NAG Library Function Document

nag sum fft hermitian 3d (c06pzc)

1 Purpose

nag_sum_fft_hermitian_3d (c06pzc) computes the three-dimensional inverse discrete Fourier transform of a trivariate Hermitian sequence of complex data values.

2 Specification

3 Description

nag_sum_fft_hermitian_3d (c06pzc) computes the three-dimensional inverse discrete Fourier transform of a trivariate Hermitian sequence of complex data values $z_{j_1j_2j_3}$, for $j_1=0,1,\ldots,n_1-1$, $j_2=0,1,\ldots,n_2-1$ and $j_3=0,1,\ldots,n_3-1$.

The discrete Fourier transform is here defined by

$$\hat{x}_{k_1k_2k_3} = \frac{1}{\sqrt{n_1n_2n_3}} \sum_{j_1=0}^{n_1-1} \sum_{j_2=0}^{n_2-1} \sum_{j_3=0}^{n_3-1} z_{j_1j_2j_3} \times \exp\left(2\pi i \left(\frac{j_1k_1}{n_1} + \frac{j_2k_2}{n_2} + \frac{j_3k_3}{n_3}\right)\right),$$

where $k_1 = 0, 1, ..., n_1 - 1$, $k_2 = 0, 1, ..., n_2 - 1$ and $k_3 = 0, 1, ..., n_3 - 1$. (Note the scale factor of $\frac{1}{\sqrt{n_1 n_2 n_3}}$ in this definition.)

Because the input data satisfies conjugate symmetry (i.e., $z_{k_1k_2k_3}$ is the complex conjugate of $z_{(n_1-k_1)k_2k_3}$), the transformed values $\hat{x}_{k_1k_2k_3}$ are real.

A call of nag_sum_fft_real_3d (c06pyc) followed by a call of nag_sum_fft_hermitian_3d (c06pzc) will restore the original data.

This function performs multiple one-dimensional discrete Fourier transforms by the fast Fourier transform (FFT) algorithm in Brigham (1974) and Temperton (1983).

4 References

Brigham E O (1974) The Fast Fourier Transform Prentice-Hall

Temperton C (1983) Fast mixed-radix real Fourier transforms J. Comput. Phys. 52 340-350

5 Arguments

1: **n1** – Integer Input

On entry: n_1 , the first dimension of the transform.

Constraint: $\mathbf{n1} \geq 1$.

2: **n2** – Integer Input

On entry: n_2 , the second dimension of the transform.

Constraint: $n2 \ge 1$.

Mark 24 c06pzc.1

c06pzc NAG Library Manual

3: **n3** – Integer Input

On entry: n_3 , the third dimension of the transform.

Constraint: $\mathbf{n3} \geq 1$.

4: $\mathbf{y}[dim]$ – const Complex

Input

Note: the dimension, dim, of the array y must be at least $(n1/2 + 1) \times n2 \times n3$.

On entry: the Hermitian sequence of complex input dataset z, where $z_{j_1j_2j_3}$ is stored in $\mathbf{y}[j_3 \times (n_1/2+1)n_2 + j_2 \times (n_1/2+1) + j_1]$, for $j_1 = 0, 1, \dots, n_1/2$, $j_2 = 0, 1, \dots, n_2 - 1$ and $j_3 = 0, 1, \dots, n_3 - 1$.

5: $\mathbf{x}[\mathbf{n1} \times \mathbf{n2} \times \mathbf{n3}] - \text{double}$

Output

On exit: the real output dataset \hat{x} , where $\hat{x}_{k_1k_2k_3}$ is stored in $\mathbf{x}[k_3 \times n_1n_2 + k_2 \times n_1 + k_1]$, for $k_1 = 0, 1, \dots, n_1 - 1, k_2 = 0, 1, \dots, n_2 - 1$ and $k_3 = 0, 1, \dots, n_3 - 1$.

6: **fail** – NagError *

Input/Output

The NAG error argument (see Section 3.6 in the Essential Introduction).

6 Error Indicators and Warnings

NE ALLOC FAIL

Dynamic memory allocation failed.

NE BAD PARAM

On entry, argument (value) had an illegal value.

NE INT

On entry, $\mathbf{n1} = \langle value \rangle$. Constraint: $\mathbf{n1} \geq 1$.

On entry, $\mathbf{n2} = \langle value \rangle$.

Constraint: $n2 \ge 1$.

On entry, $\mathbf{n3} = \langle value \rangle$. Constraint: $\mathbf{n3} \geq 1$.

NE INTERNAL ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

7 Accuracy

Some indication of accuracy can be obtained by performing a forward transform using nag_sum_fft_real_3d (c06pyc) and a backward transform using nag_sum_fft_hermitian_3d (c06pyc), and comparing the results with the original sequence (in exact arithmetic they would be identical).

8 Parallelism and Performance

nag_sum_fft_hermitian_3d (c06pzc) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

nag_sum_fft_hermitian_3d (c06pzc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

c06pzc.2 Mark 24

Please consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

The time taken by nag_sum_fft_hermitian_3d (c06pzc) is approximately proportional to $n_1n_2n_3\log(n_1n_2n_3)$, but also depends on the factors of n_1 , n_2 and n_3 . nag_sum_fft_hermitian_3d (c06pzc) is fastest if the only prime factors of n_1 , n_2 and n_3 are 2, 3 and 5, and is particularly slow if one of the dimensions is a large prime, or has large prime factors.

Workspace is internally allocated by nag_sum_fft_hermitian_3d (c06pzc). The total size of these arrays is approximately proportional to $n_1n_2n_3$.

10 Example

See Section 10 in nag sum fft real 3d (c06pyc).

Mark 24 c06pzc.3 (last)