and for well-behaved functions (no discontinuities, peaks or cusps), the accuracy should be a small multiple of *machine precision*.

## 8 Parallelism and Performance

Not applicable.

## 9 Further Comments

None.

## 10 Example

This example interpolates the function  $x + \cos(5x)$ , as specified on a 65-point Gauss–Lobatto grid on  $[-1, 1]$ , onto a coarse uniform grid.

## 10.1 Program Text

```
/* nag_ode_bvp_ps_lin_grid_vals (d02uwc) Example Program.
*
* Copyright 2011, Numerical Algorithms Group.
*
* Mark 23, 2011.
*/
#include <math.h>
#include <nag.h>
#include <nag_stdl�.h>
#include <nagd02.h>
#include <nagx02.h>

#ifndef __cplusplus
extern "C" {
#endif
    static double NAG_CALL exact(double x);
#ifndef __cplusplus
}
#endif
int main(void)
{
    /* Scalars */
    Integer      exit_status = 0;
    Integer      i, n, nip;
    double       a = -1.0, b = 1.0;
    double       uerr = 0.0;
    double       tenepr = 10.0 * nag_machine_precision;
    /* Arrays */
    double       *f = 0, *fip = 0, *x = 0, *xip = 0;
    /* NAG types */
    Nag_Boolean  reqerr = Nag_FALSE;
    NagError     fail;

    INIT_FAIL(fail);

    printf("nag_ode_bvp_ps_lin_grid_vals (d02uwc) Example Program Results\n\n");

    /* Skip heading in data file */
    scanf("%*[^\n] ");
    scanf("%"NAG_IFMT "%*[^\n] ", &n);
    scanf("%"NAG_IFMT "%*[^\n] ", &nip);
    if (
        !(f = NAG_ALLOC((n + 1), double)) ||
        !(fip = NAG_ALLOC((nip), double)) ||
        !(xip = NAG_ALLOC((nip), double)) ||
        !(x = NAG_ALLOC((n + 1), double))
    )
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    /* Set up solution grid:
     * nag_ode_bvp_ps_lin_cgl_grid (d02ucc).
     * Generate Chebyshev Gauss-Lobatto grid.
     */
    nag_ode_bvp_ps_lin_cgl_grid(n, a, b, x, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_ode_bvp_ps_lin_cgl_grid (d02ucc).\n%s\n",
               fail.message);
        exit_status = 1;
        goto END;
    }

    /* Set up problem right hand sides for grid. */
    for (i = 0; i < n + 1; i++) f[i] = exact(x[i]);
```

```

/* Map to an equally spaced grid:
 * nag_ode_bvp_ps_lin_grid_vals (d02uwc).
 * Interpolate a function from Chebyshev grid to uniform grid
 * using barycentric Lagrange interpolation.
 */
nag_ode_bvp_ps_lin_grid_vals(n, nip, x, f, xip, fip, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_ode_bvp_ps_lin_grid_vals (d02uwc).\n%n\n",
           fail.message);
    exit_status = 1;
    goto END;
}

/* Print solution.*/
printf("Numerical solution f\n\n");
printf("      x          f\n");
for (i = 0; i < nip; i++) printf("%10.4f %10.4f\n", xip[i], fip[i]);

if (reqerr) {
    for (i = 0; i < nip; i++) uerr = MAX(uerr, fabs(fip[i] - exact(xip[i])));
    printf("f is within a multiple %"NAG_IFMT " of machine precision.\n",
           10 * ((Integer) (uerr/teneeps) + 1));
}
END:
NAG_FREE(f);
NAG_FREE(fip);
NAG_FREE(x);
NAG_FREE(xip);
return exit_status;
}

static double NAG_CALL exact(double x)
{
    return x + cos(5.0 * x);
}

```

## 10.2 Program Data

```
nag_ode_bvp_ps_lin_grid_vals (d02uwc) Example Program Data
 64          : n
 17          : nip
```

## 10.3 Program Results

```
nag_ode_bvp_ps_lin_grid_vals (d02uwc) Example Program Results
```

Numerical solution f

| x       | f       |
|---------|---------|
| -1.0000 | -0.7163 |
| -0.8750 | -1.2060 |
| -0.7500 | -1.5706 |
| -0.6250 | -1.6249 |
| -0.5000 | -1.3011 |
| -0.3750 | -0.6745 |
| -0.2500 | 0.0653  |
| -0.1250 | 0.6860  |
| 0.0000  | 1.0000  |
| 0.1250  | 0.9360  |
| 0.2500  | 0.5653  |
| 0.3750  | 0.0755  |
| 0.5000  | -0.3011 |
| 0.6250  | -0.3749 |
| 0.7500  | -0.0706 |
| 0.8750  | 0.5440  |
| 1.0000  | 1.2837  |